



PSCC2020

multiDC



HVDC Loss Factors in the Nordic Power Market

Andrea Tosatto, Spyros Chatzivasileiadis
Technical University of Denmark (DTU)

July 2, 2020
XXI Power System Computation Conference

Zero-price difference between zones



Hours of operation with zero-price-difference and corresponding losses (€)

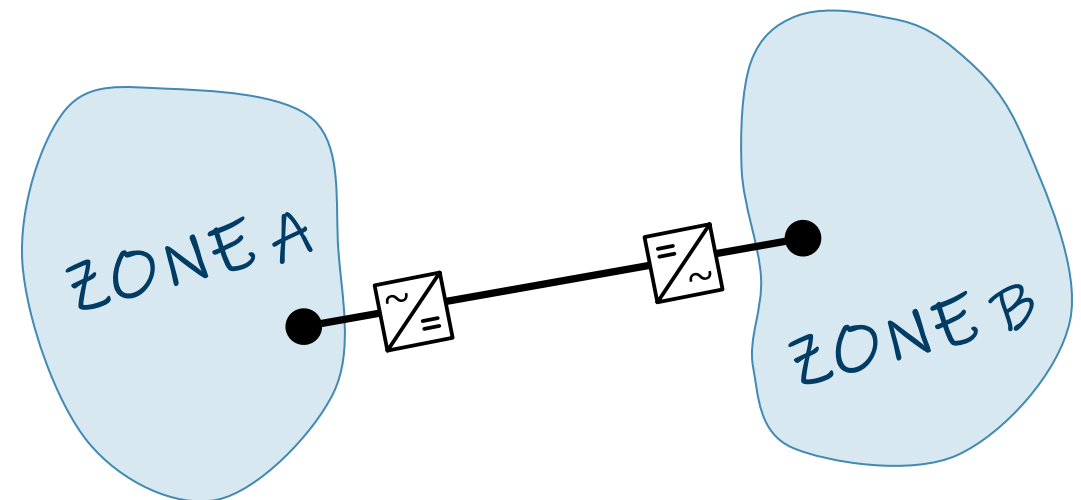
	2017		2018	
	%	LOSSES	%	LOSSES
KONTISKAN	61%	1.2 M€	53%	1.5 M€
STOREBÆLT	73%	0.8 M€	74%	1.1 M€
SKAGERRAK	47%	3.2 M€	46%	4.7 M€
ESTLINK	76%	3.1 M€	95%	6.7 M€
FENNOSKAN	99%	3.8 M€	80%	4.2 M€
		12 M€		18 M€

Source: <https://www.nordpoolgroup.com/>

Introduction of HVDC loss factors

- With the current practice, **losses** are **not considered** in the market clearing process.

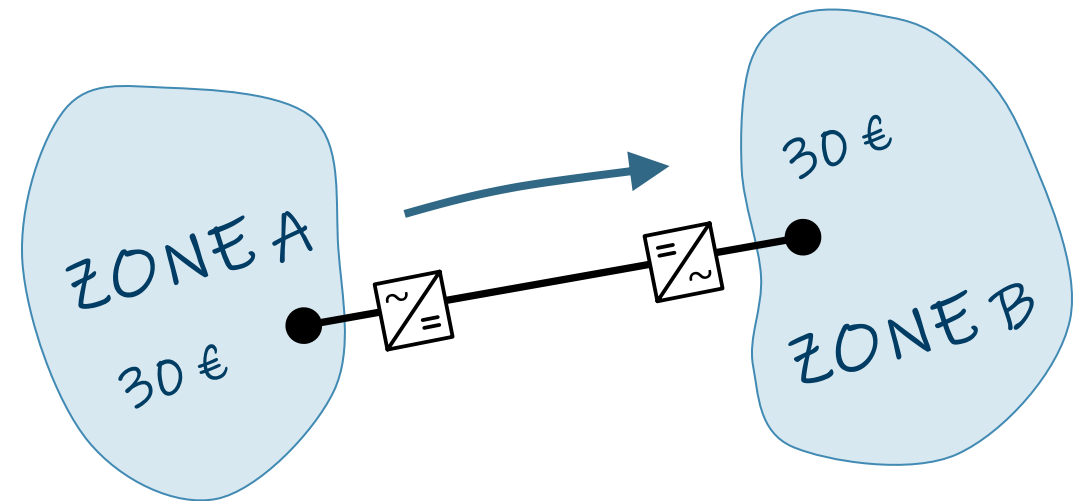
$$\text{Price of electricity} = \text{Cost of energy} + \text{Cost of congestion}$$



Introduction of HVDC loss factors

- With the current practice, **losses** are **not considered** in the market clearing process.

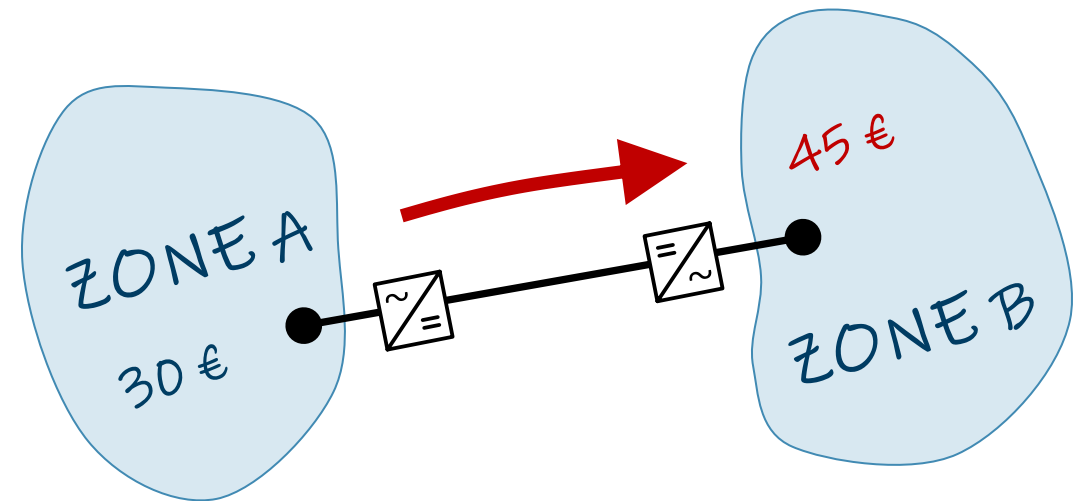
$$\text{Price of electricity} = \text{Cost of energy} + \text{Cost of congestion}$$



Introduction of HVDC loss factors

- With the current practice, **losses** are **not considered** in the market clearing process.

