

Spyros Chatzivasileiadis

Data-driven applications for power system security assessment

Spot the difference!



North East Blackout 2003



- North East Blackout 2003
- Affected 55 million people in the US and Canada
- Estimated cost of 7-10 billion USD
- Took 2 days (!) for full restoration!



Blackouts are **rare** but **costly!**

- Frequency of power interruptions
 - 1 hour per year
- Economic damage from power interruptions
 - about 80 billion USD/year (US only, 2005)
- Total electric energy cost in the US:
 - 370 billion USD/year

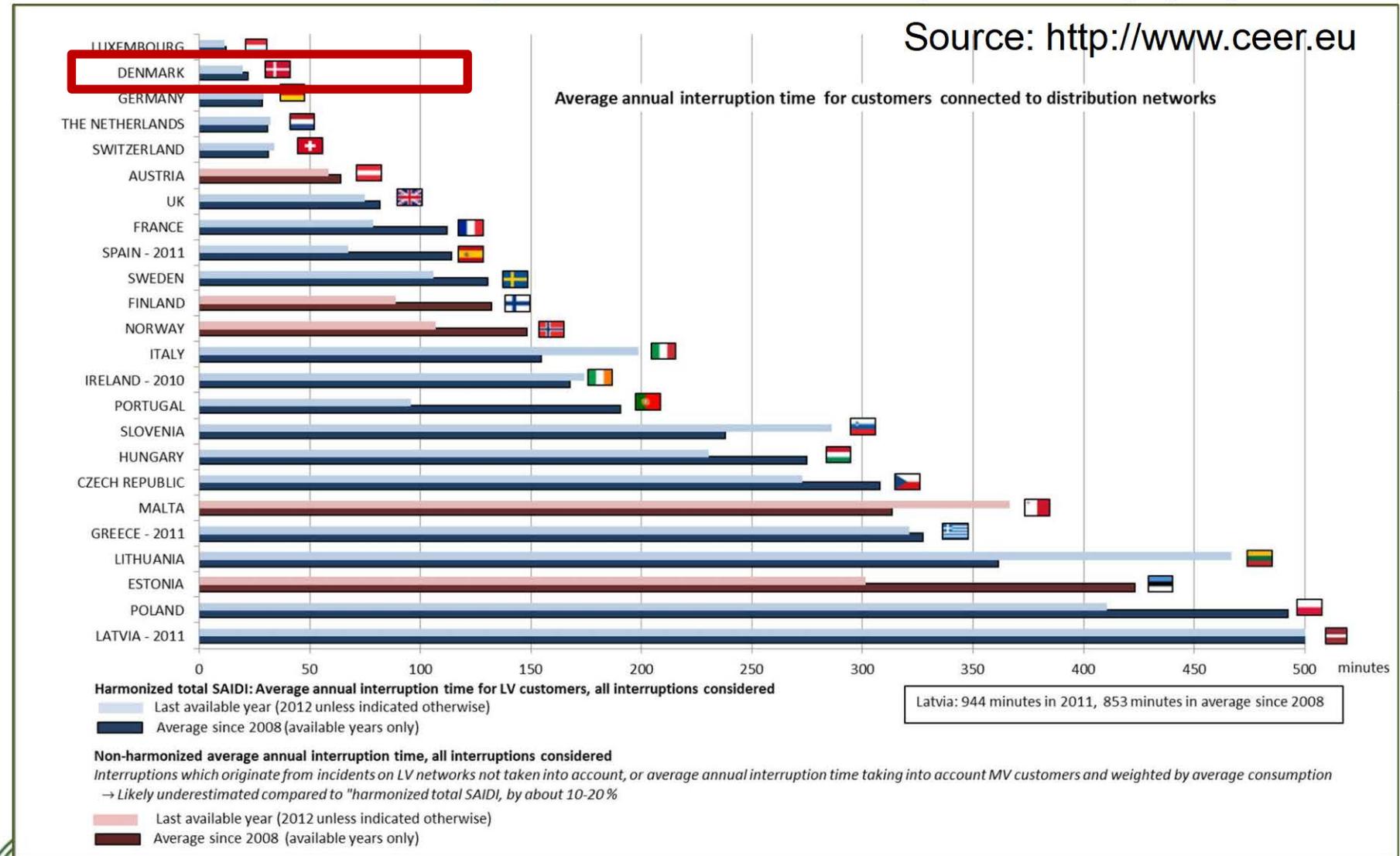
India Blackout 2012 →
affected 700 million people (!)



*Affected
regions
in red*

Average annual interruption time in European countries (2012 data)

Source: M. Bollen, W. Friedl, PES GM 2014
<http://grouper.ieee.org/groups/td/dist/sd/doc/2014-08%20European%20Benchmarking%20Report%20on%20Quality%20of%20Supply-%20Mathew%20Bollen+Werner%20Friedl.pdf>



Operators run every day a security assessment



Energinet Control Room, Denmark

- Security = ability to withstand disturbances
- Security Assessment:
 - Screen contingency list every 15 mins
 - Prepare contingency plans for critical scenarios
- Run both:
 - **Steady-state**, i.e. power flows to check N-1 and violation of limits
 - **Dynamic** simulations

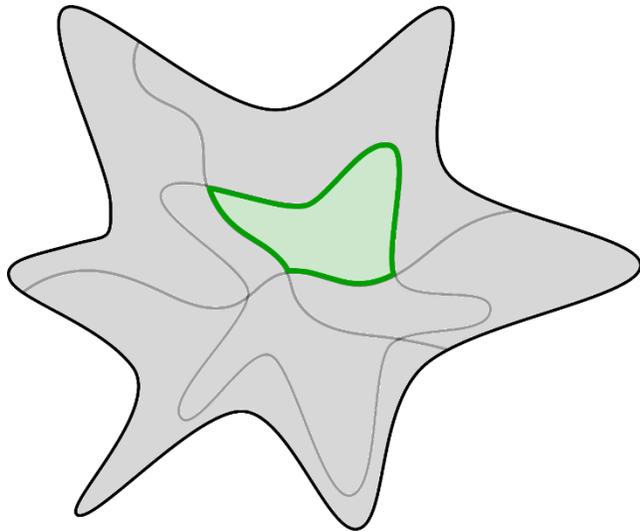
Challenges

- Dynamic simulations are hard
 - System of differential-algebraic equations with 10k degrees of freedom
- Checking for N-k contingencies is a hard combinatorial problem
 - Usually computationally impossible to check even for all N-2 in a realistic systems with thousands of buses
- The safe operating region is a non-linear non-convex region
 - Impossible to use analytical tricks to determine it

So.... what do we do?

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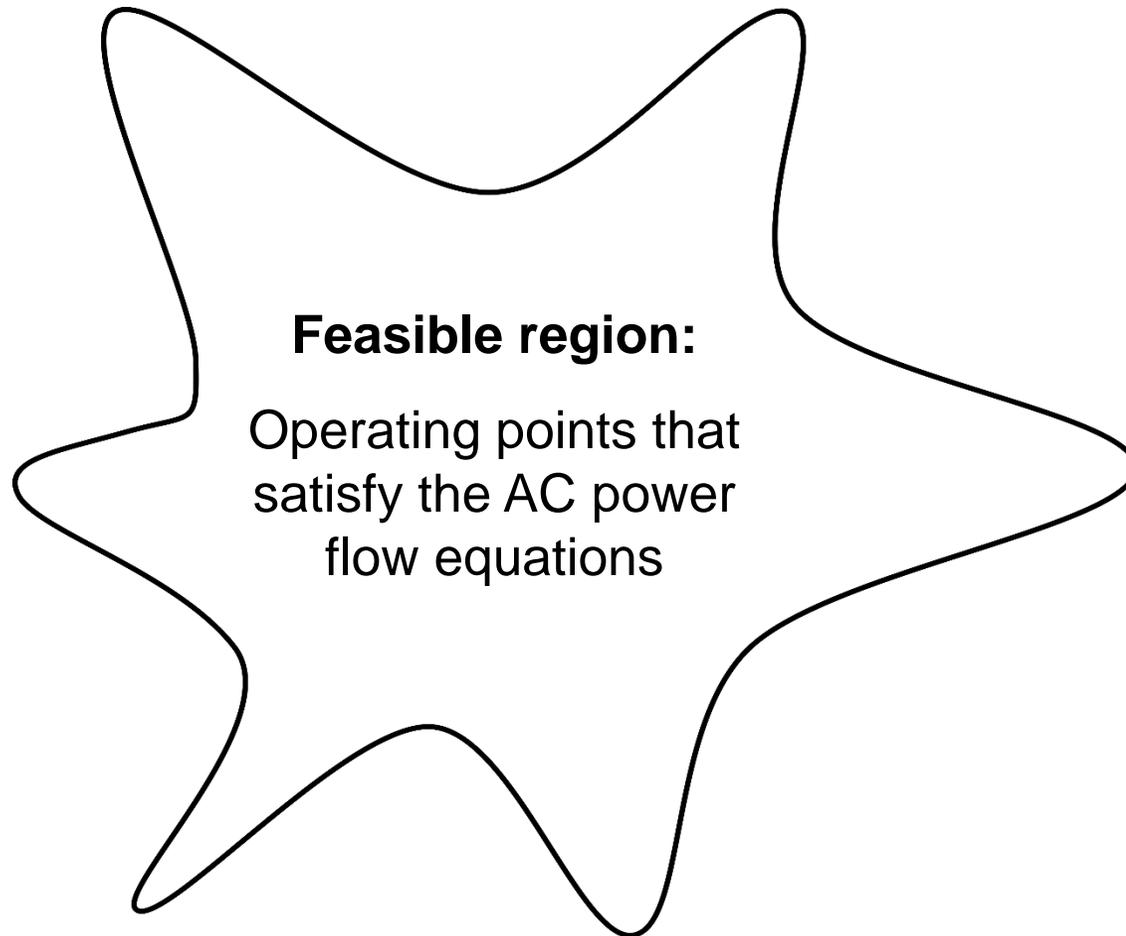
Identifying the power system security region



- Run a lot of **simulations** assessing each operating point
 - Several approaches for efficient approximations to boost computation speed
- **Stability certificates**
 - Extract **sufficient conditions** for sub-areas of the security region
- **Machine learning** approaches
 - Train for a given dataset and **infer** for all new points

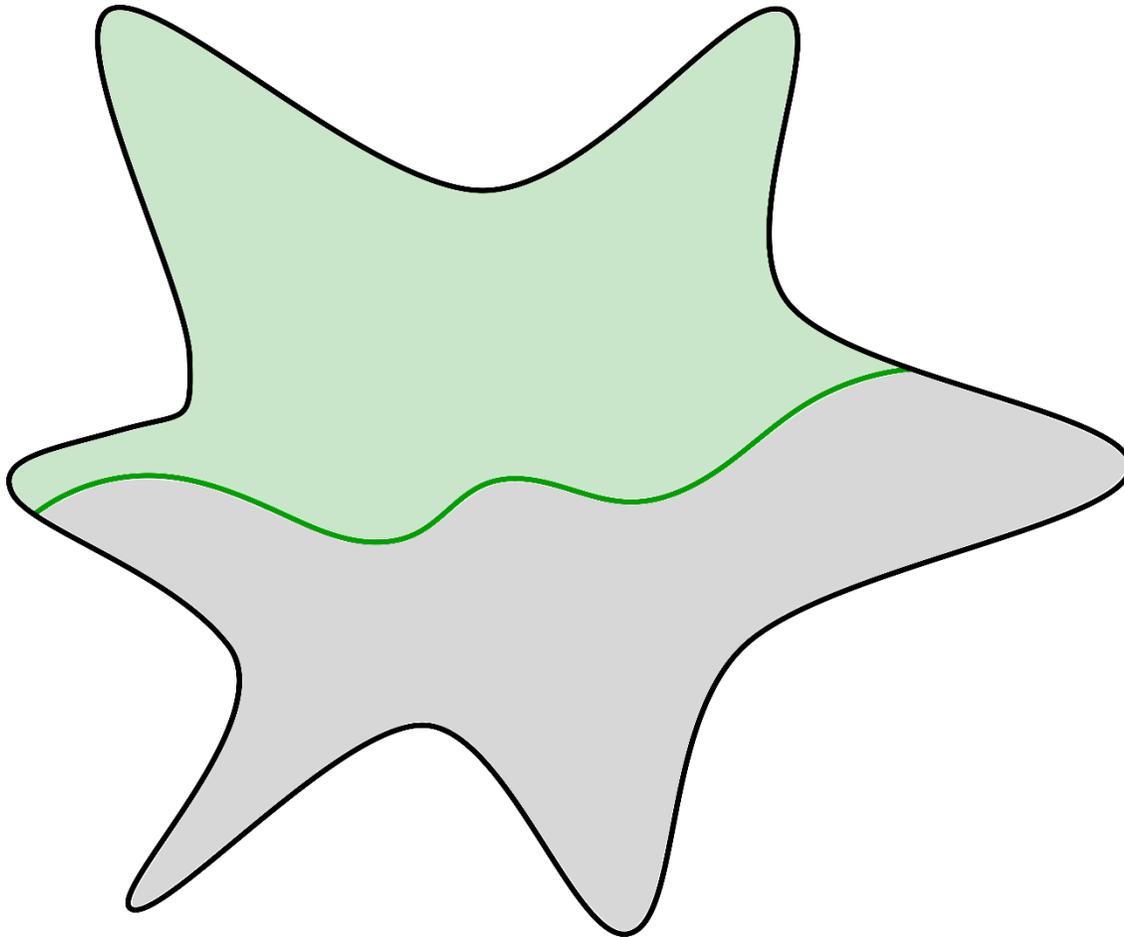
Power System Security Assessment

The safe operating region of power system operations



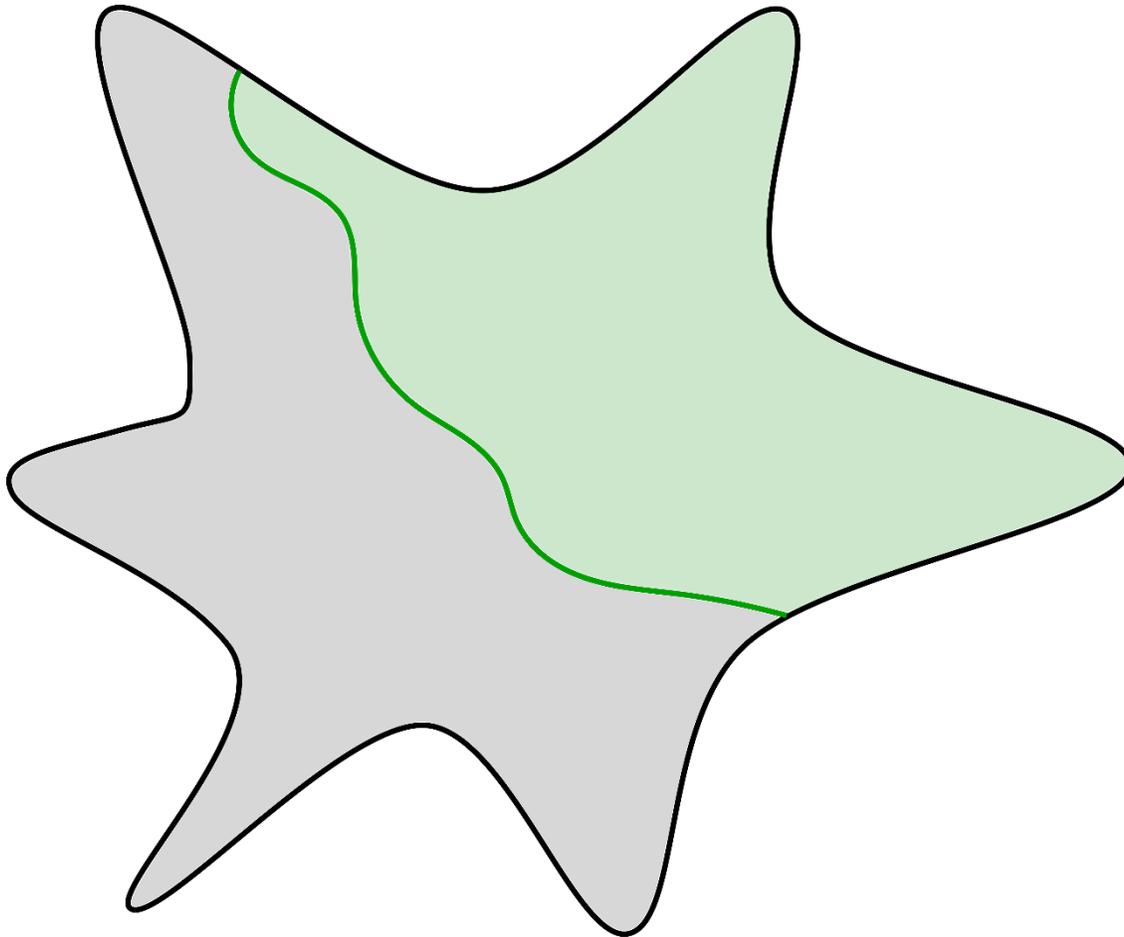
- Non-linear and non-convex AC power flow equations
- Component limits