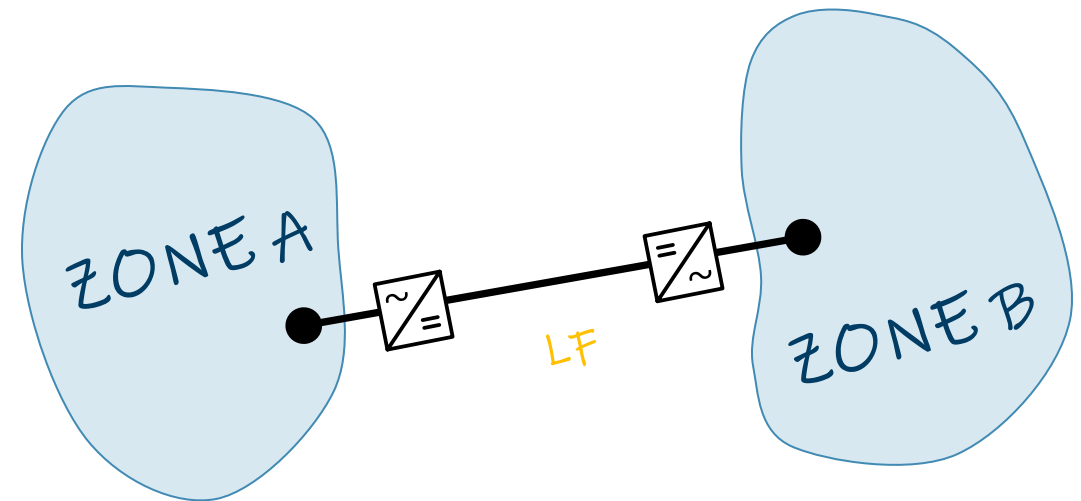
$$\text{Price of electricity} = \text{Cost of energy} + \text{Cost of congestion}$$



Introduction of HVDC loss factors

- With the current practice, **losses** are **not considered** in the market clearing process.
- The **Nordic TSOs** have proposed the introduction of linear HVDC loss factors^{*}.

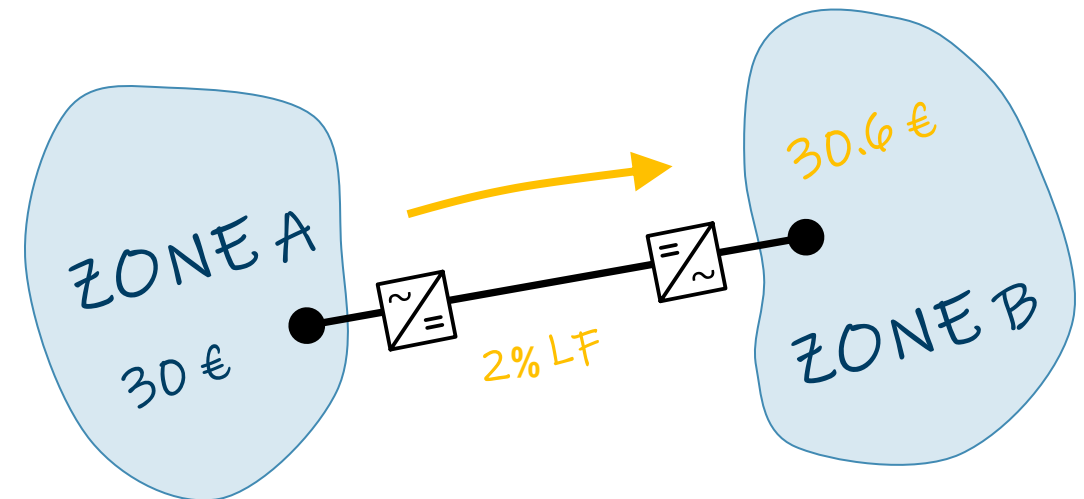
$$\text{Price of electricity} = \text{Cost of energy} + \text{Cost of congestion} + \text{Cost of losses}$$



Introduction of HVDC loss factors

- With the current practice, **losses** are **not considered** in the market clearing process.
- The **Nordic TSOs** have proposed the introduction of linear HVDC loss factors^{*}.
- The introduction of HVDC loss factors creates **price differences** to cover the cost of losses.

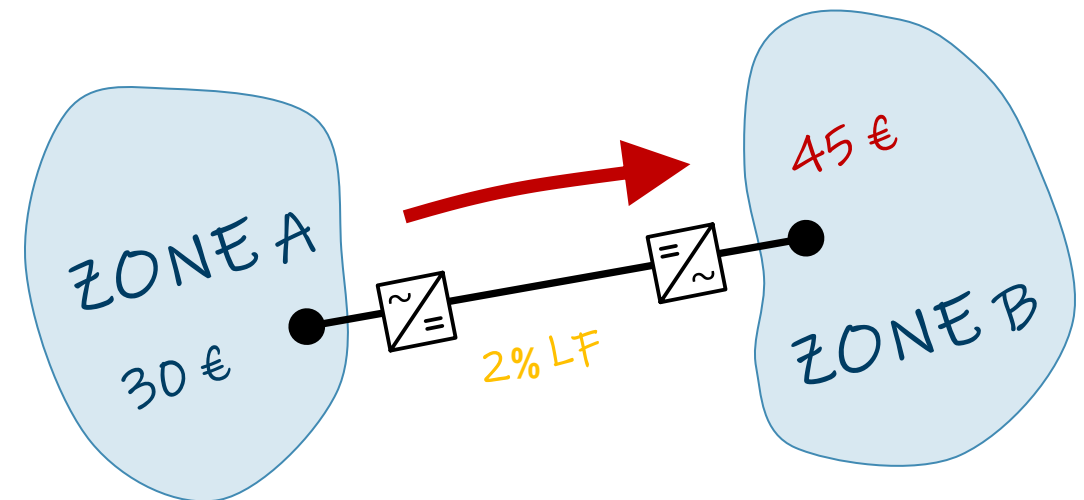
$$\text{Price of electricity} = \text{Cost of energy} + \text{Cost of congestion} + \text{Cost of losses}$$



Introduction of HVDC loss factors

- With the current practice, **losses** are **not considered** in the market clearing process.
- The **Nordic TSOs** have proposed the introduction of linear HVDC loss factors^{*}.
- The introduction of HVDC loss factors creates **price differences** to cover the cost of losses.

$$\text{Price of electricity} = \text{Cost of energy} + \text{Cost of congestion} + \text{Cost of losses}$$

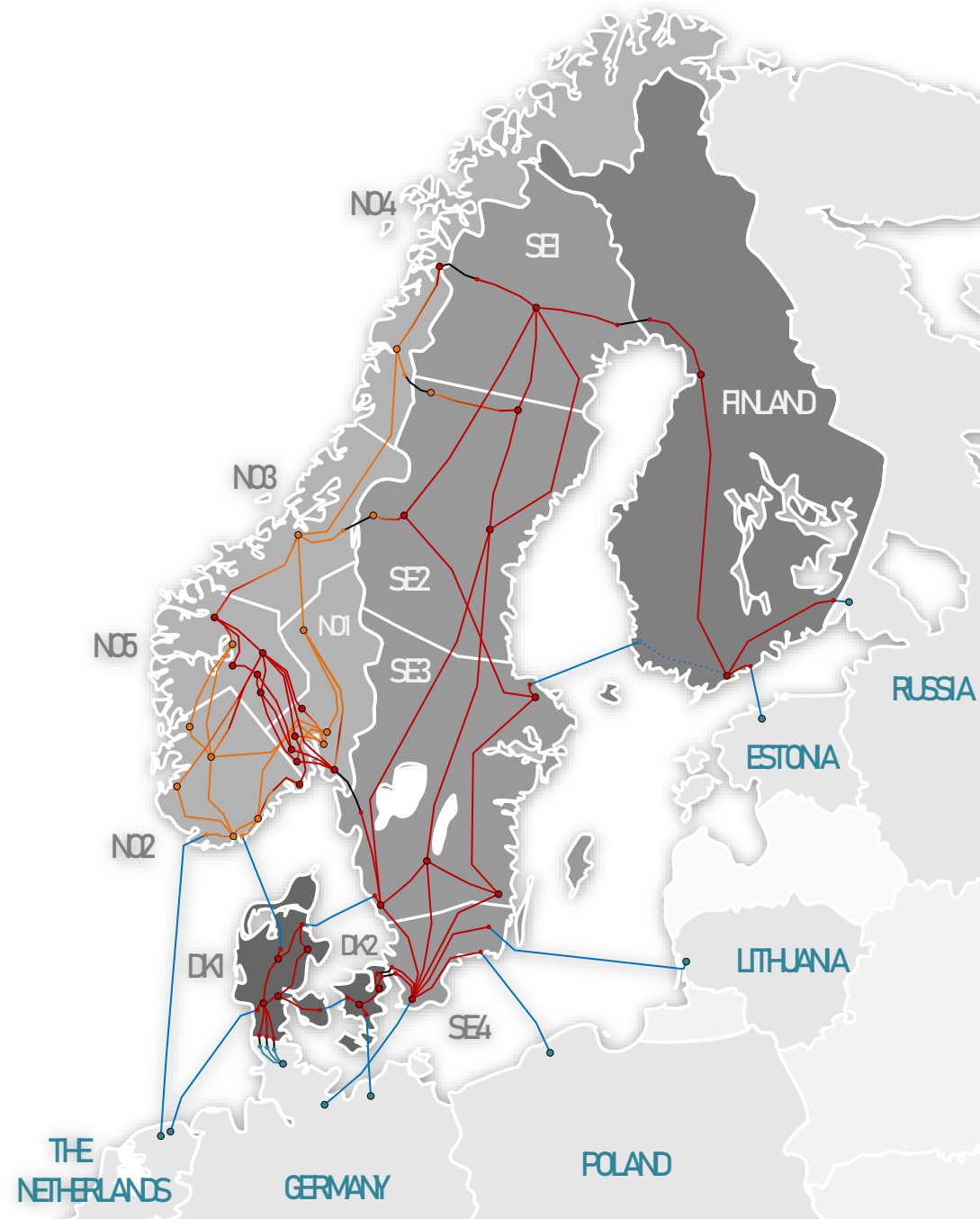


Introduction of HVDC loss factors

Stage	AC losses	HVDC losses	
		Current practice	TSOs proposal
D-2	<ul style="list-style-type: none"> TSOs estimate losses 	<ul style="list-style-type: none"> TSOs estimate losses Bilateral agreements 	-
D-1	<ul style="list-style-type: none"> Price-independent bids in the market 	<ul style="list-style-type: none"> Price-independent bids in the market 	<ul style="list-style-type: none"> Losses are calculated using loss factors The ones who create losses pay
RT	<ul style="list-style-type: none"> Any mismatch is covered in the balancing market 	<ul style="list-style-type: none"> Any mismatch is covered in the balancing market 	<ul style="list-style-type: none"> If losses calculated with loss factors are exact, society pay less