The feasible space of power system operations



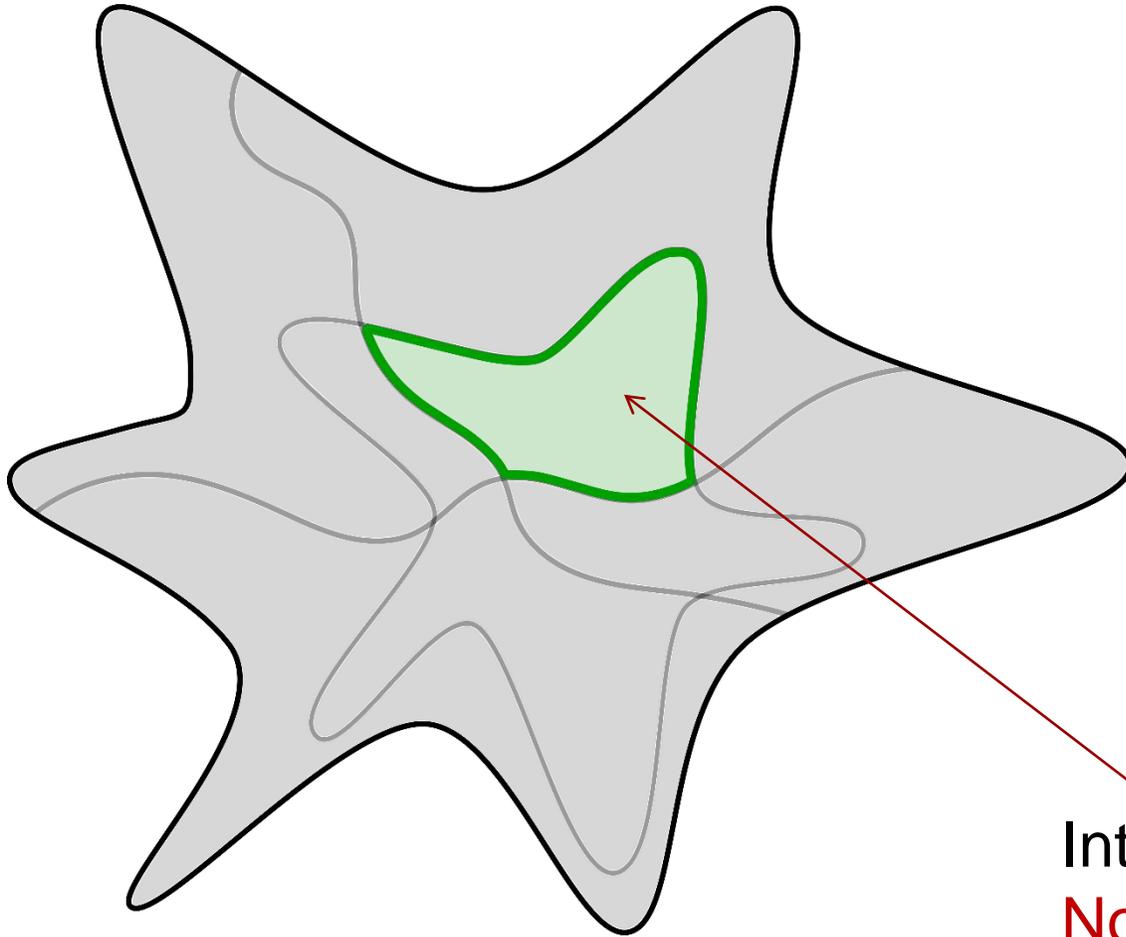
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The feasible space of power system operations



- Non-linear and non-convex AC power flow equations
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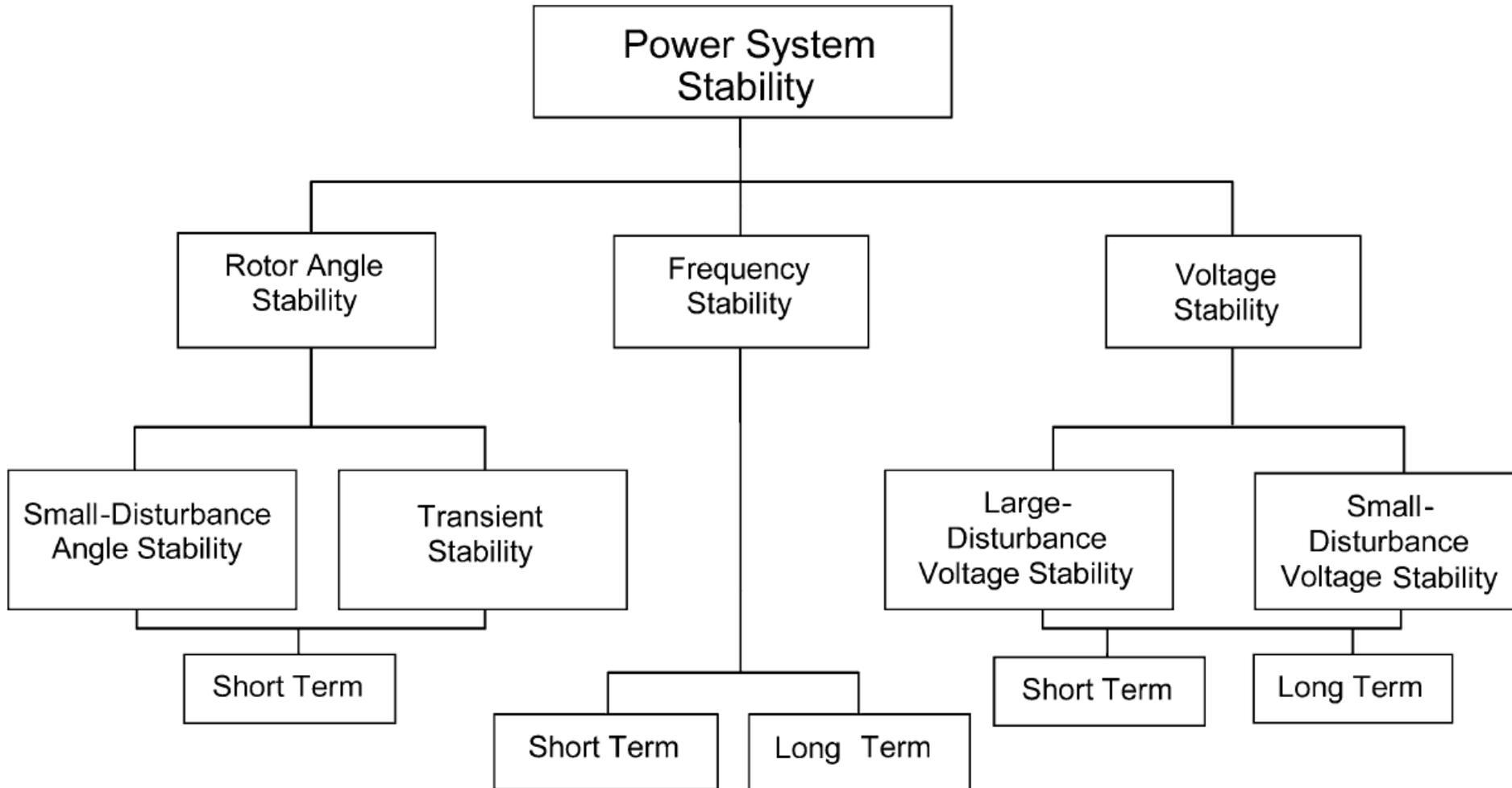
The feasible space of power system operations



- Non-linear and non-convex AC power flow equations
- Component limits
- + N-1 security criterion
- + Stability Limits

Intersection of all security/stability criteria:
Non-linear and **non-convex** security region

Operators have to check for all instability types



AND steady-state security!

N-1
contingency
analysis
through power
flows

Focus of this lecture:

Machine Learning for Power System Security Assessment

- Decision Trees
 - First proposed by Louis Wehenkel (Univ of Liege) in the '90s
 - Very successful
 - Applications in the industry
 - Research is still ongoing; latest focus is on interpretability (remember Dolores's talk? 😊)
- Neural networks
- Deep Neural Networks (same as neural networks but deep 😊)
 - One paper on feature extraction (Sun, Konstantelos, Strbac, 2018)
 - One paper inspired by image processing (Hidalgo, Hancharou, Thams, Chatzivasileiadis, 2019)

Machine learning applications

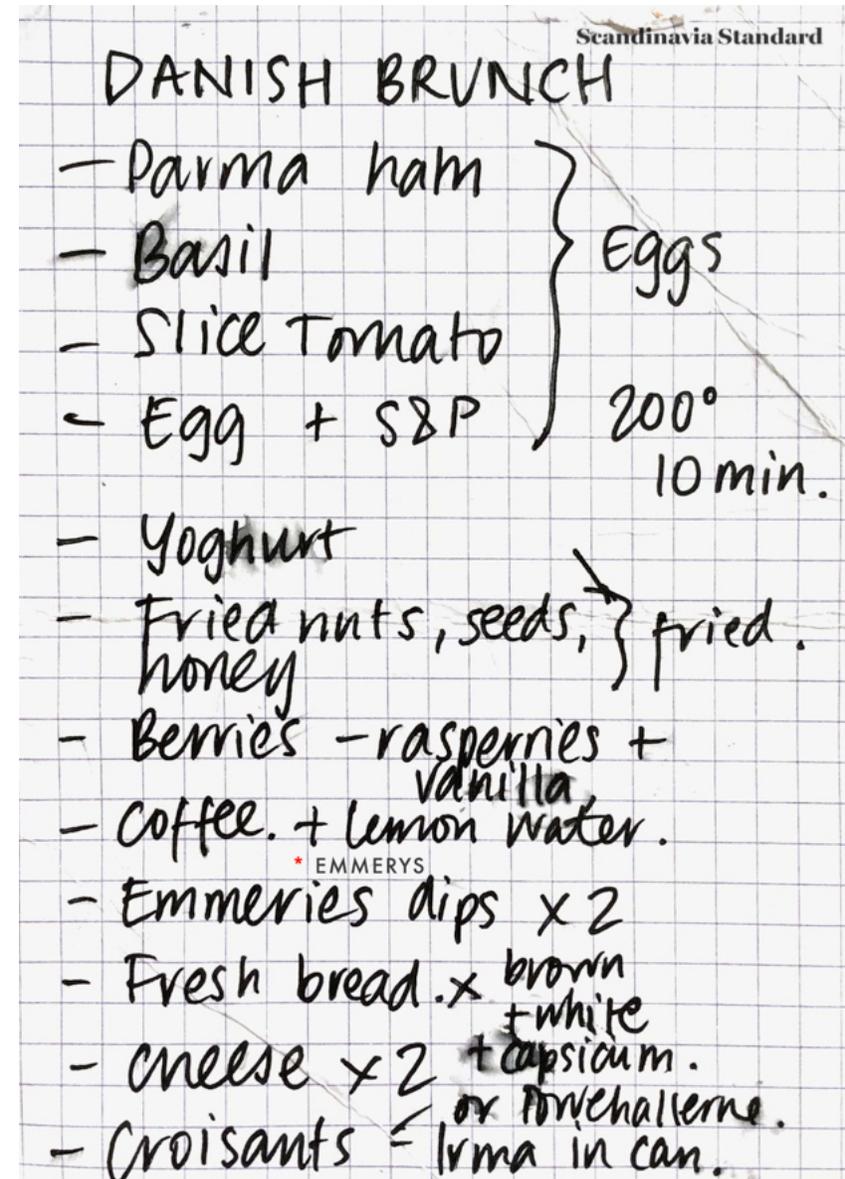
(for power system security assessment)

A very short overview

The ingredients

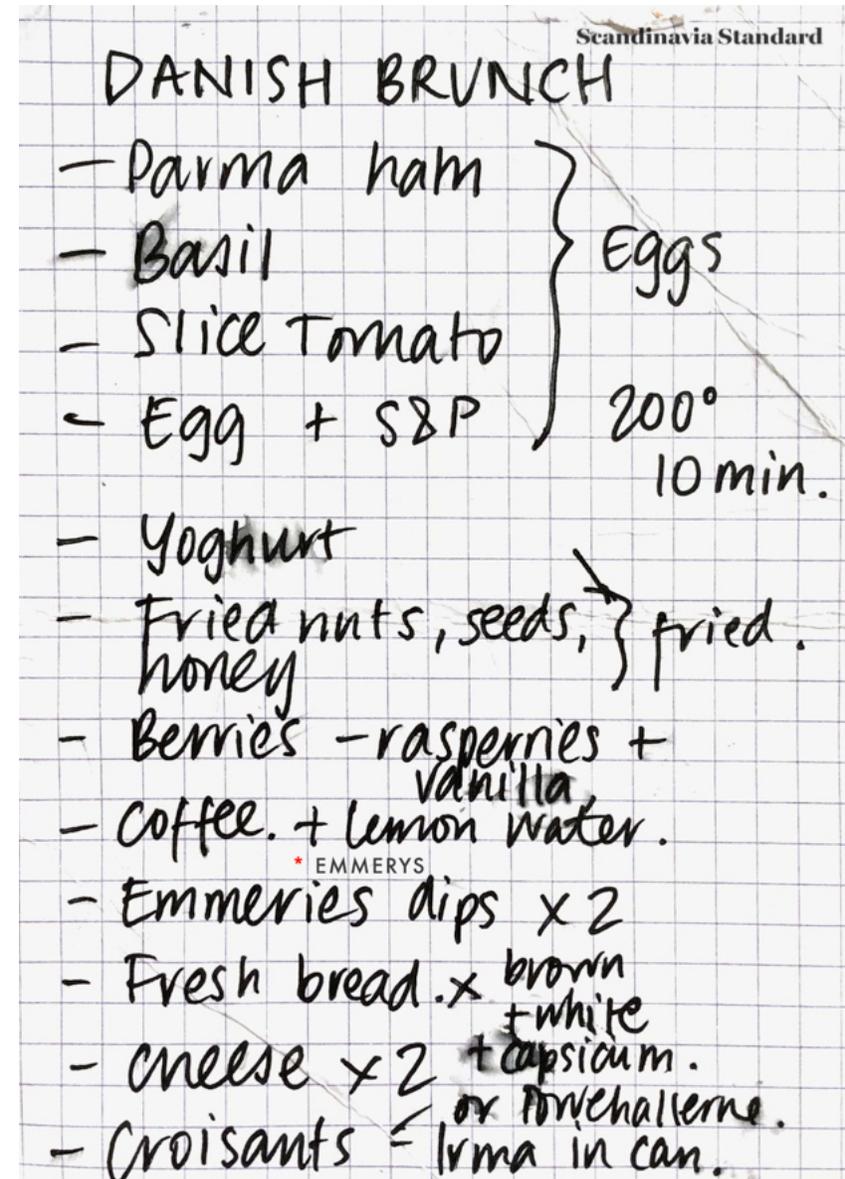
What do we need?

If we want to apply machine learning approaches for power system security



The ingredients

- A training database
- A training algorithm
- A test database
 - To test accuracy of the approach



Test Database

Test Database

Traditionally:

- Split training database to e.g. 80% training samples and 20% test samples
- Train with the 80%
- Test with the 20%

Modern toolboxes have this integrated and automatized → only need to provide a training database

Point to remember:

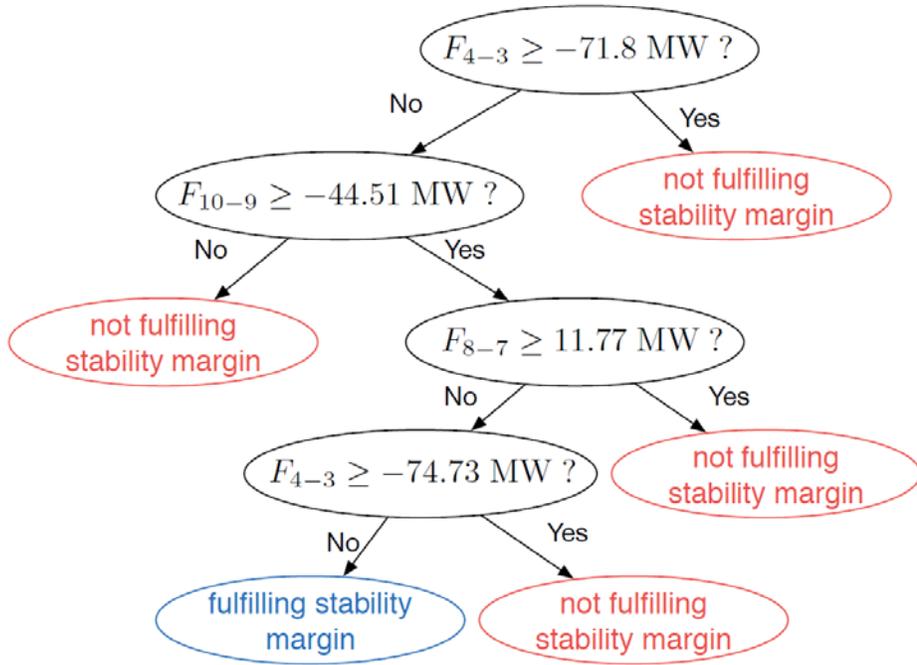
The test database determines the performance of your method. If the test data come from the same simulations as your training data, the accuracy can be deceptively high. Would it be equally high in reality?