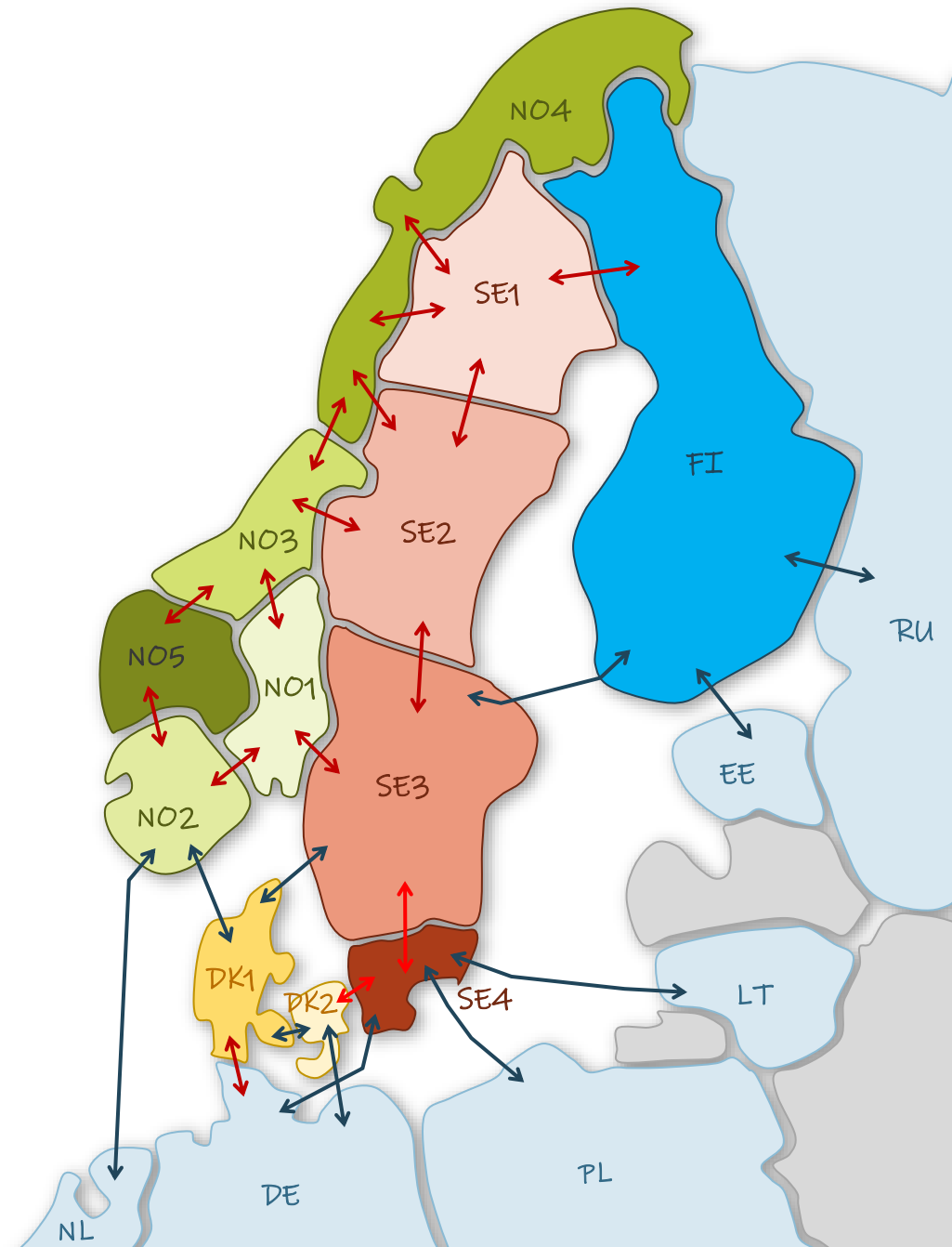
Nordic test network

- **Test case:**
 - 369 nodes, 362 AC and 10 HVDC transmission lines;
 - 631 generating units;
 - Actual wind, solar and load profiles from 2017.



Nordic test network

- **Test case:**
 - 369 nodes, 362 AC and 10 HVDC transmission lines;
 - 631 generating units;
 - Actual wind, solar and load profiles from 2017.
- **Nordic market:**
 - Zonal-pricing market;
 - Nodes aggregated into bidding zones;
 - Actual transfer capacities from NordPool.



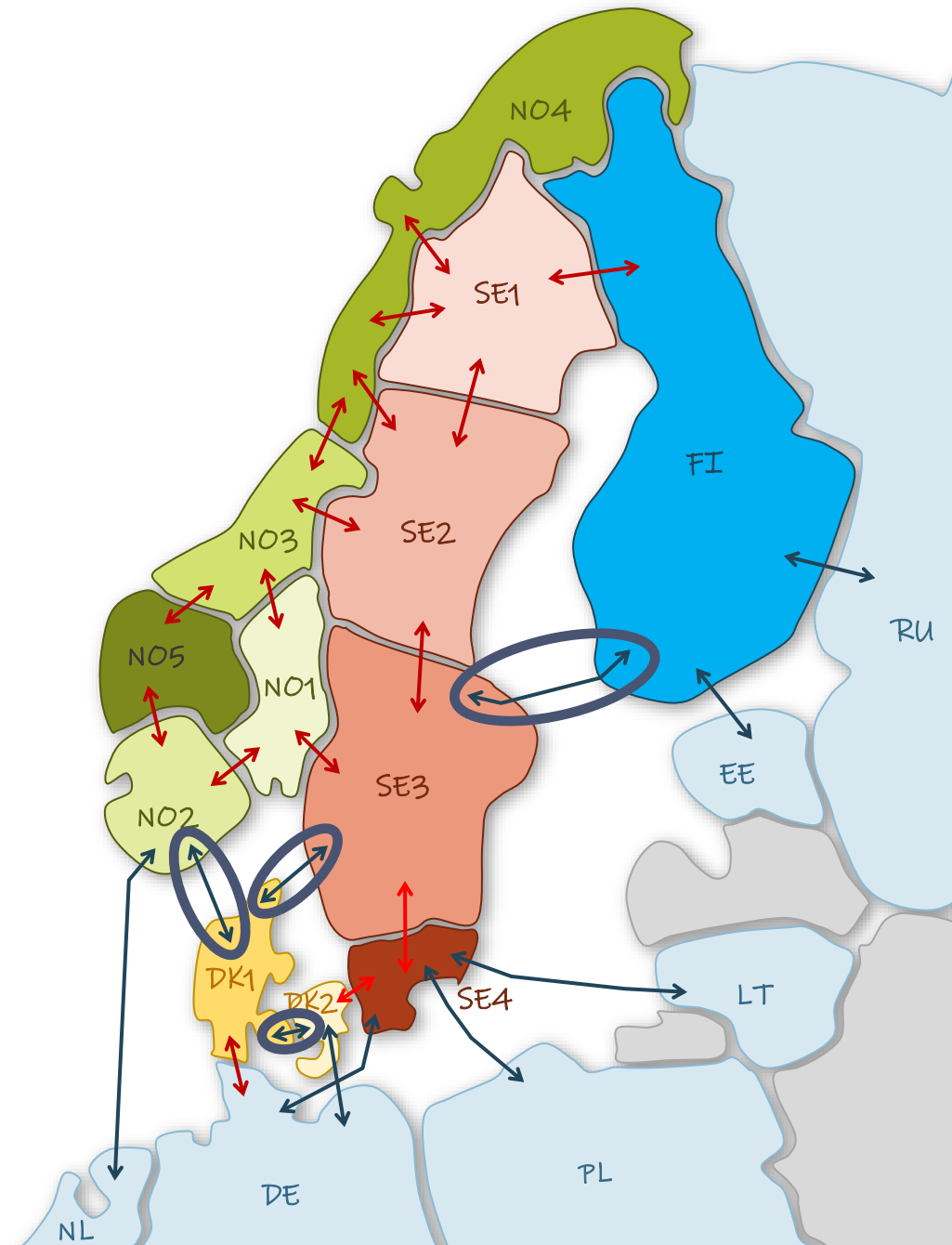
Nordic test network

- **Simulations:**

- Focus on intra-Nordic HVDC lines;
- Two analyses:

1. **Linear** vs. **piecewise-linear**

2. **HVDC** vs. **AC+HVDC**



Market clearing algorithm

- Market clearing algorithm based on Available Transmission Capacities (**ATC**)

$$\begin{aligned}
 \min_{\mathbf{g}, \mathbf{f}} \quad & \mathbf{c}^T \mathbf{g} \\
 \text{s.t.} \quad & \underline{\mathbf{G}} \leq \mathbf{g} \leq \bar{\mathbf{G}} \\
 & -\underline{\text{ATC}} \leq \mathbf{f} \leq \overline{\text{ATC}} \\
 & \mathbf{I}^d \mathbf{d} - \mathbf{I}^g \mathbf{g} + \mathbf{I}^f \mathbf{f} + \mathbf{p}^{* \text{loss}} = \mathbf{0}
 \end{aligned}$$

Market clearing algorithm

- Market clearing algorithm based on Available Transmission Capacities (**ATC**)
- Quadratic loss functions are used to calculate **linear approximations** to be introduced in the market.
- Utilization of **binary variables** to determine the direction of the flows.