Ideally → use a different real-life dataset

(Unfortunately, not always possible)

Training a neural network

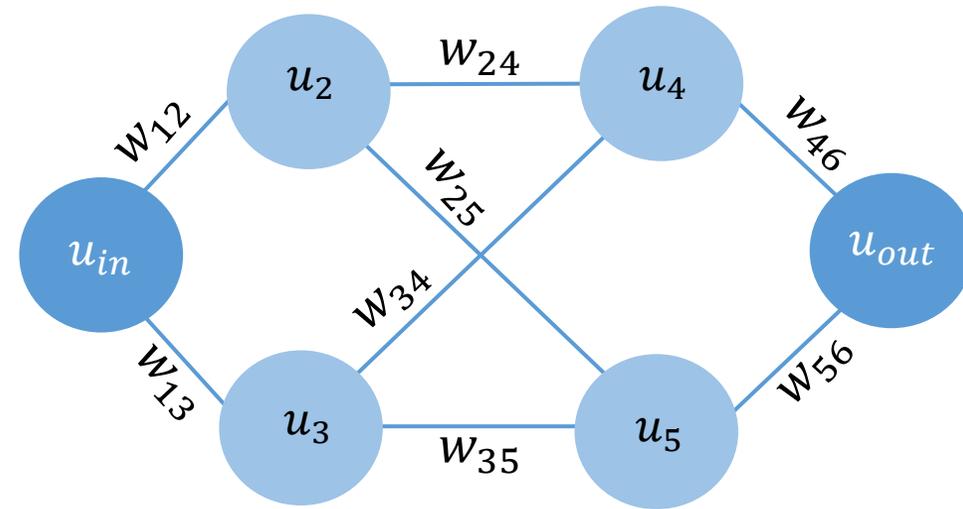
Decision Trees



- Decision rules
 - If $\text{line_flow} > \text{FF}$ then else...

F. Thams, L. Halilbašić, P. Pinson, S. Chatzivasileiadis, and R. Eriksson, "Data-driven security-constrained OPF," in *10th IREP Symposium – Bulk Power Systems Dynamics and Control*, 2017.

Neural Networks



- Linear weights
- On every node: a non-linear activation function
 - e.g **RELU**: $u_j = \max(0, w_{ij}x_i + b_i)$
 - Many other possibilities, e.g. sigmoid function and others

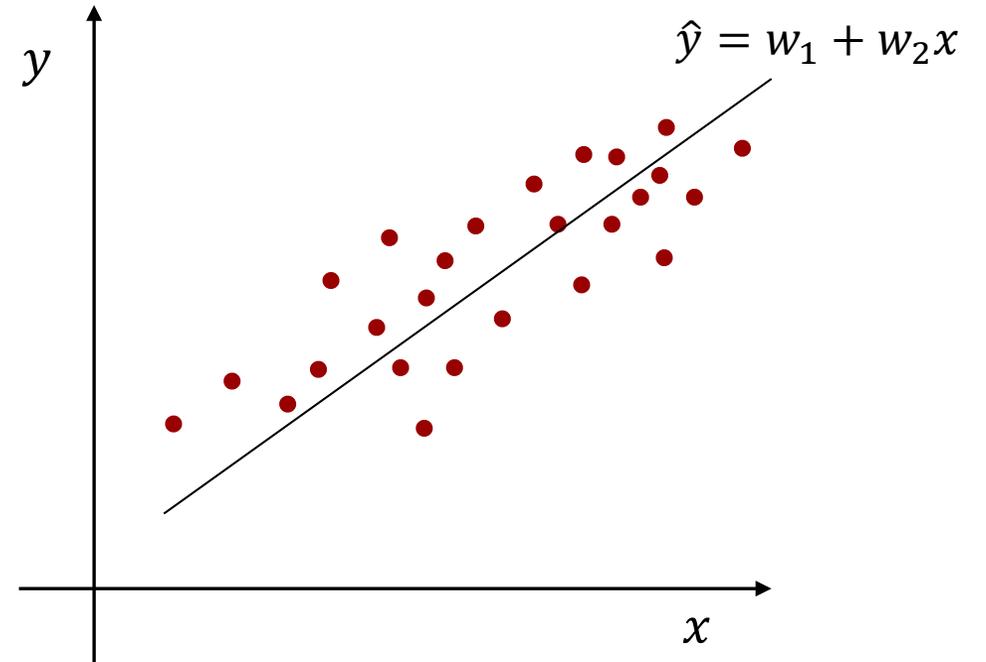
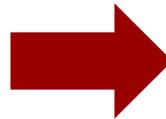
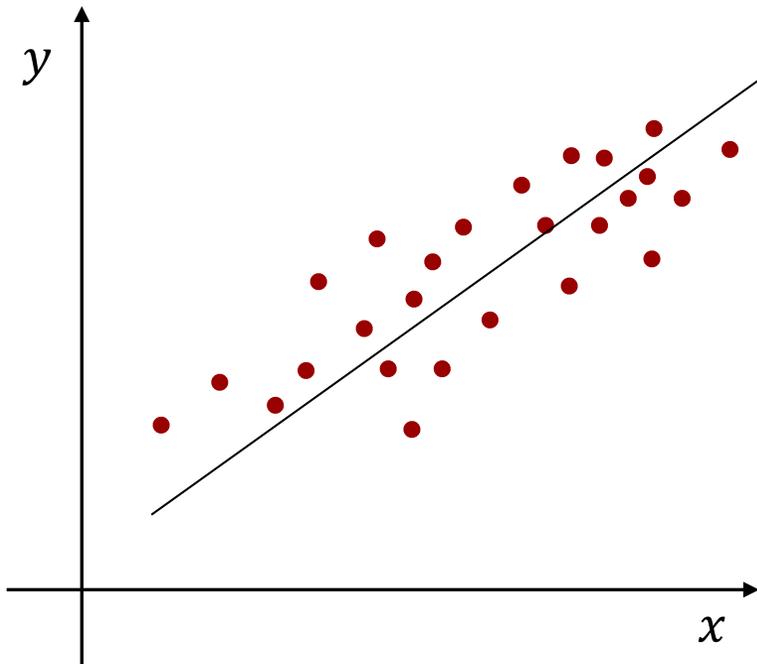
Training a neural network

- Batch size vs Iterations vs Epochs
- Loss function
- Evaluation of performance
 - Confusion matrix
 - Performance metrics

Batch size vs Iterations vs Epochs

Example from linear regression;
neural network works similarly

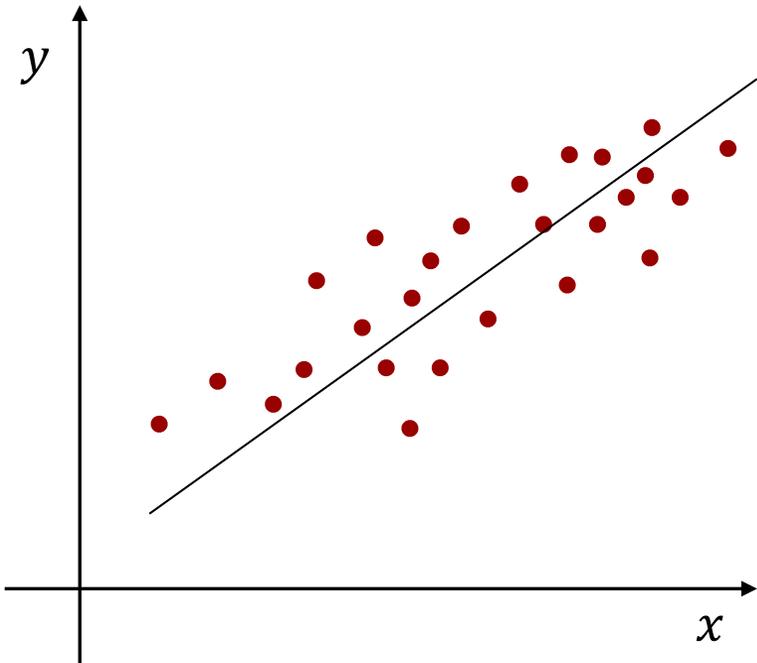
Goal: *estimate* w_1, w_2 to fit $\hat{y} = w_1 + w_2x$



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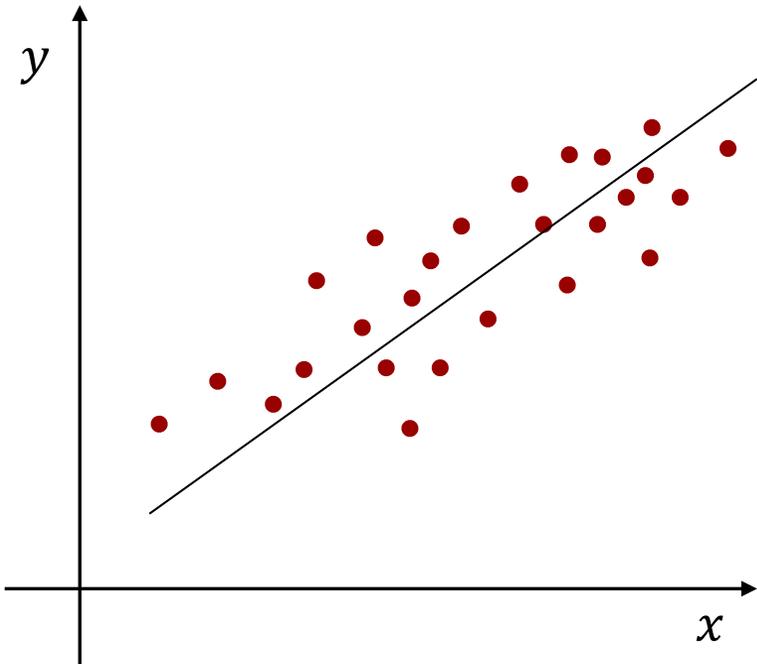


- Ideally we want to enter all our data in our linear regression algorithm to estimate w_1, w_2
- But, the size of data can be immense!
- That's why we need to split our dataset in **batches**

Batch size vs Iterations vs Epochs

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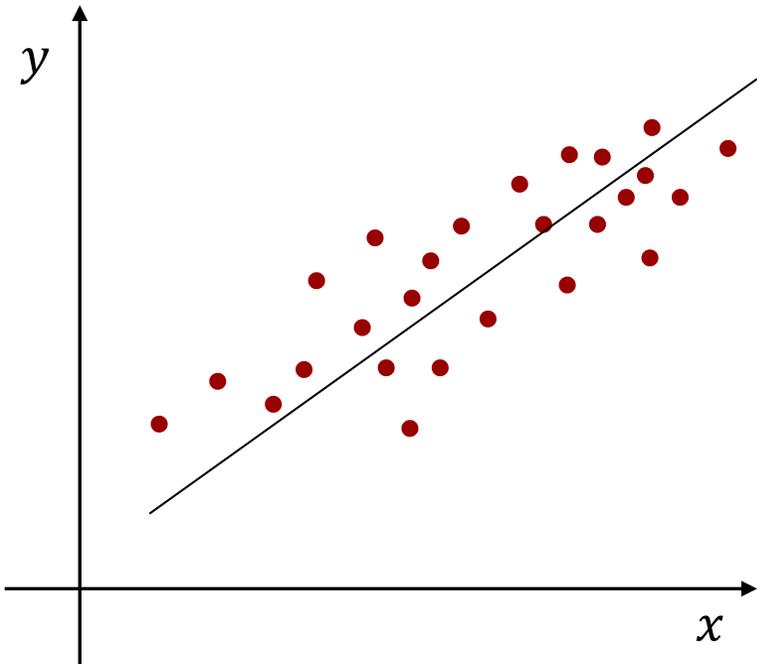


- Ideally we want to enter all our data in our linear regression algorithm to estimate w_1, w_2
- But, the size of data can be immense!
- That's why we need to split our dataset in **batches**
- Total **#data = batch_size * iterations**
e.g. if 1000 datapoints and batch_size=200,
then $1000=200*5$ iterations

Batch size vs Iterations vs Epochs

Example from linear regression;
neural network works similarly

Goal: estimate w_1, w_2 to fit $\hat{y} = w_1 + w_2x$



More info:

<https://towardsdatascience.com/epoch-vs-iterations-vs-batch-size-4dfb9c7ce9c9>

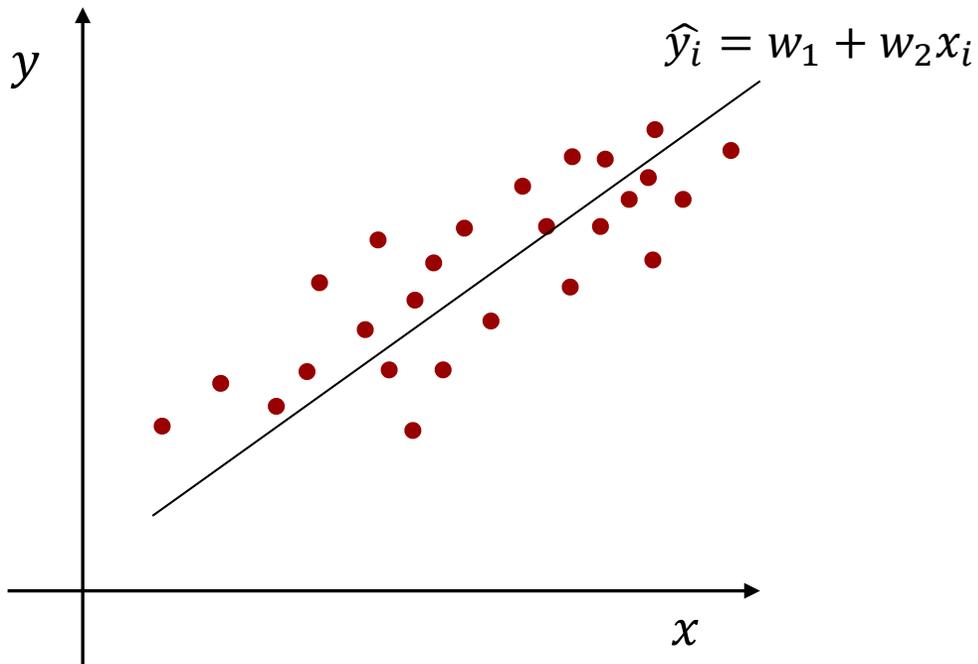
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- But, the size of data can be immense!
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- Total **#data = batch_size * iterations**
e.g. if 1000 datapoints and batch_size=200, then $1000=200*5$ iterations
- **Epochs**: passing the whole dataset only once is not enough!
 - 1 Epoch = passing the dataset through the neural network ONCE

Loss function:

To find the best estimates for w_1, w_2
we need to run an optimization!

y_i : actual/correct value

\hat{y}_i : estimated value



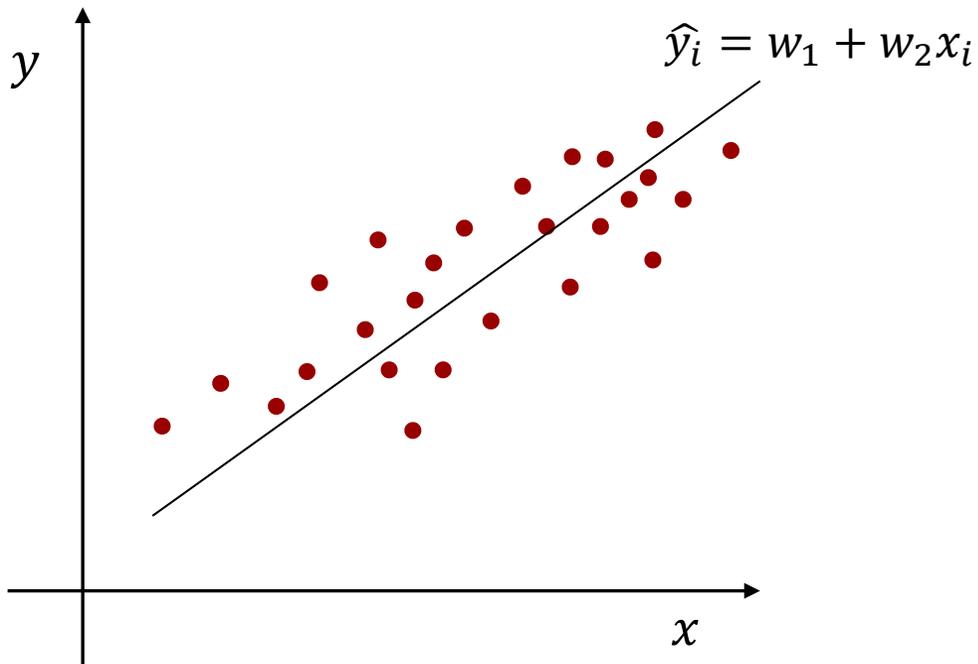
$$\begin{aligned} & \min_{w_1, w_2} \|y_i - \hat{y}_i\| \\ \text{s.t.} \quad & \hat{y}_i = w_1 + w_2 x_i \quad \forall i \end{aligned}$$

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Rewrite:

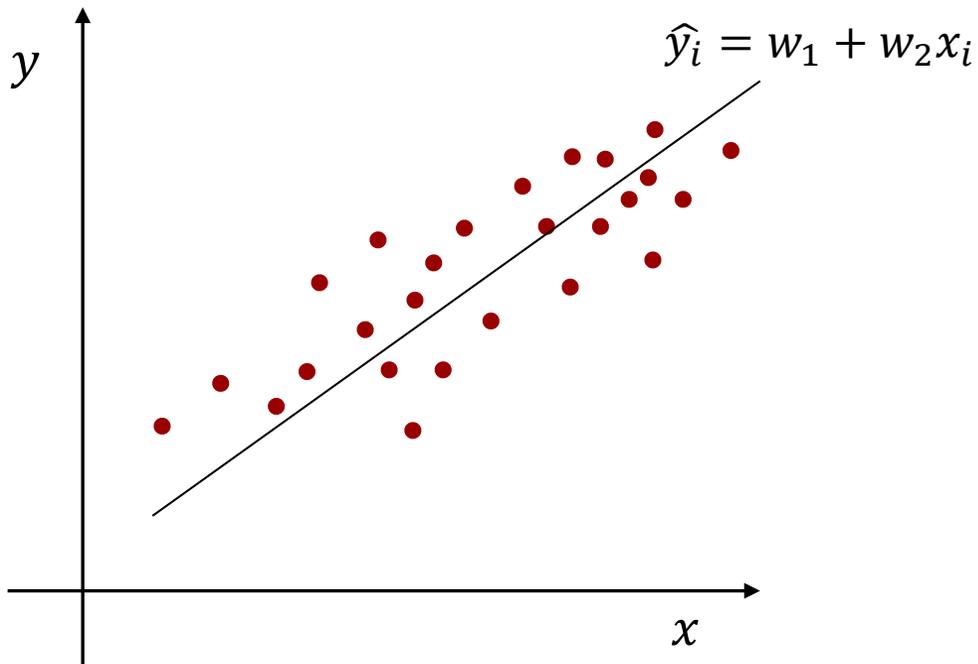
$$\min_{w_1, w_2} \|y_i - (w_1 + w_2 x_i)\| \quad \forall i$$

Loss function:

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Rewrite:

$$\min_{w_1, w_2} \|y_i - (w_1 + w_2 x_i)\| \quad \forall i$$

What cost function shall we use?

Cost function (often called “**Loss function**”)

- A series of different options:

https://ml-cheatsheet.readthedocs.io/en/latest/loss_functions.html

https://isaacchanghau.github.io/post/loss_functions/

- Often used for classification problems: **cross-entropy**
- For **2 classes**, i.e. $y_i = \{0,1\}$ and $\hat{y}_i = [0,1]$:

$$\mathcal{L} = -\frac{1}{n} \sum_{i=1}^n y_i \log \hat{y}_i + (1 - y_i) \log(1 - \hat{y}_i)$$

Cross-entropy: the insights

- Insight #1: you **minimize** over the estimation errors of **all points in the batch**

$$\mathcal{L} = -\frac{1}{n} \sum_{i=1}^n y_i \log \hat{y}_i + (1 - y_i) \log(1 - \hat{y}_i)$$

- Insight #2:
 - **Actual** values: **either 0 or 1**
 - **Estimated** values: **between 0 and 1**

$$y_i = \{0,1\} \quad \text{but} \quad \hat{y}_i = [0,1]$$

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- Insight #3: **Why the minus?**

Hint: explain it for one point

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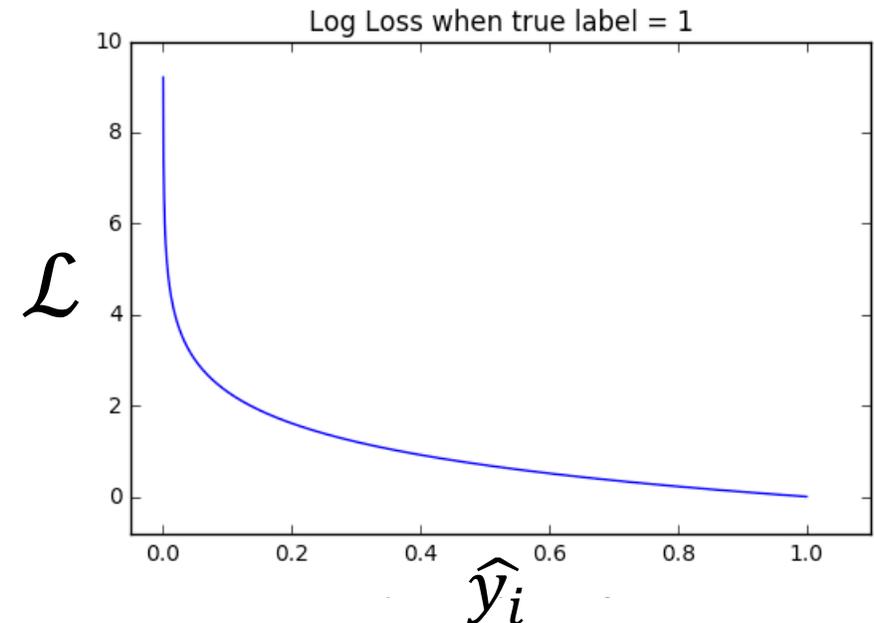
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- Insight #4: $y_i=1$, \mathcal{L} when $\hat{y}_i = [0,1]$

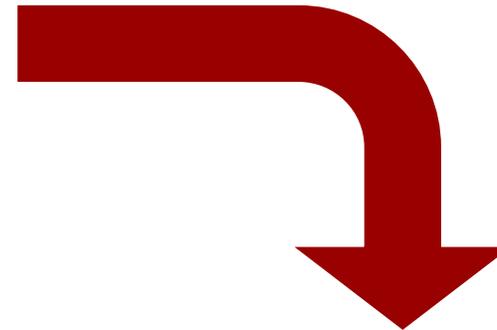


Evaluating the performance: Confusion matrix

		Target class (actual values)	
		1	0
Output class (predicted values)	1	True positive (TP)	False positive (FP)
	0	False negative (FN)	True Negative (TN)

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Classification for power system security

		Actually Safe	Actually Unsafe
		Predicted safe	True positive (TP)
Predicted Unsafe	False negative (FN)	True Negative (TN)	

Performance Metrics: Accuracy

- Accuracy: The proportion of correct classifications in the whole dataset

$$\text{Accuracy} = \frac{TP + TN}{TP + FP + TN + FN}$$

- **Example:** Assume 1000 datapoints
 - Actually safe: 500 TP=480 FP=30
 - Actually unsafe: 500 FN=20 TN=470

Accuracy = ?

	Actually Safe	Actually Unsafe
Predicted safe	True positive (TP)	False positive (FP)
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- **Example:** Assume 1000 datapoints
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$$\text{Accuracy} = \frac{480 + 470}{480 + 20 + 470 + 30} = 95\%$$

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Evaluating performance by measuring **only accuracy** is often **not enough**

Why?

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Why?

- **Example:** Assume 1000 datapoints
 - Actually safe: 20 TP= 1 FP=30
 - Actually unsafe: 980 FN= 19 TN=950

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Performance Metrics: Accuracy

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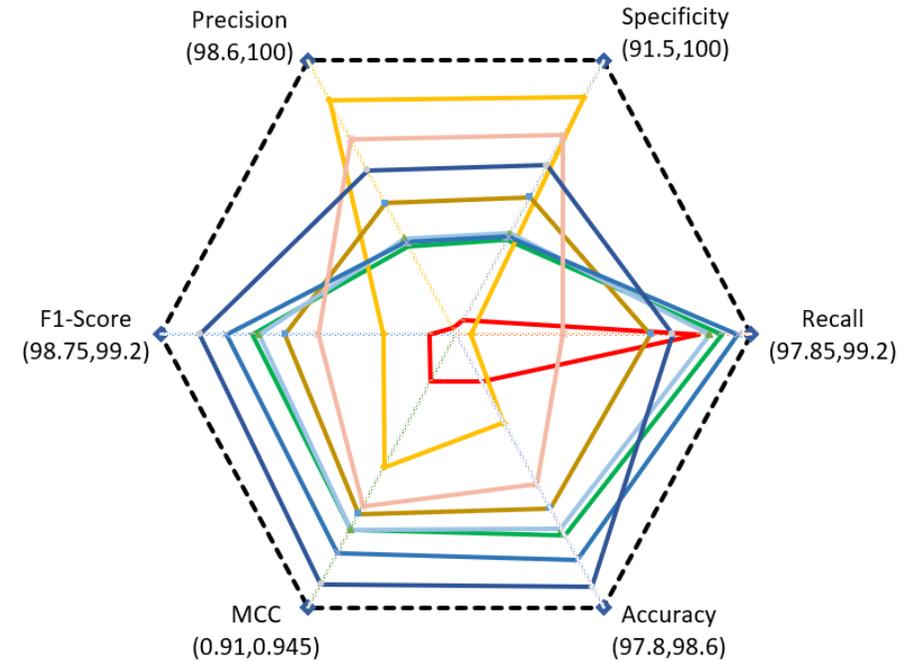
- **Example:** Assume 1000 datapoints
 - Actually safe: 20 TP= 1 FP=30
 - Actually unsafe: 980 FN= 19 TN=950

$$\text{Accuracy} = \frac{1+950}{1+19+950+30} = 95\%$$

- *95% accurate but we have misclassified almost all truly safe points!*
- *For heavily unbalanced data, accuracy is not sufficient!*

Performance metrics

- Accuracy
- Recall: True Positive Rate $\frac{TP}{TP+FN}$
- Specificity: True Negative Rate $\frac{TN}{TN+FP}$
- Precision: Positive Predictive Value $\frac{TP}{TP+FP}$
- F1: harmonic mean of Precision and Recall $F1 = \frac{Precision \cdot Recall}{Precision+Recall}$
- **MCC (Matthews correlation coefficient)**
 (only for binary classification – 2 classes only)
 - MCC=1 → perfect prediction
 - MCC=0 → random (like flipping a coin)
 - MCC= -1 → Completely mistaken

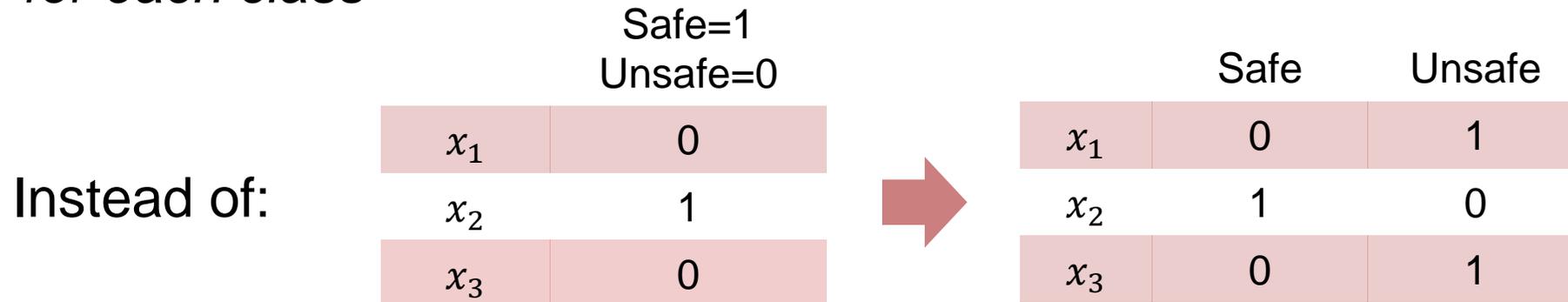


Hidalgo-Arteaga, Hancharou, Thams, Chatzivasileiadis, Powertech 2019

$$MCC = \frac{(TP \cdot TN) - (FP \cdot FN)}{\sqrt{(TP + FP)(TP + FN)(TN + FP)(TN + FN)}}$$

Key hints for your implementation

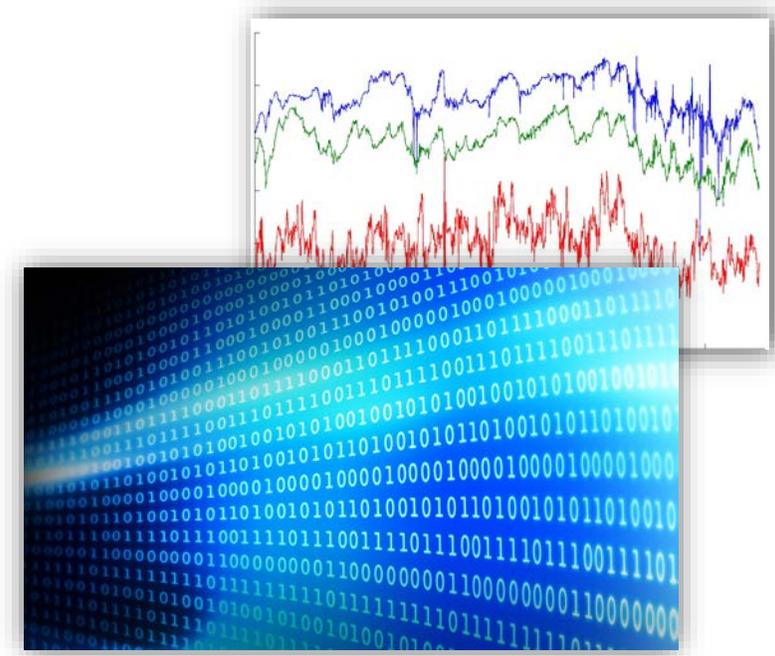
- Regularization: Training of neural networks work better if you normalize your inputs
 - Try to normalize your active power setpoints (e.g. if $PG1 = 30$ MW and $PG1_{max} = 100$ MW, then $PG1=0.3$)
- 1-hot encoding: Neural networks work better if you use *one vector for each class*



Training database

We need data!