$$\begin{array}{ll}
 \min_{\mathbf{g}, \mathbf{f}, \mathbf{f}^+, \mathbf{u}, \mathbf{p}^{\text{loss}}} & \mathbf{c}^T \mathbf{g} \\
 \text{s.t.} & \underline{\mathbf{G}} \leq \mathbf{g} \leq \bar{\mathbf{G}} \\
 & \left\{ \begin{array}{l} \mathbf{f} = \mathbf{f}^+ - \mathbf{f}^- \\ 0 \leq \mathbf{f}^+ \leq \mathbf{u} \overline{\text{ATC}} \\ 0 \leq \mathbf{f}^- \leq (1 - \mathbf{u}) \underline{\text{ATC}} \\ \mathbf{u} \in \{0, 1\} \end{array} \right. \\
 & \left\{ \begin{array}{l} \mathbf{p}^{\text{loss}} = \alpha (\mathbf{f}^+ + \mathbf{f}^-) + \beta \\ |\mathbf{d}| - |\mathbf{g}| + |\mathbf{f}| + \mathbf{D}^{\text{loss}} \mathbf{p}^{\text{loss}} = 0 \end{array} \right.
 \end{array}$$

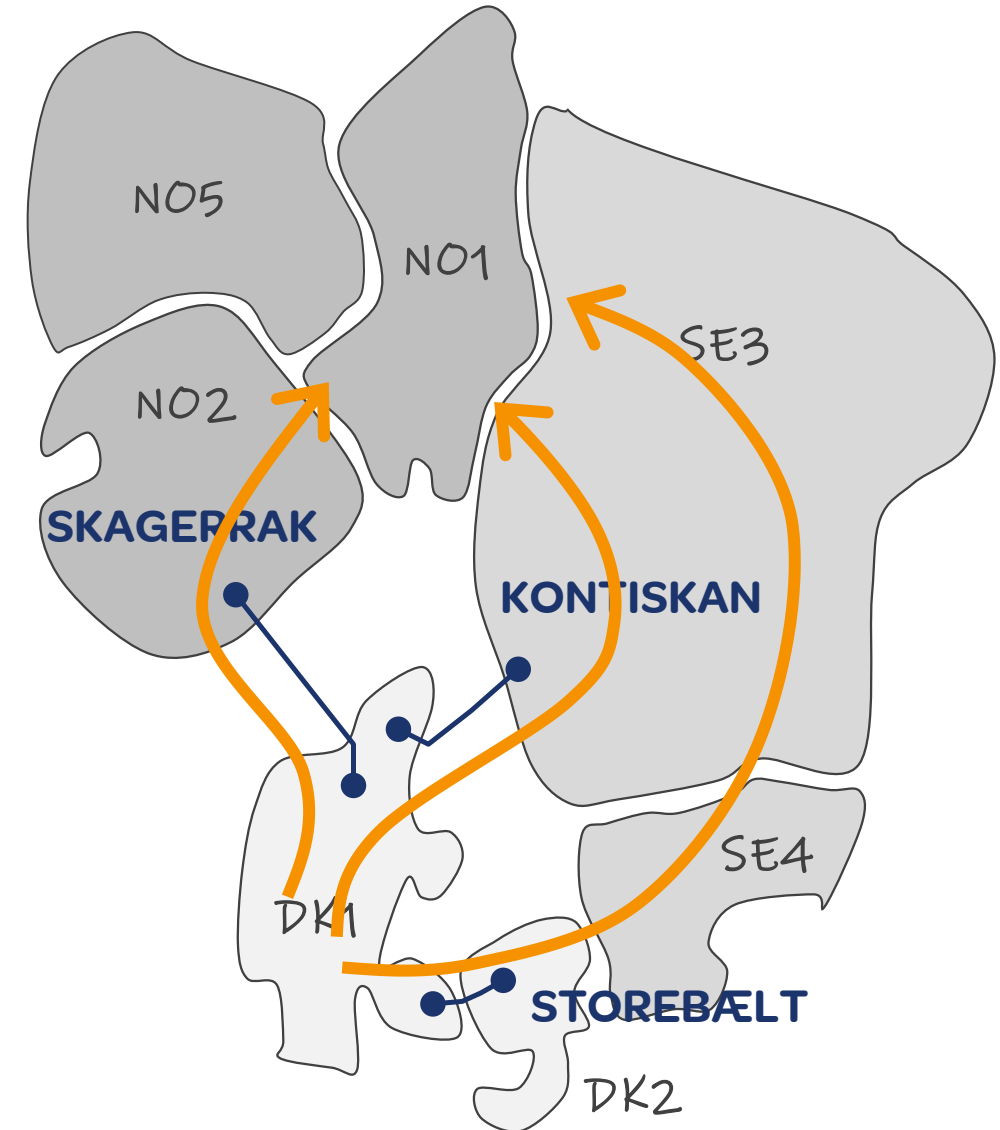
Market clearing algorithm

- Market clearing algorithm based on Available Transmission Capacities (**ATC**)
- Quadratic loss functions are used to calculate **linear approximations** to be introduced in the market.
- Utilization of **binary variables** to determine the direction of the flows.
- Investigation of:
 - **linear** and **piecewise linear** loss factors.
 - **HVDC** and **AC** loss factors.

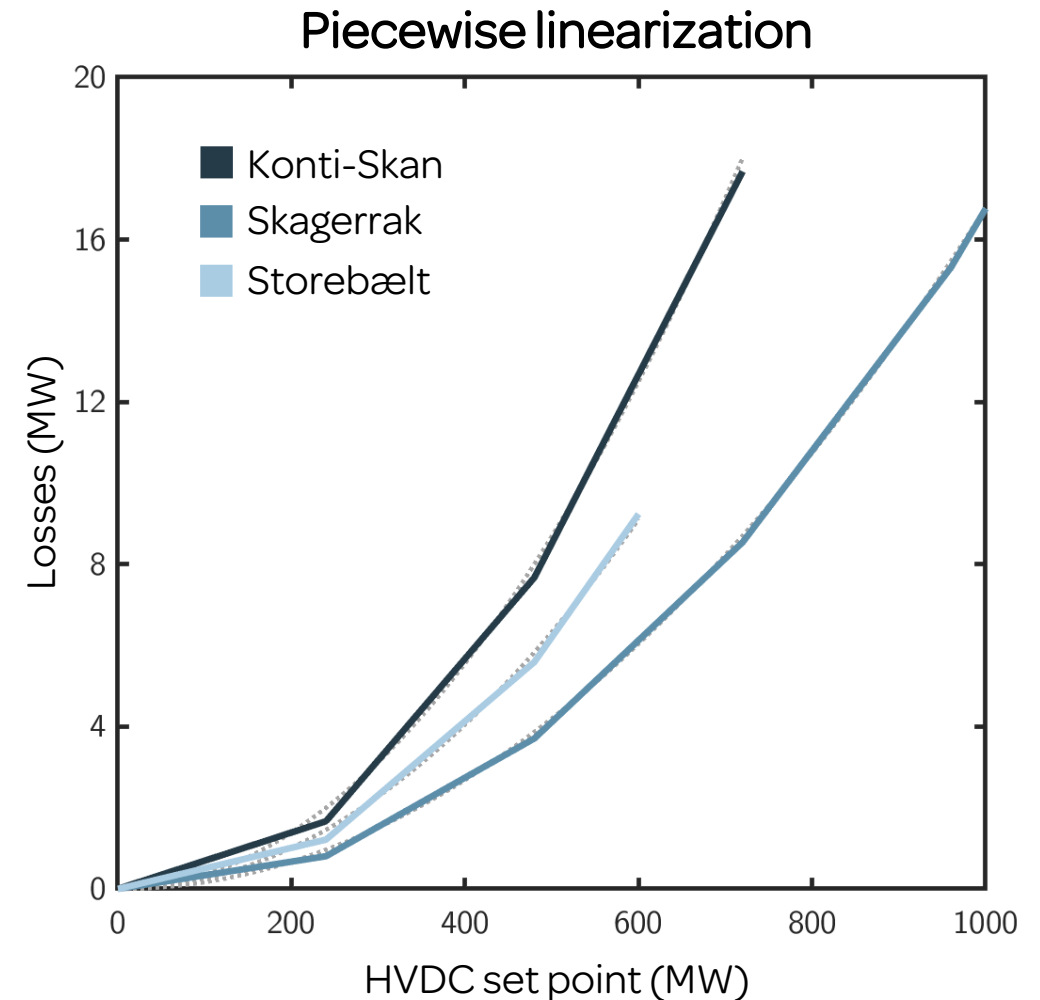
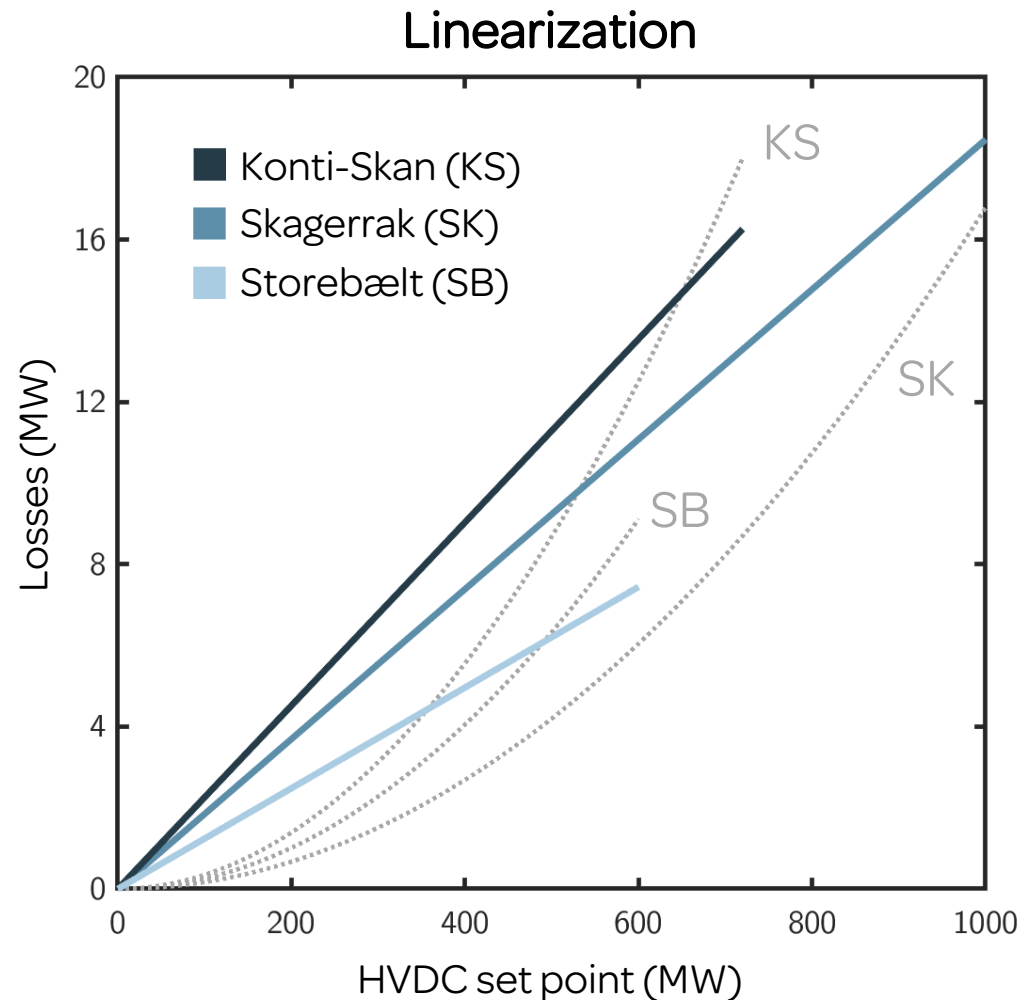
$$\begin{aligned}
 & \min_{\mathbf{g}, \mathbf{f}, \mathbf{f}_k^\pm, \mathbf{u}_k^\pm, \mathbf{p}^{\text{loss}}} \quad \mathbf{c}^T \mathbf{g} \\
 & \text{s.t.} \quad \underline{\mathbf{G}} \leq \mathbf{g} \leq \bar{\mathbf{G}} \\
 & \text{flow definition} \quad \left\{ \begin{aligned} & \mathbf{f} = \sum_k (\mathbf{f}_k^+ - \mathbf{f}_k^-) \\ & (\mathbf{u}_k^\pm - \mathbf{u}_{k+1}^\pm) \bar{\mathbf{F}}_{k-1} \leq \mathbf{f}_k^\pm \leq (\mathbf{u}_k^\pm - \mathbf{u}_{k+1}^\pm) \bar{\mathbf{F}}_k \quad \forall k \neq K \\ & \mathbf{u}_K^\pm \bar{\mathbf{F}}_{K-1} \leq \mathbf{f}_K^\pm \leq \mathbf{u}_K^\pm \bar{\mathbf{F}}_K \\ & \mathbf{u}_k^\pm \geq \mathbf{u}_{k+1}^\pm \quad \forall k \neq K \\ & \mathbf{u}_k^\pm \in \{0,1\} \quad \forall k \neq K \end{aligned} \right. \\
 & \text{loss definition} \quad \left\{ \begin{aligned} & \mathbf{p}^{\text{loss}} = \sum_k \alpha_k (\mathbf{f}_k^+ - \mathbf{f}_k^-) + \\ & \quad + \sum_{k \neq K} \beta_k (\mathbf{u}_k^+ - \mathbf{u}_{k+1}^+ + \mathbf{u}_k^- - \mathbf{u}_{k+1}^-) + \\ & \quad + \beta_K (\mathbf{u}_K^+ + \mathbf{u}_K^-) \end{aligned} \right. \\
 & \quad \quad \quad |\mathbf{d}| - |\mathbf{g}| + |\mathbf{f}| + \mathbf{D}^{\text{loss}} \mathbf{p}^{\text{loss}} = 0
 \end{aligned}$$