- Data that accurately capture the whole security region
 - so that we can successfully use machine learning approaches for classification
- Historical data are insufficient
 - Contain very limited number of abnormal situations
- Need to generate simulation data
- **Assessing the stability of 100'000s of operating points is an extremely demanding task**
 - Immense search space



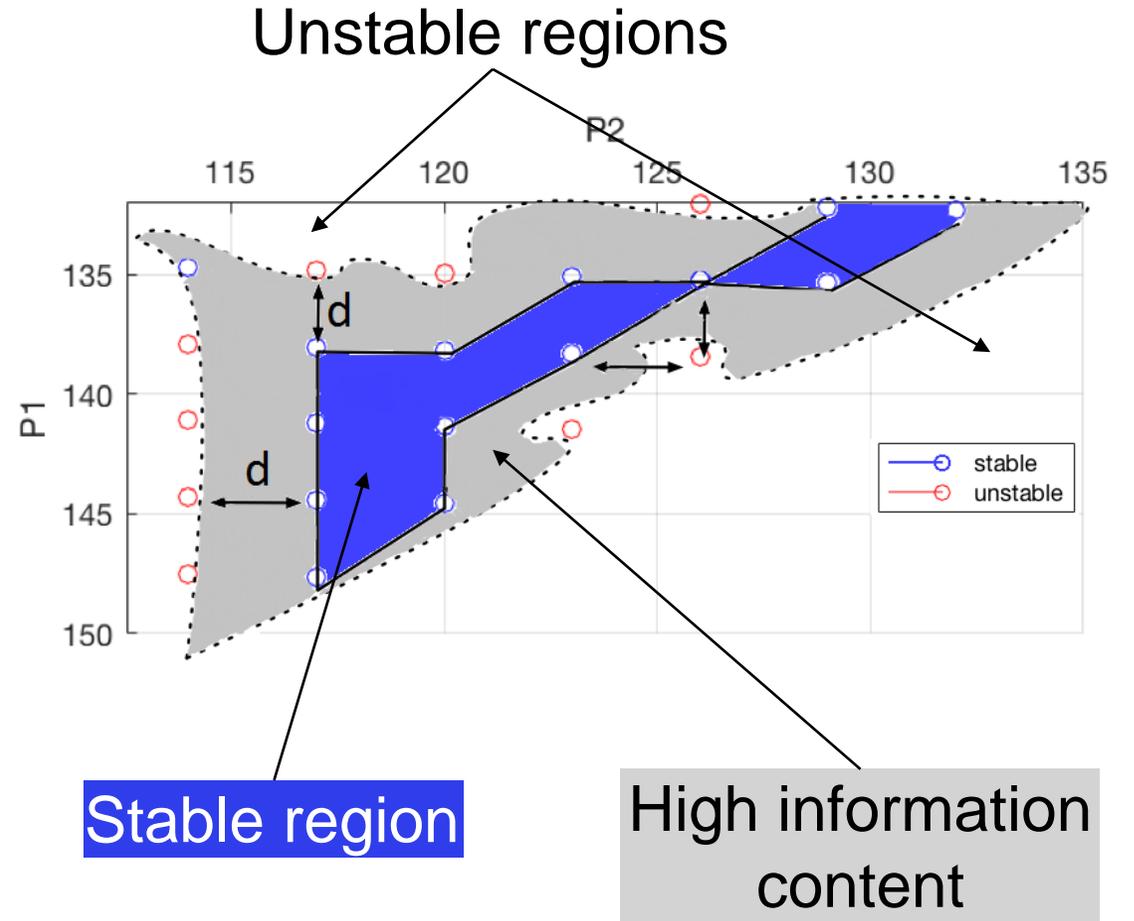
Efficient Database Generation

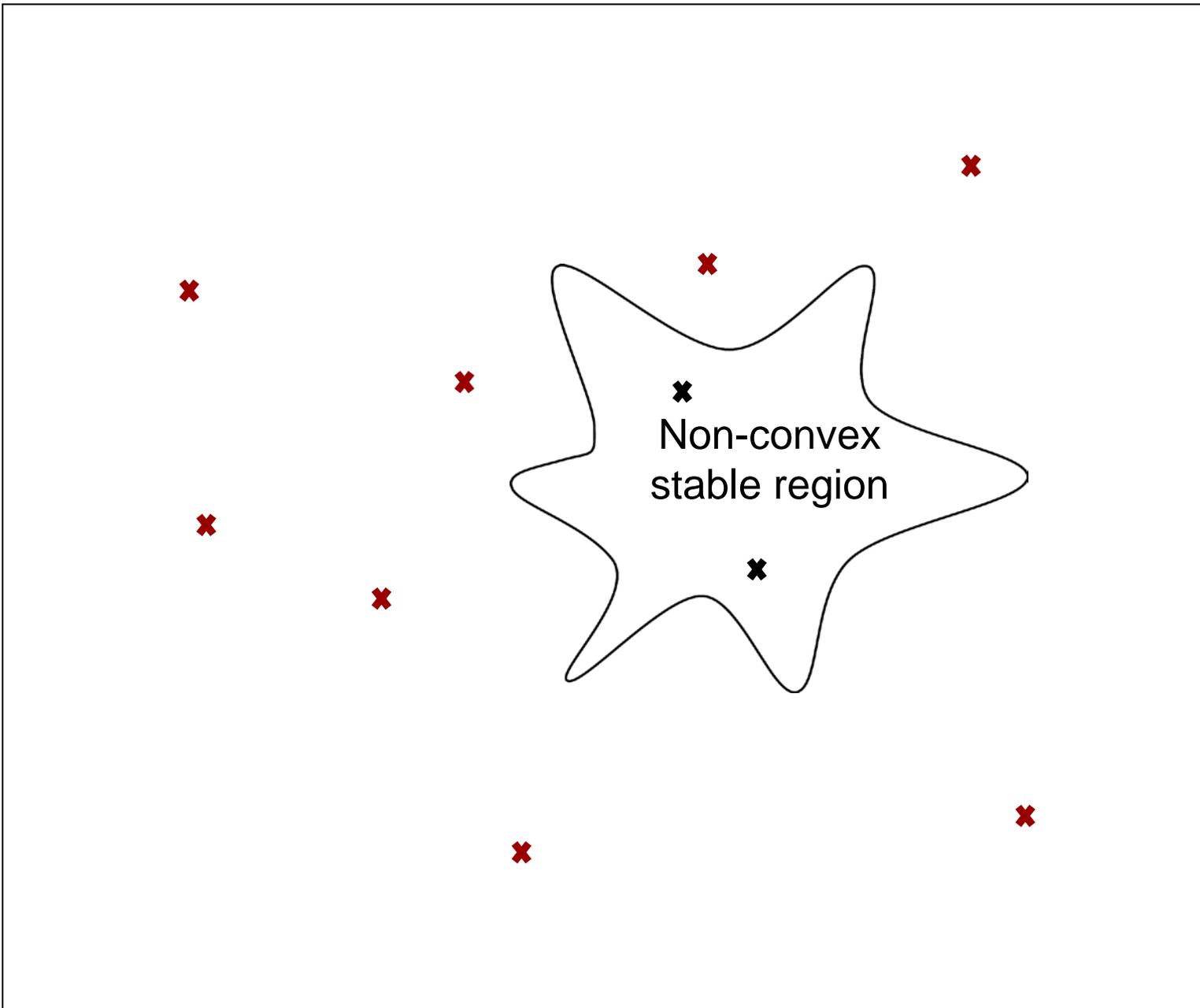
- Modular and highly efficient algorithm
- Can accommodate numerous definitions of power system security (e.g. N-1, N-k, small-signal stability, voltage stability, transient stability, **or a combination** of them)
- **10-20 times faster** than existing state-of-the-art approaches
- Our use case: N-1 security + small-signal stability
- Generated Database for NESTA 162-bus system online available!
https://github.com/johnnyDEDK/OPs_Nesta162Bus (>500,000 points)

F. Thams, A. Venzke, R. Eriksson, and S. Chatzivasileiadis, "Efficient database generation for data-driven security assessment of power systems". Accepted in IEEE Trans. Power Systems, 2019. <https://www.arxiv.org/abs/1806.0107.pdf>

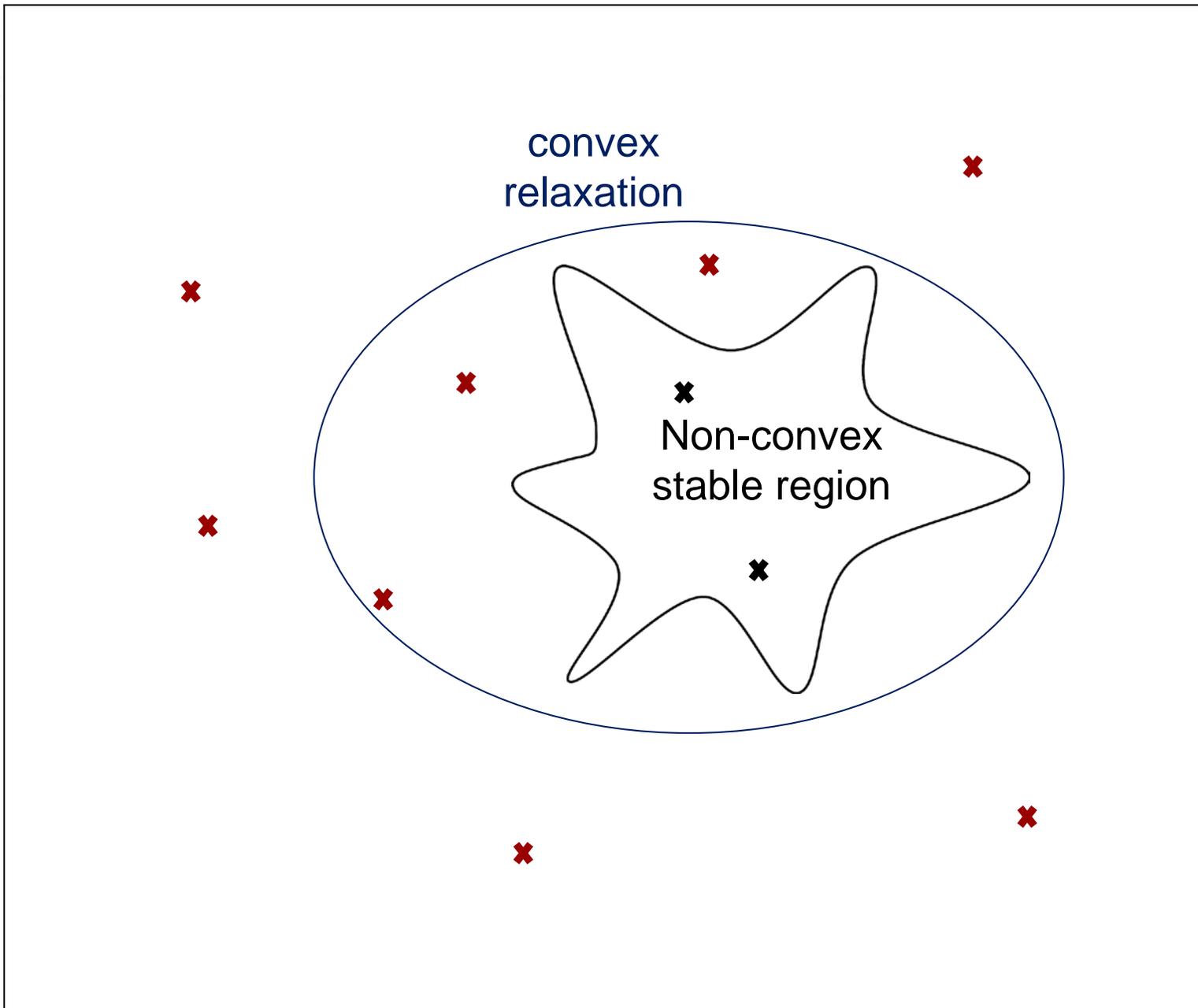
Efficient Database Generation

- The goal
 - **Focus** on the **boundary between stability and instability**
 - We call it: “high information content” region
- How?
 1. Using convex relaxations
 2. And “Directed Walks”



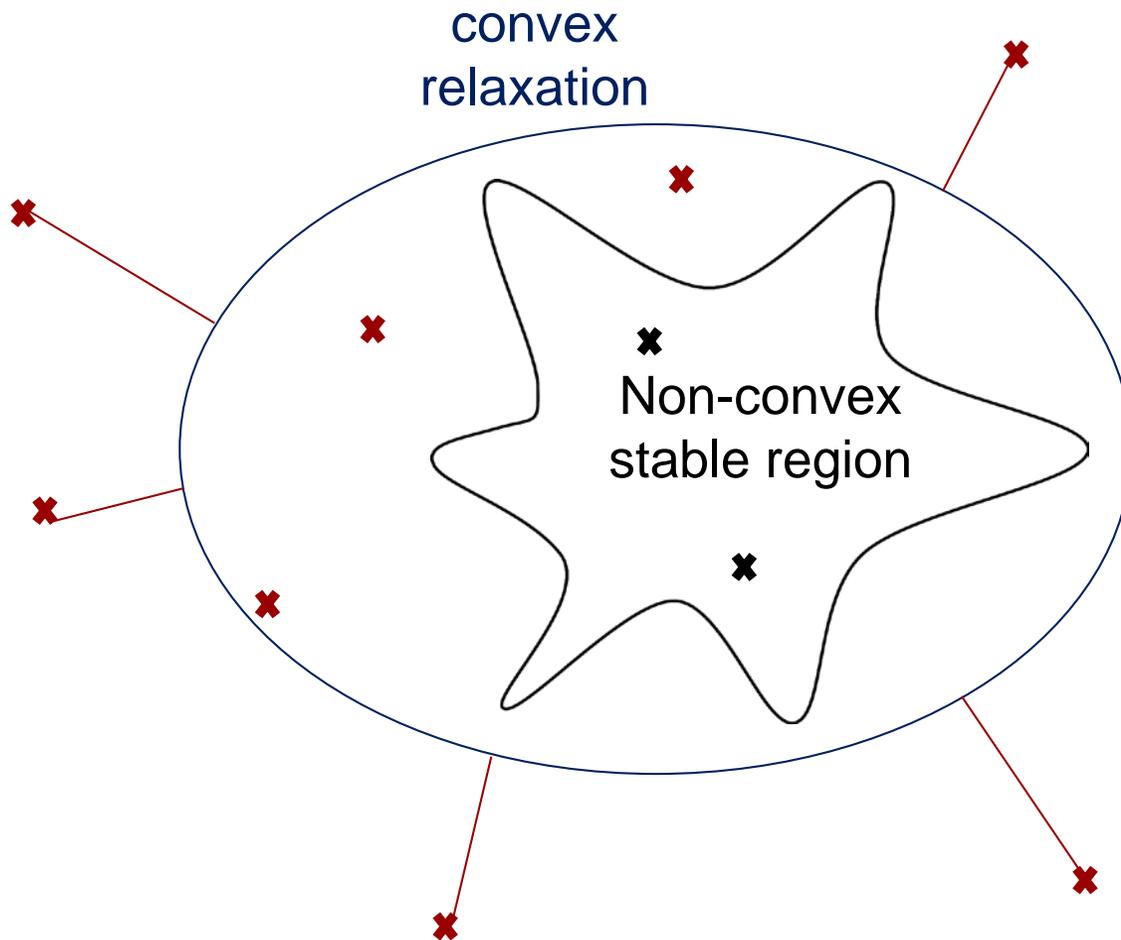


Convex relaxations to discard infeasible regions



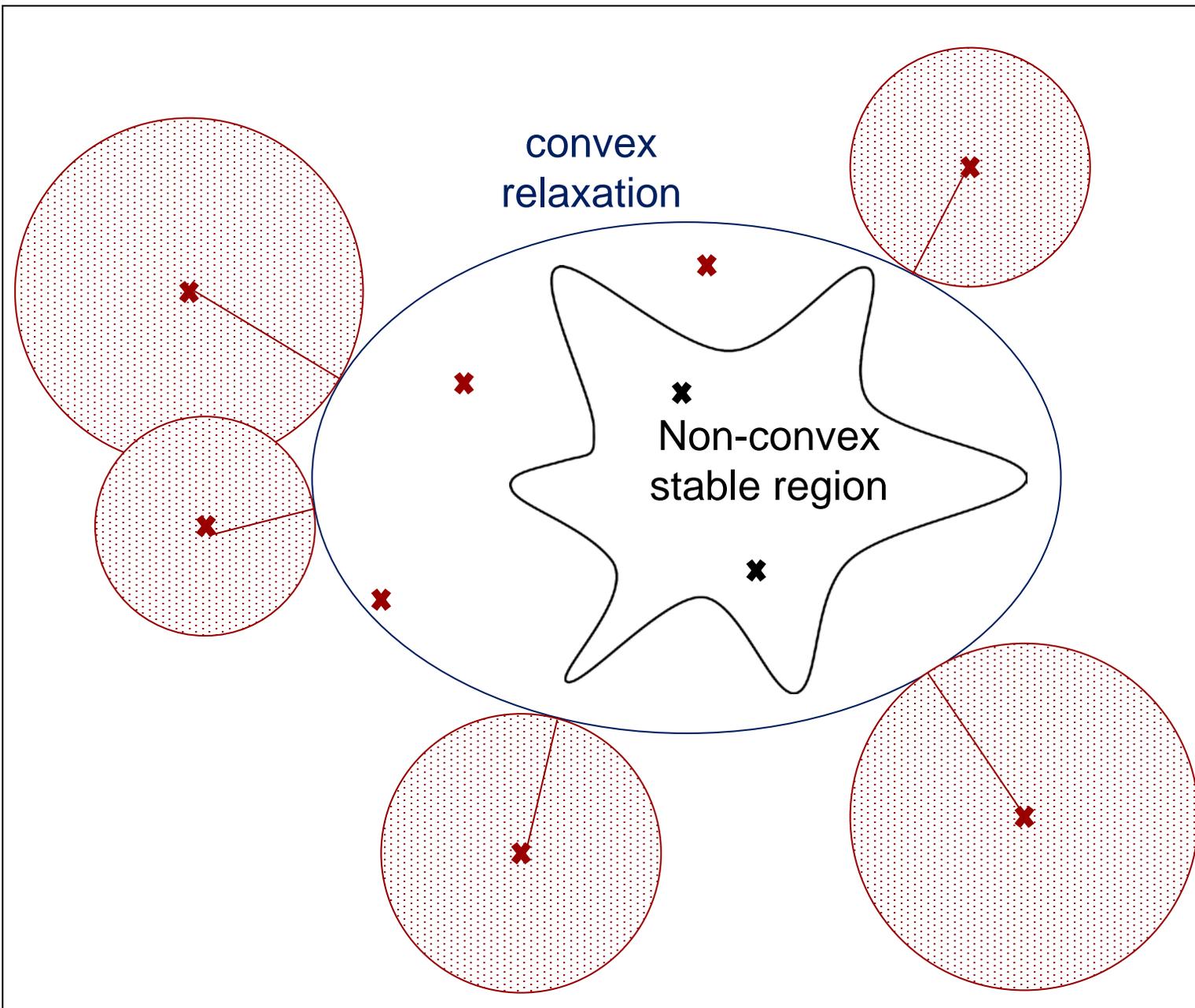
Convex relaxations to discard infeasible regions

- **Certificate**: if point infeasible for semidefinite relaxation \rightarrow infeasible for the original problem



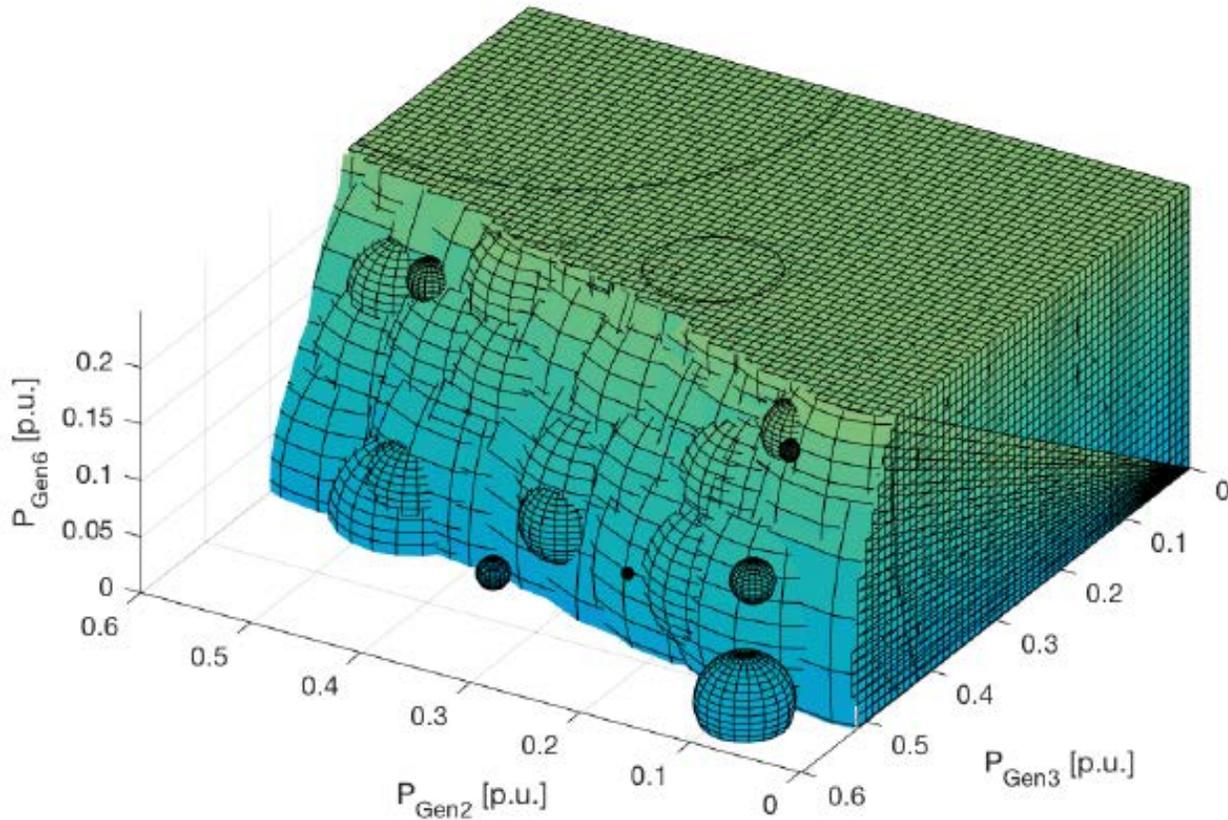
Convex relaxations to discard infeasible regions

- Certificate: if point infeasible for semidefinite relaxation \rightarrow infeasible for the original problem
- If infeasible point: find **minimum radius** to feasibility



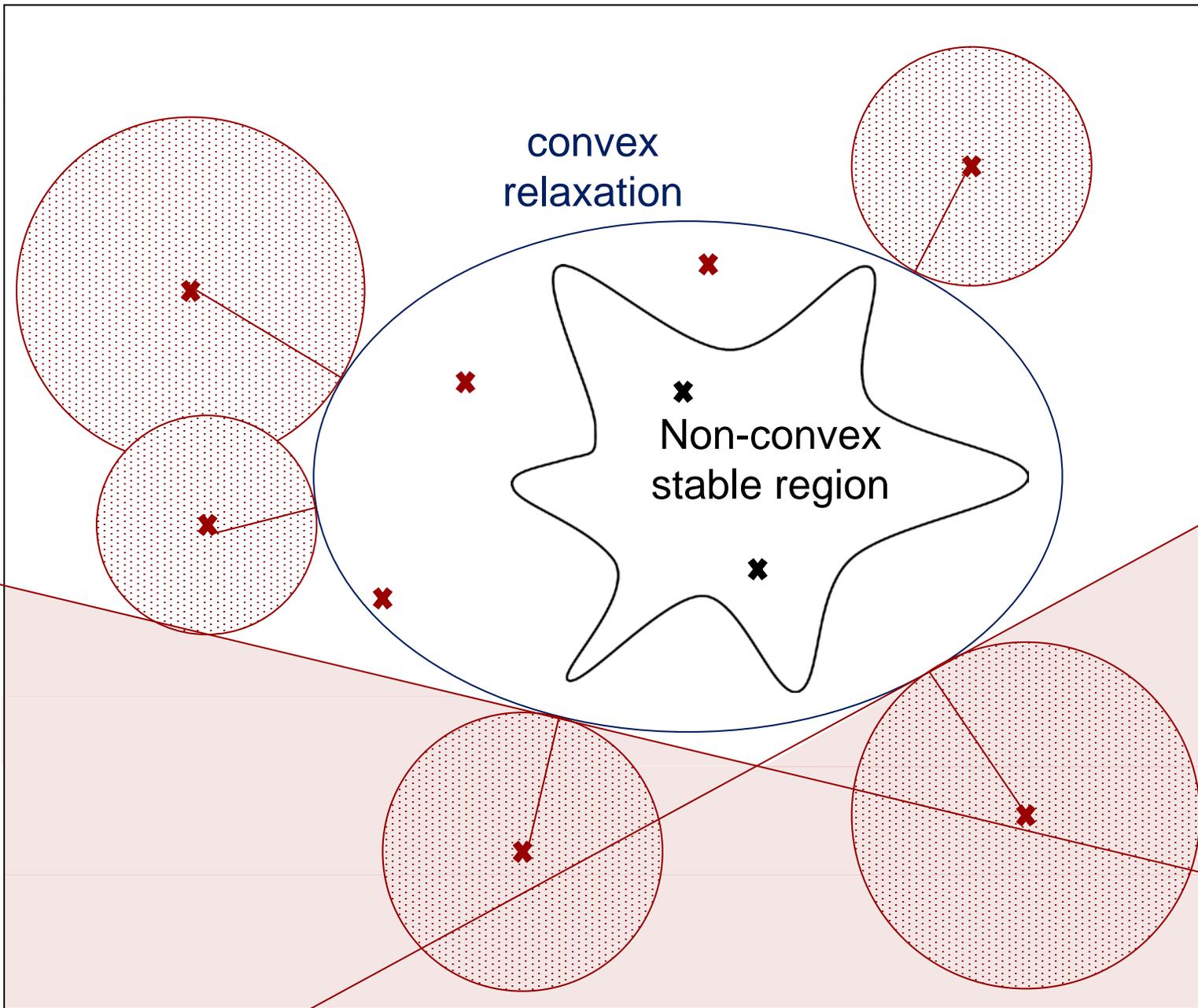
Convex relaxations to discard infeasible regions

- **Certificate**: if point infeasible for semidefinite relaxation \rightarrow infeasible for the original problem
- If infeasible point: find **minimum radius** to feasibility
- **Discard** all points inside the (hyper)sphere



- 3D projection of hyperspheres
- IEEE 14-bus system
- **Rapidly discarding (=classifying) large chunks of the search space as infeasible to focus on the boundary**

F. Thams, A. Venzke, R. Eriksson, and S. Chatzivasileiadis, "Efficient database generation for data-driven security assessment of power systems". Accepted in IEEE Trans. Power Systems, 2019. <https://www.arxiv.org/abs/1806.0107.pdf>

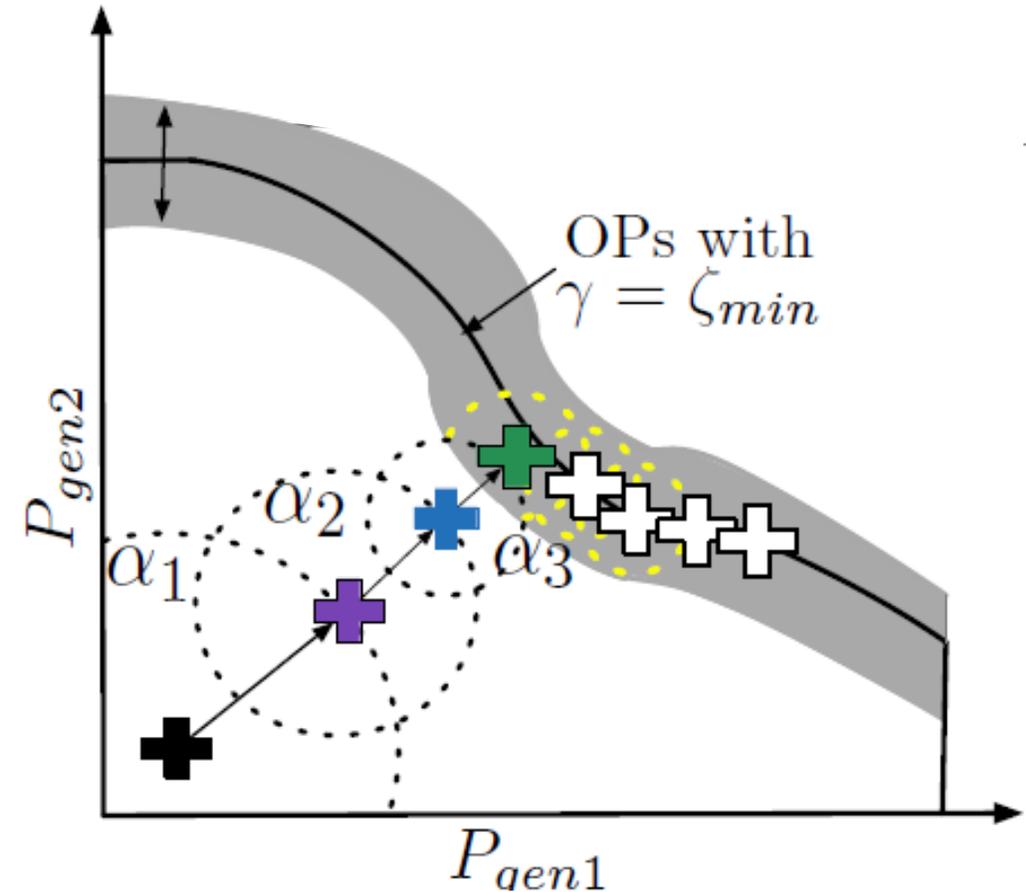


Convex relaxations to discard infeasible regions

- Currently working on hyperplanes
- Paper will appear soon

Directed Walks

- “Directed walks”: **steepest-descent based algorithm** to explore the remaining search space, **focusing on the area around the security boundary**
 1. Variable step-size
 2. Parallel computation
 3. Full N-1 contingency check



Results

	Points close to the security boundary (within distance γ)	
	IEEE 14-bus	NESTA 162-bus
Brute Force	100% of points in 556.0 min	<i>intractable</i>
Importance Sampling	100% of points in 37.0 min	901 points in 35.7 hours
Proposed Method	100% of points in 3.8 min	183'295 points in 37.1 hours

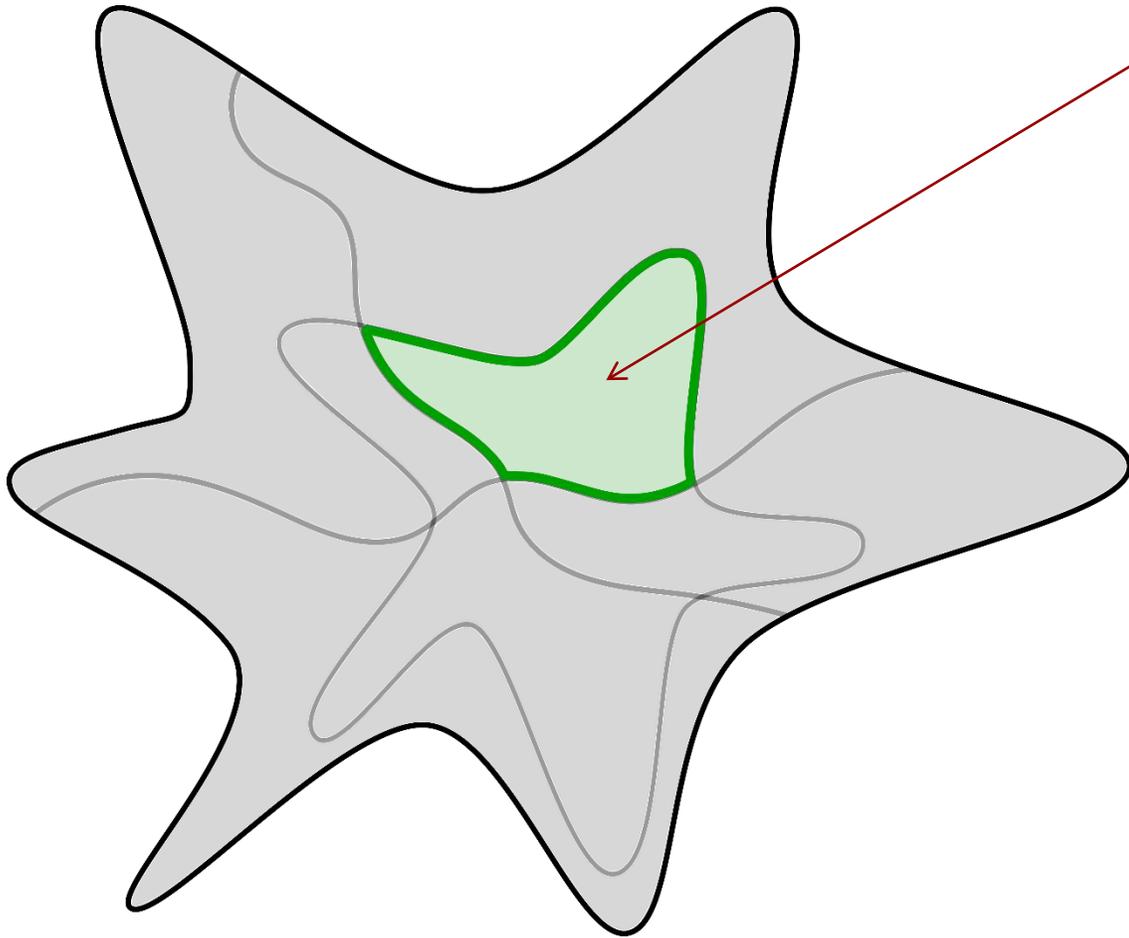
- Further benefits for the decision tree:
 - Higher accuracy
 - Better classification quality (Matthews correlation coefficient)

Generated Database for NESTA 162-bus system online available!

https://github.com/johnnyDEDK/OPs_Nesta162Bus

From decision trees to mixed integer linear programming

The feasible space of power system operations



Intersection of all security/stability criteria:
Non-linear and **non-convex** security region



Electricity markets should determine setpoints that are only within this area



Optimization **constraints should represent this area**



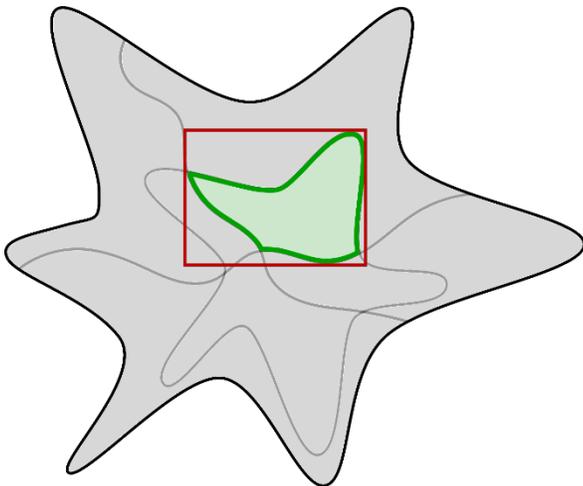
Impossible → differential and non-linear algebraic equations

What do TSOs and market operators do?