Linear vs. Piecewise-linear

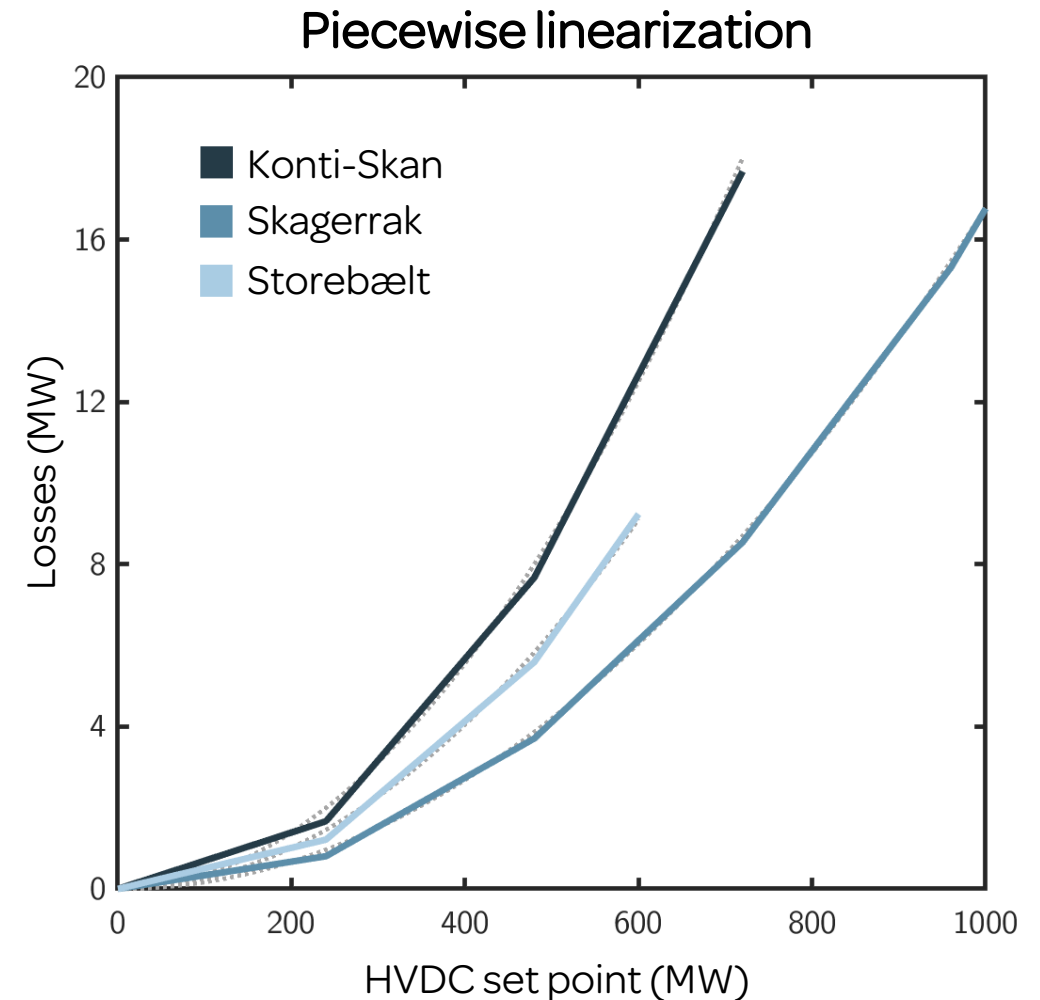
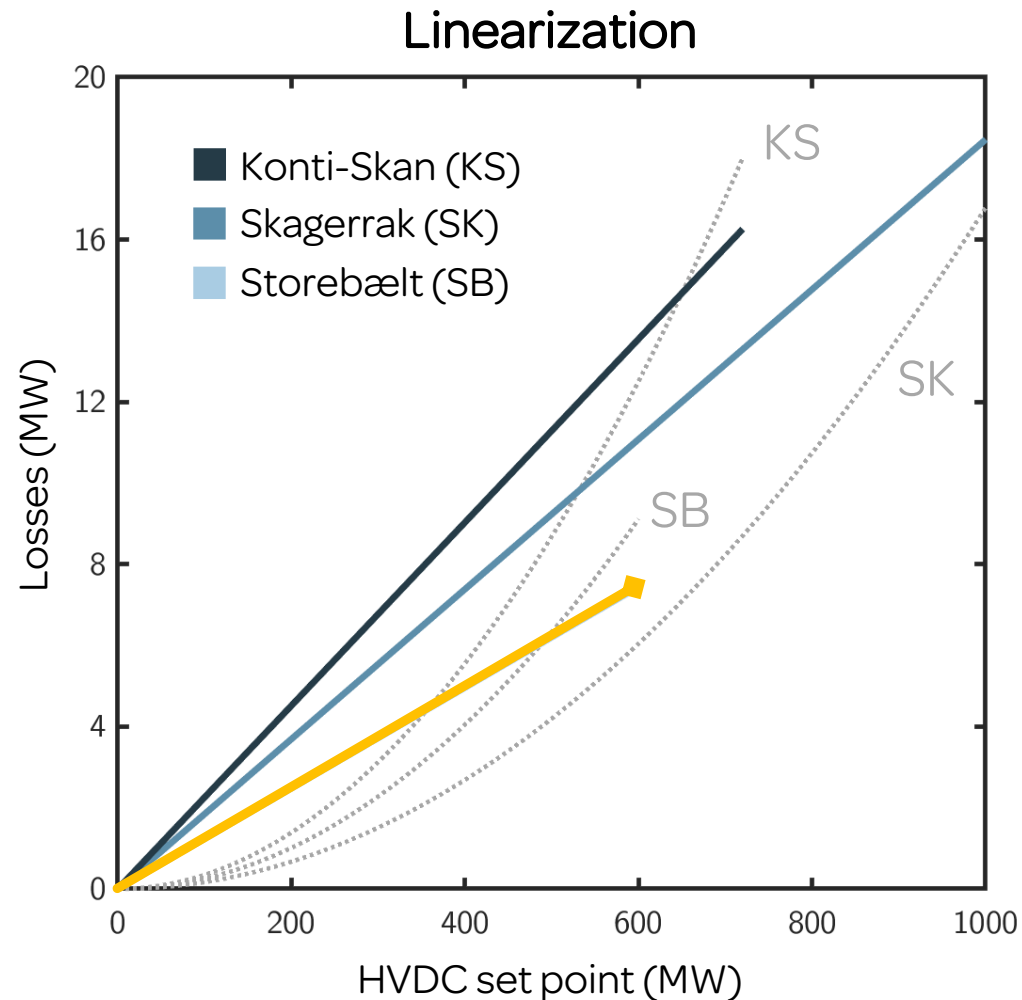
- Losses are **non-linear**.
- Linear loss factors **unfairly penalize one HVDC** line over the other.
- What happens if there are several **parallel** HVDC paths?
 - This is the case of Skagerrak, Kontiskan and Storebælt.