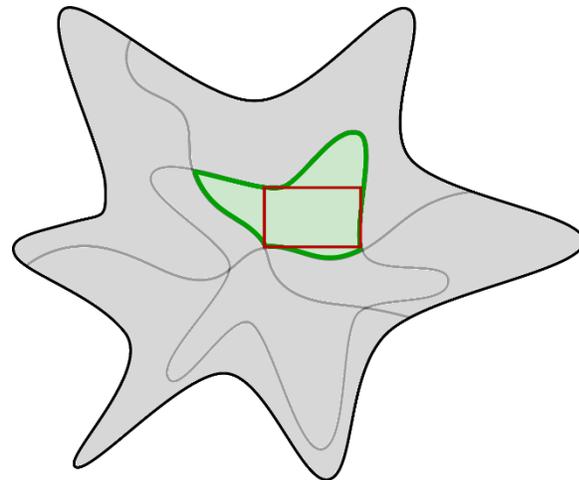
Linear approximations

Net Transfer Capacity

Inaccurate

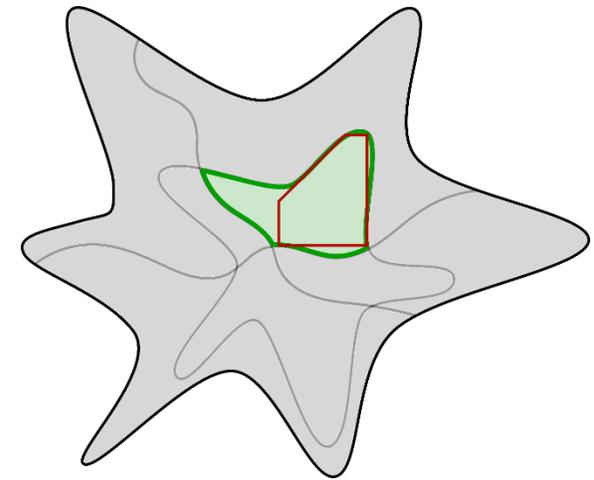


Too conservative



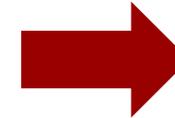
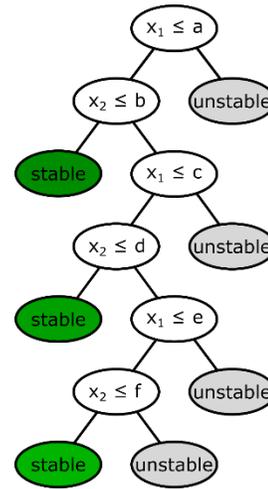
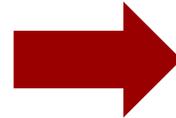
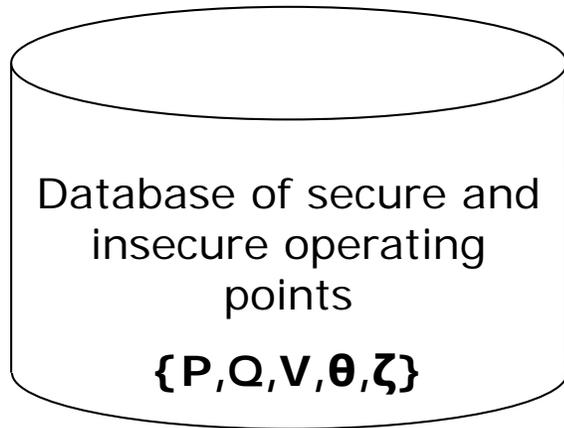
Flow-based market coupling

Single convex region



Our proposal: Data-driven Security Constrained OPF

How does it work?



$$PTDF \cdot (P_G - P_D) \leq F_{L,p}^{\max} y_p + F_L^{\max} (1 - y_p)$$

$$PTDF \cdot (P_G - P_D) \geq F_{L,p}^{\min} y_p - F_L^{\max} (1 - y_p)$$

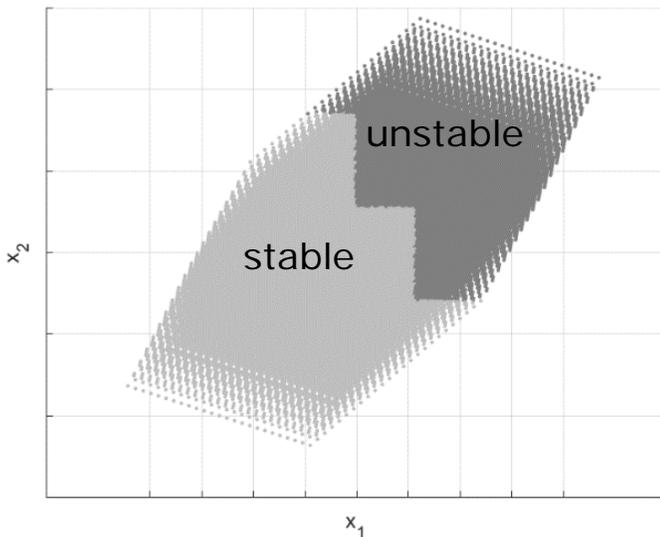
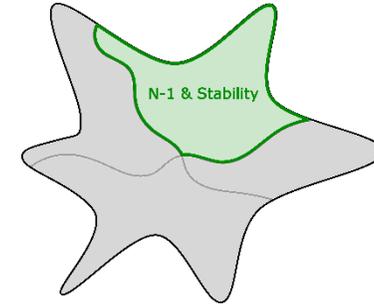
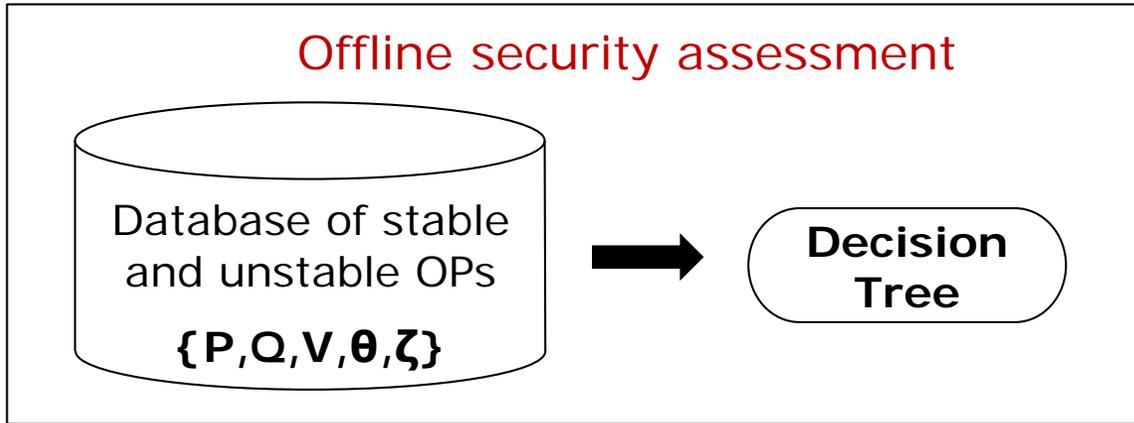
Operating points provided by the TSOs through simulated and real data

Train a decision tree to classify secure and insecure regions

Exact reformulation to MILP

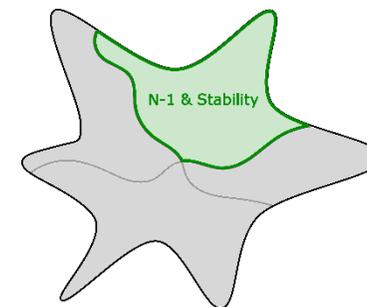
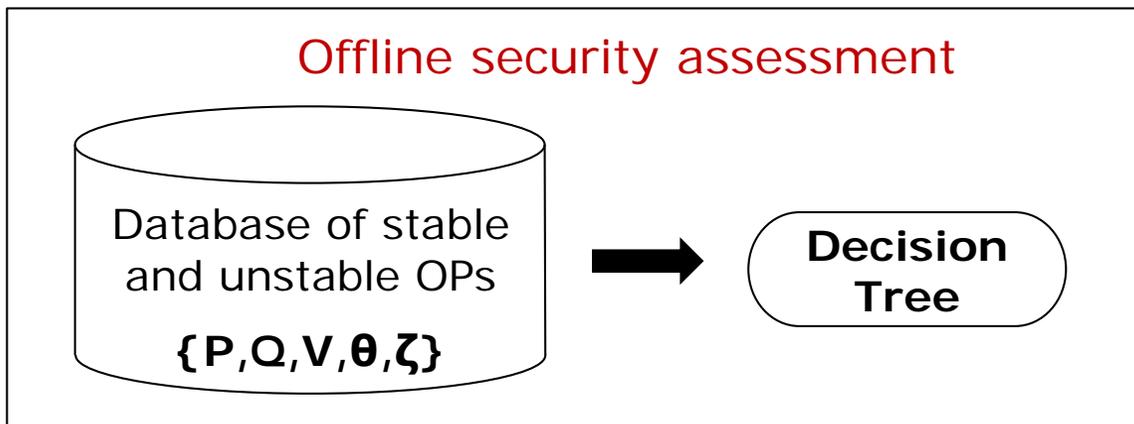
*Thams et al IREP 2017,
Halilbasic et al PSCC 2018*

Data-driven security-constrained OPF

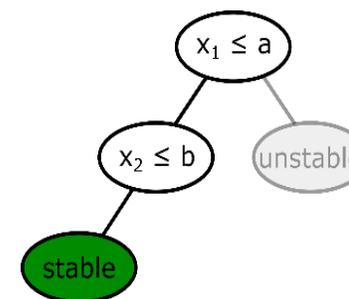
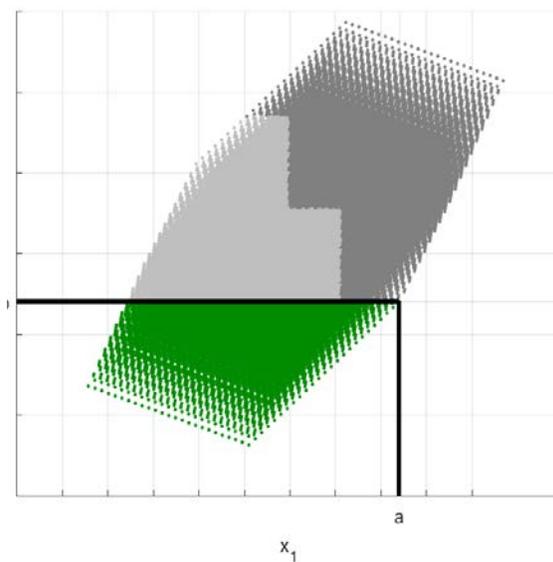
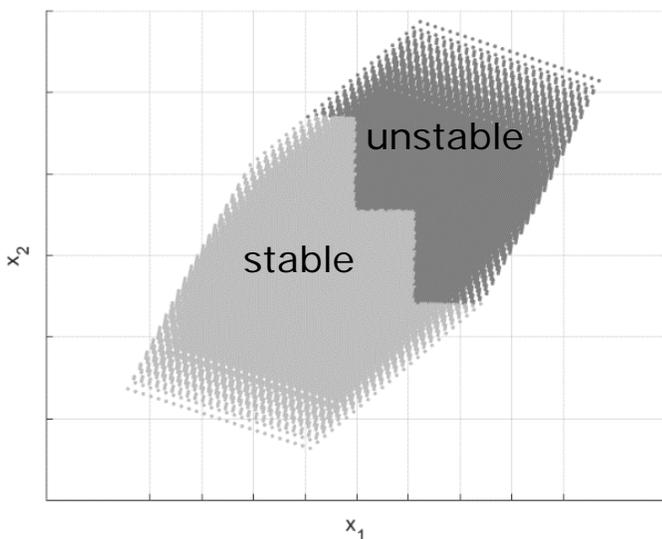


*Thams et al IREP 2017,
Halilbasic et al PSCC 2018*

Data-driven security-constrained OPF

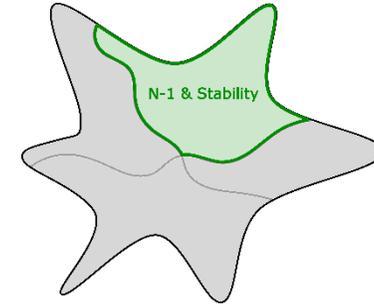
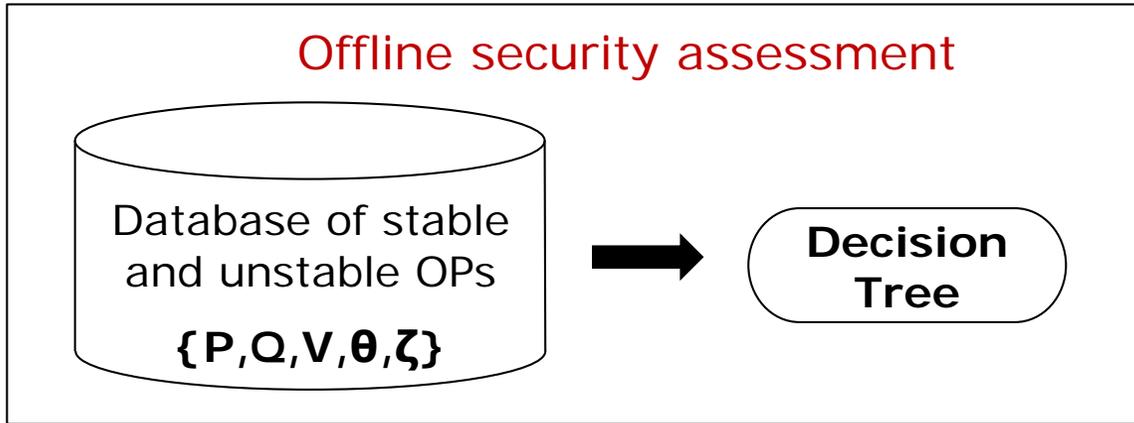


Partitioning the secure operating region

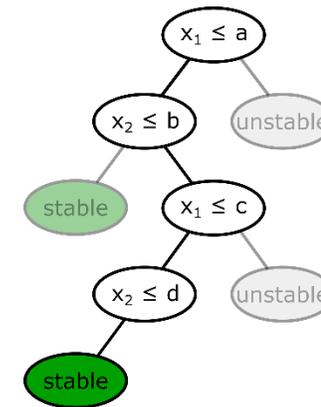
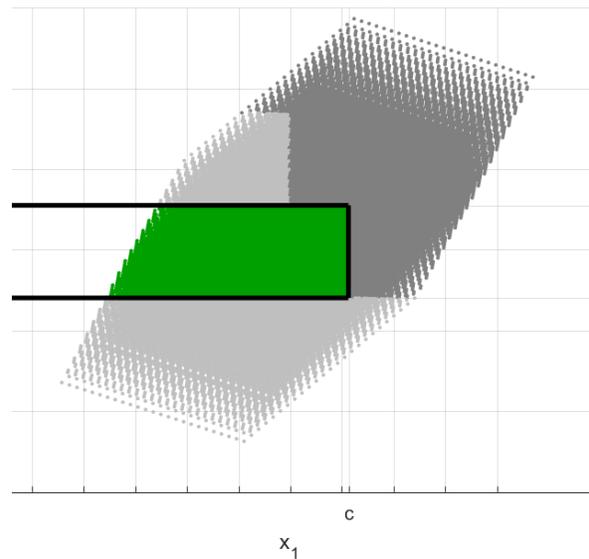
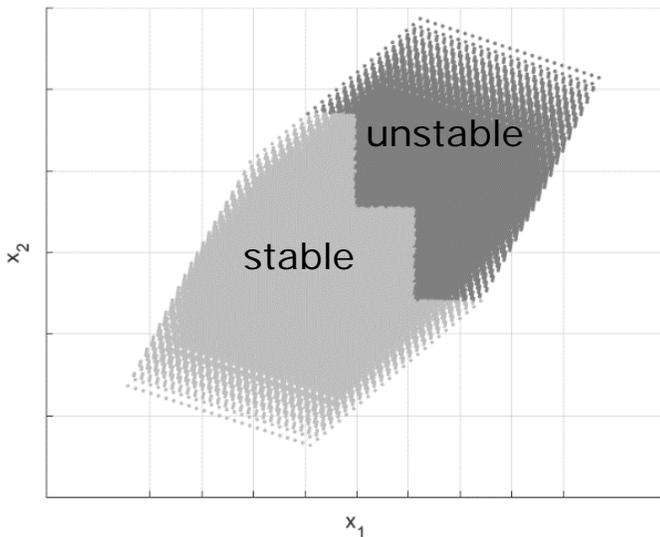


*Thams et al IREP 2017,
Halilbasic et al PSCC 2018*

Data-driven security-constrained OPF

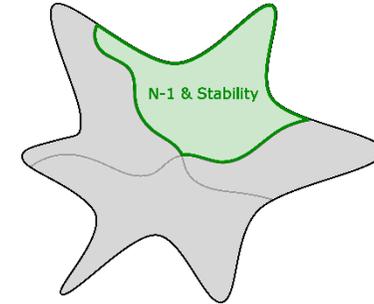
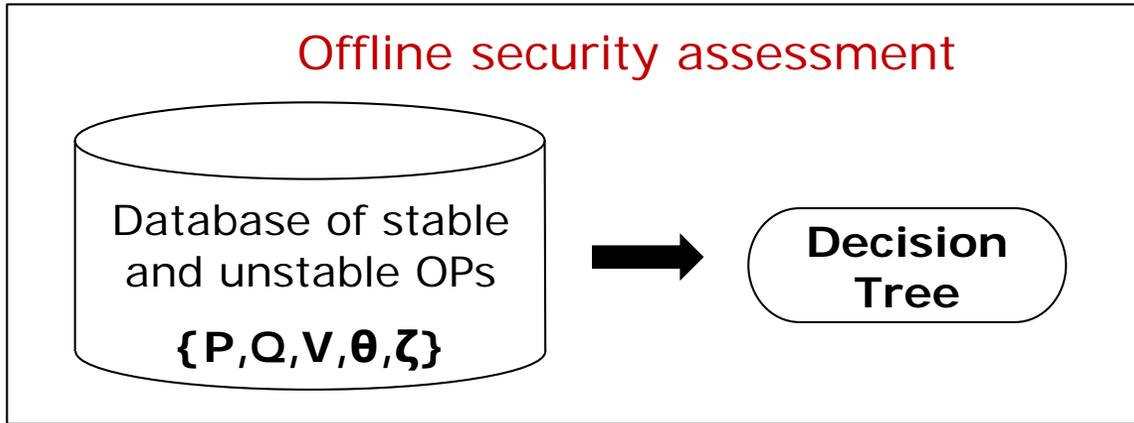


Partitioning the secure operating region

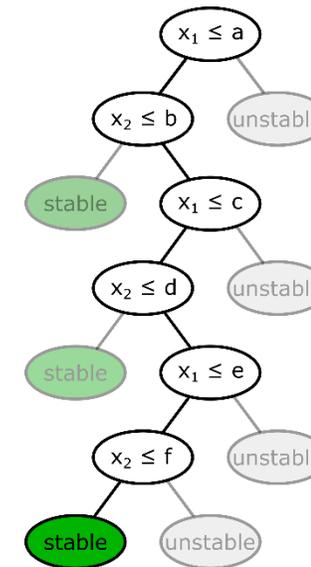
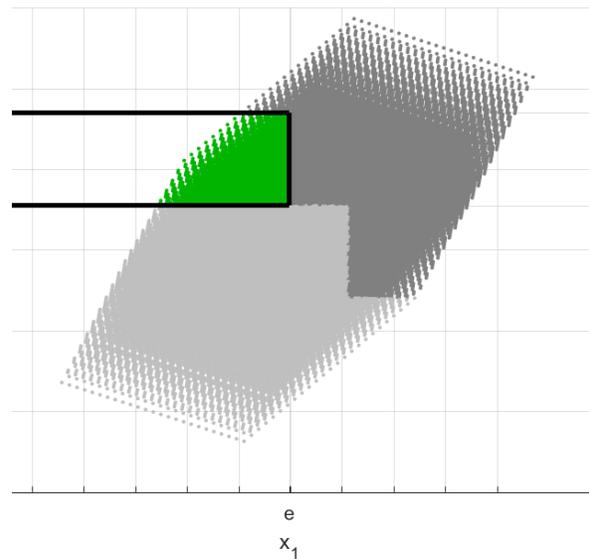
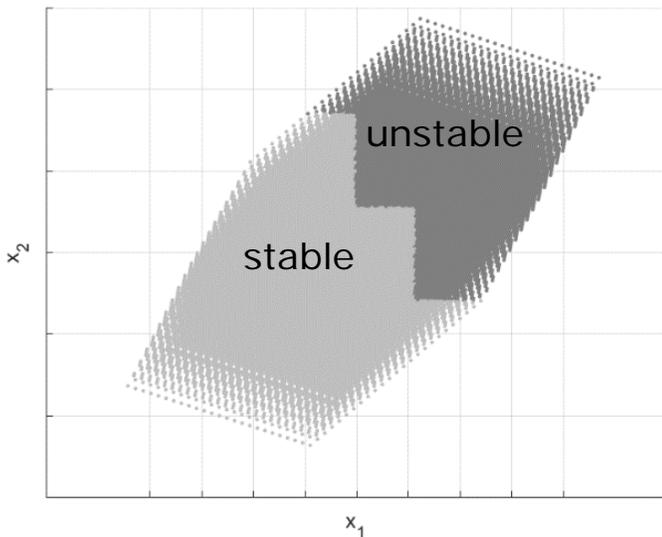


*Thams et al IREP 2017,
Halilbasic et al PSCC 2018*

Data-driven security-constrained OPF



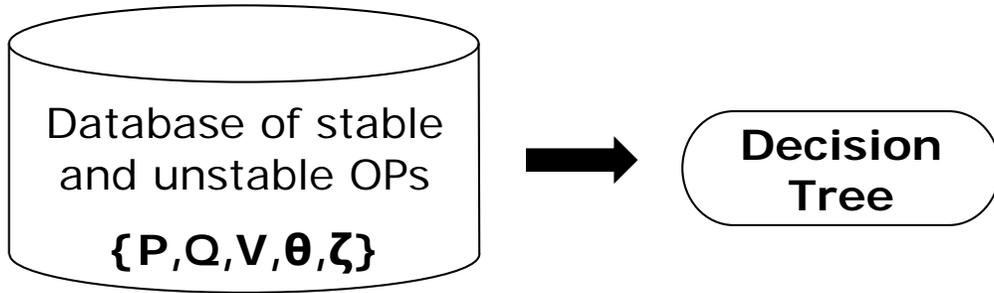
Partitioning the secure operating region



*Thams et al IREP 2017,
Halilbasic et al PSCC 2018*

Data-driven security-constrained OPF

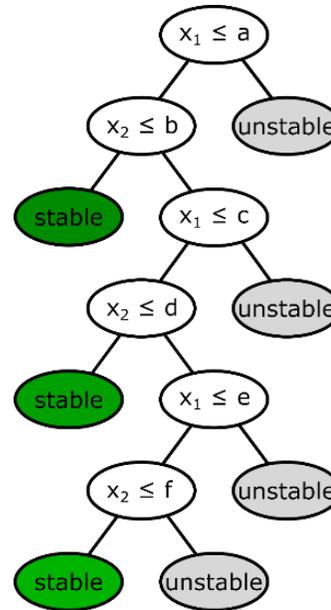
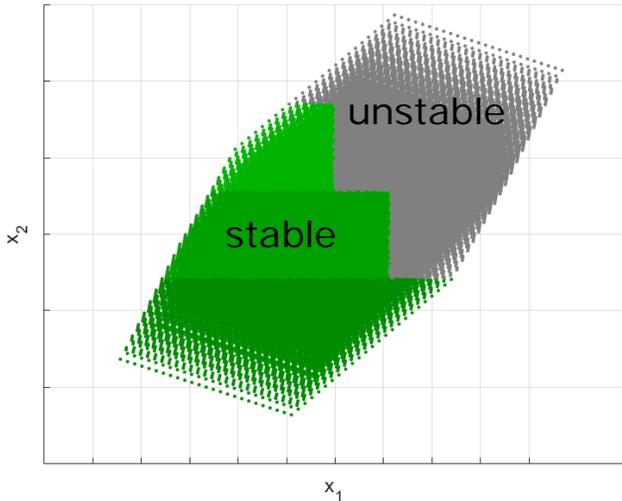
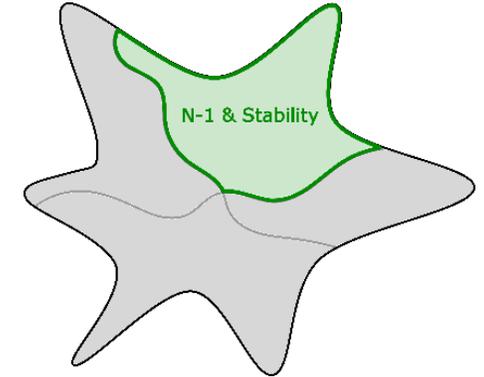
Offline security assessment



Optimization

Integer Programming to incorporate partitions (DT)

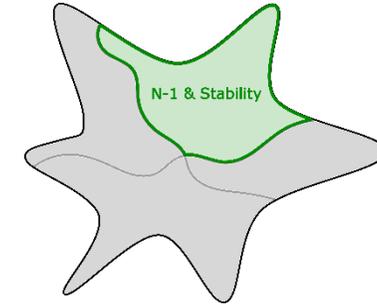
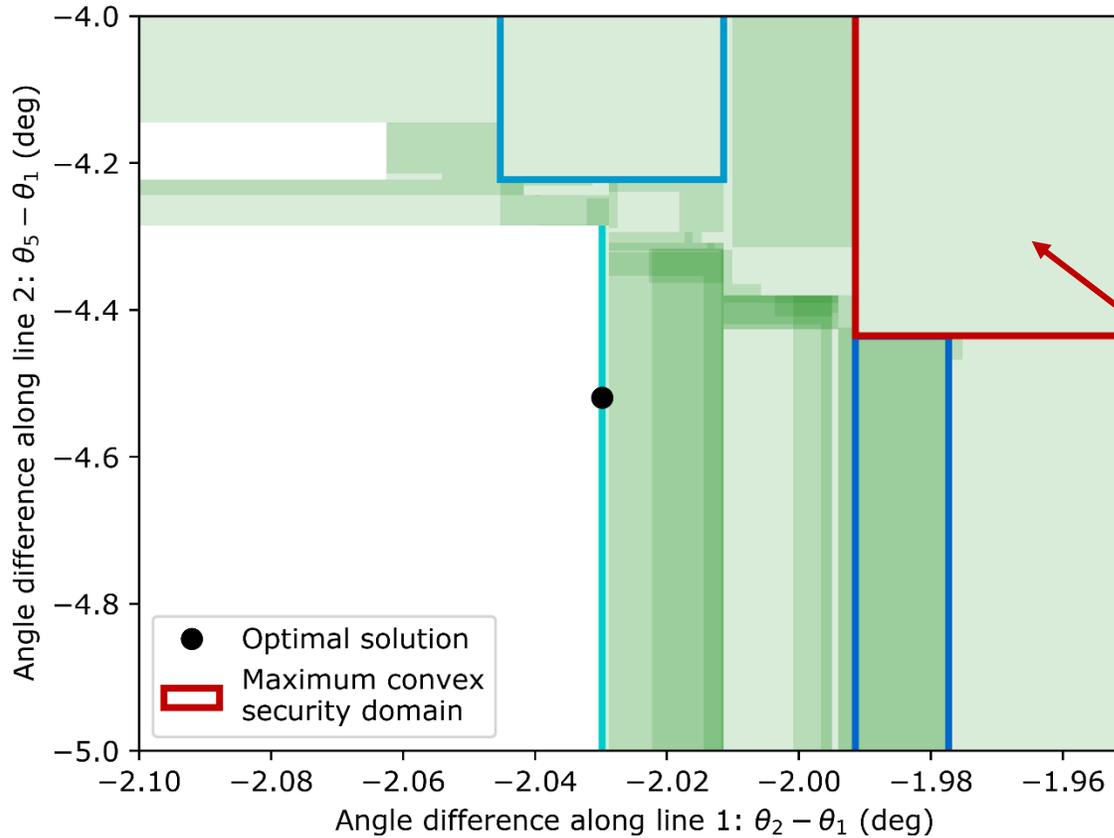
- DC-OPF (MILP)
- AC-OPF (MINLP)
- Relaxation (MIOCP, MISOCP)



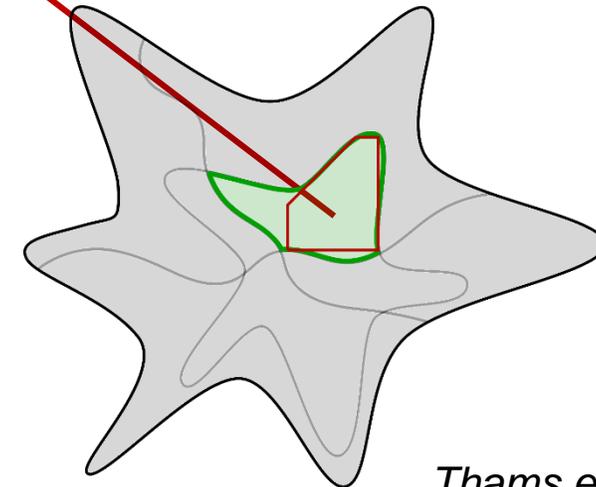
- Each leaf is a convex region
- FBMC corresponds to the leaf that maps the largest convex region

*Thams et al IREP 2017,
Halilbasic et al PSCC 2018*

We gain ~22% of the feasible space using data and Mixed Integer Programming

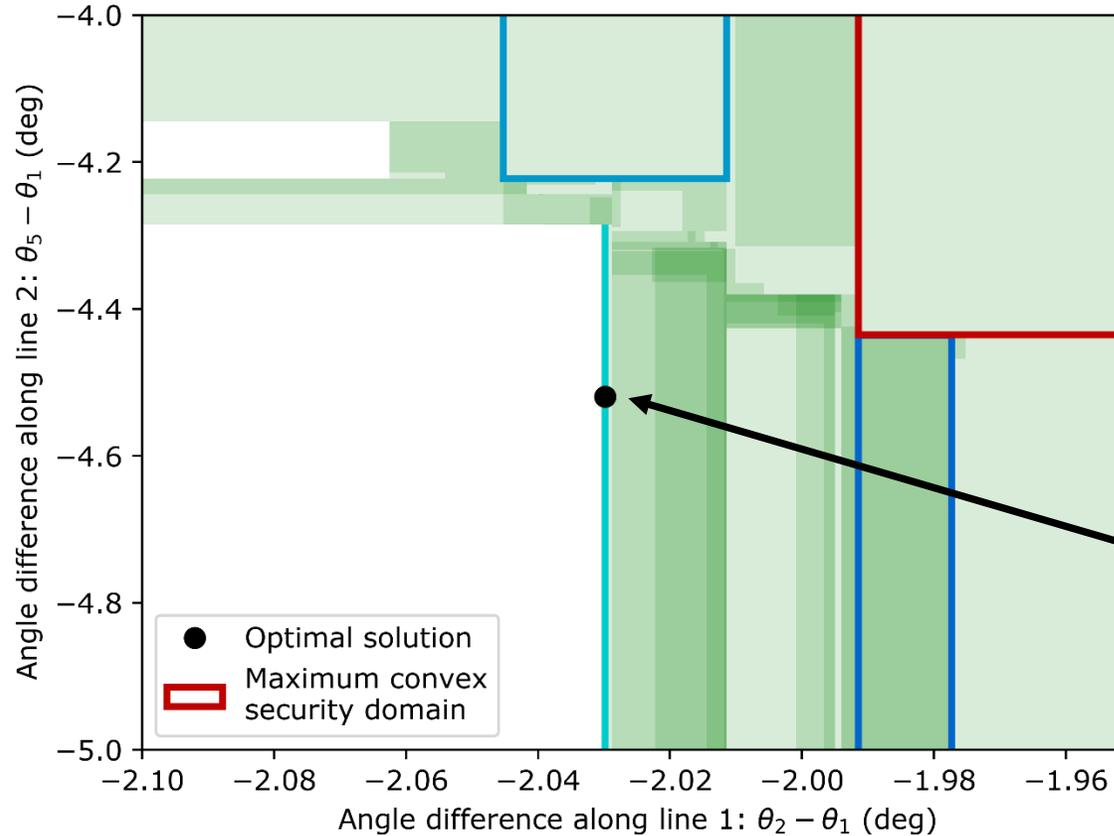
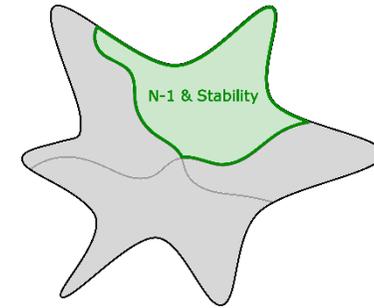


Largest convex region covers ~78%



*Thams et al IREP 2017,
Halilbasic et al PSCC 2018*

MIP + convex AC-OPF approximation finds better solutions than nonconvex problem!



Optimum located at boundary of considered security region

*Thams et al IREP 2017,
Halilbasic et al PSCC 2018*

Thank you!

spchatz@elektro.dtu.dk

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