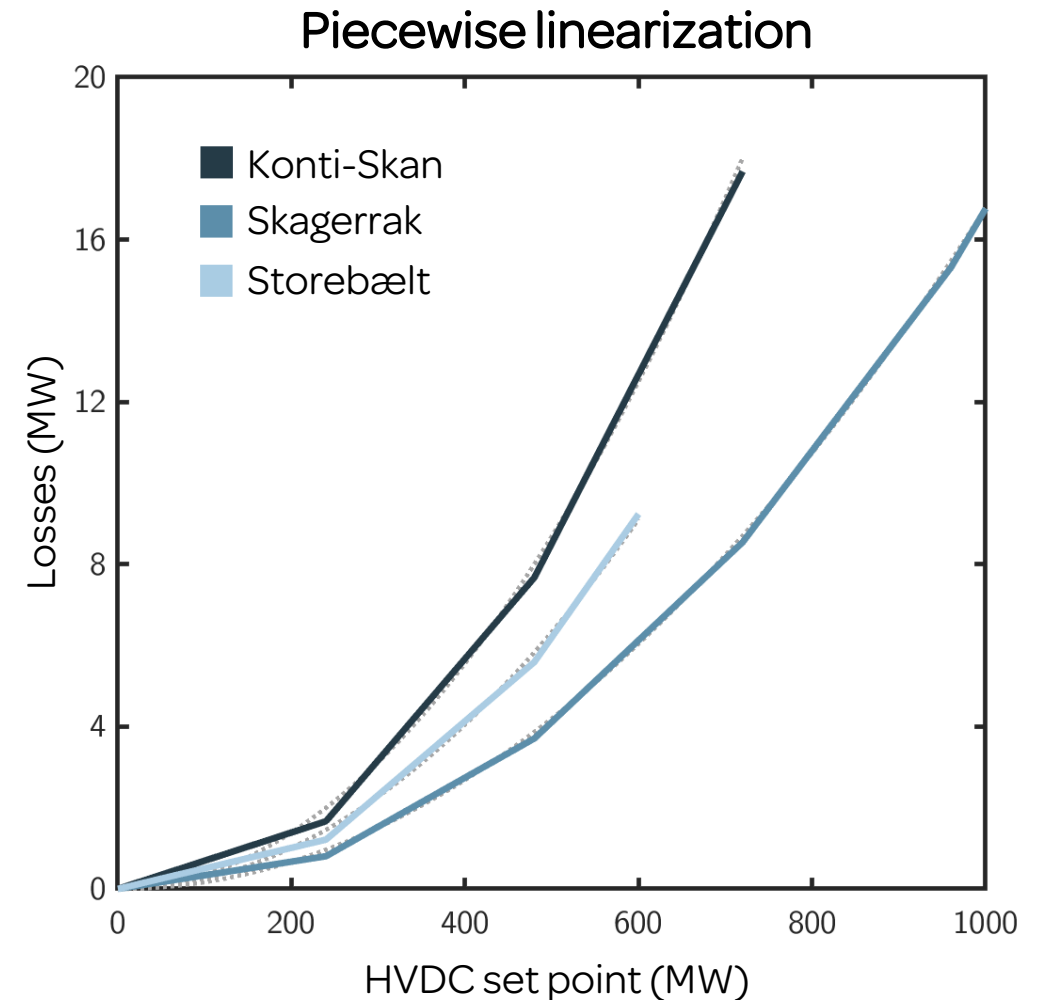
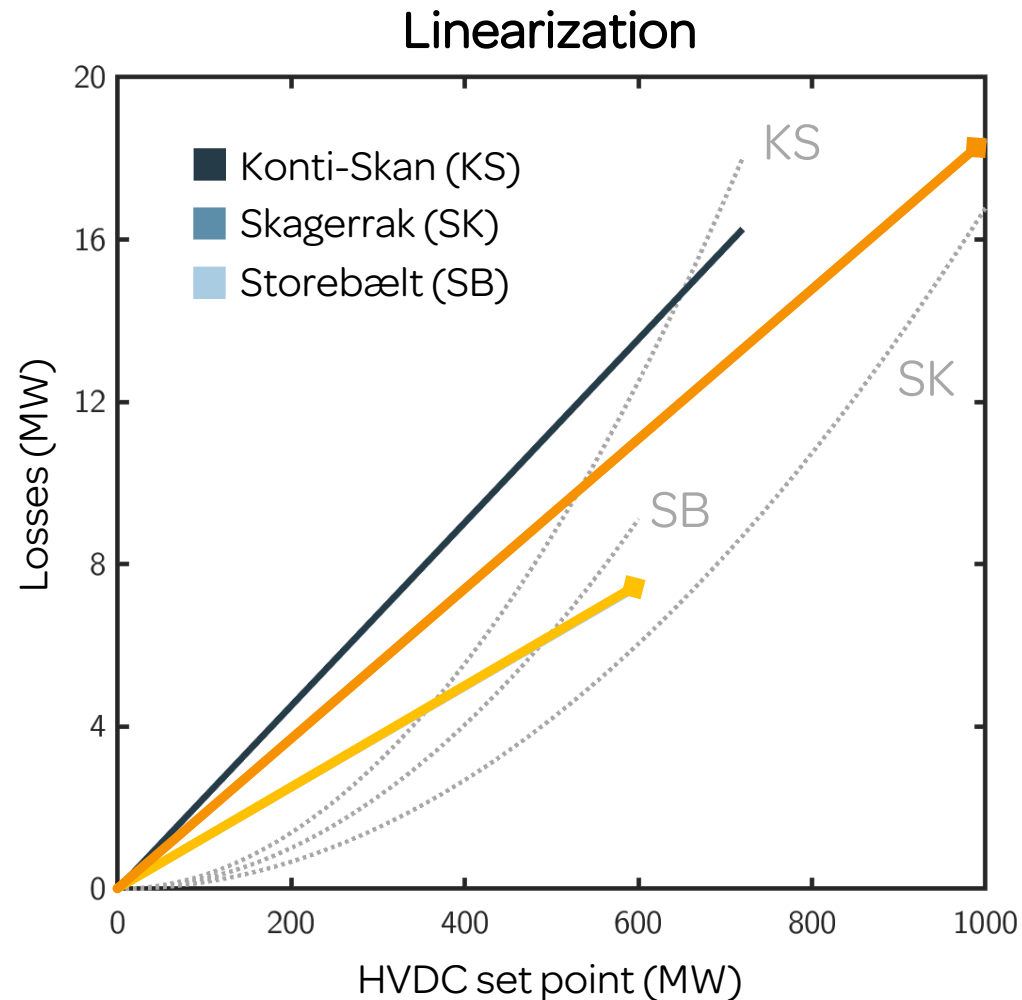
Linear vs. Piecewise-linear



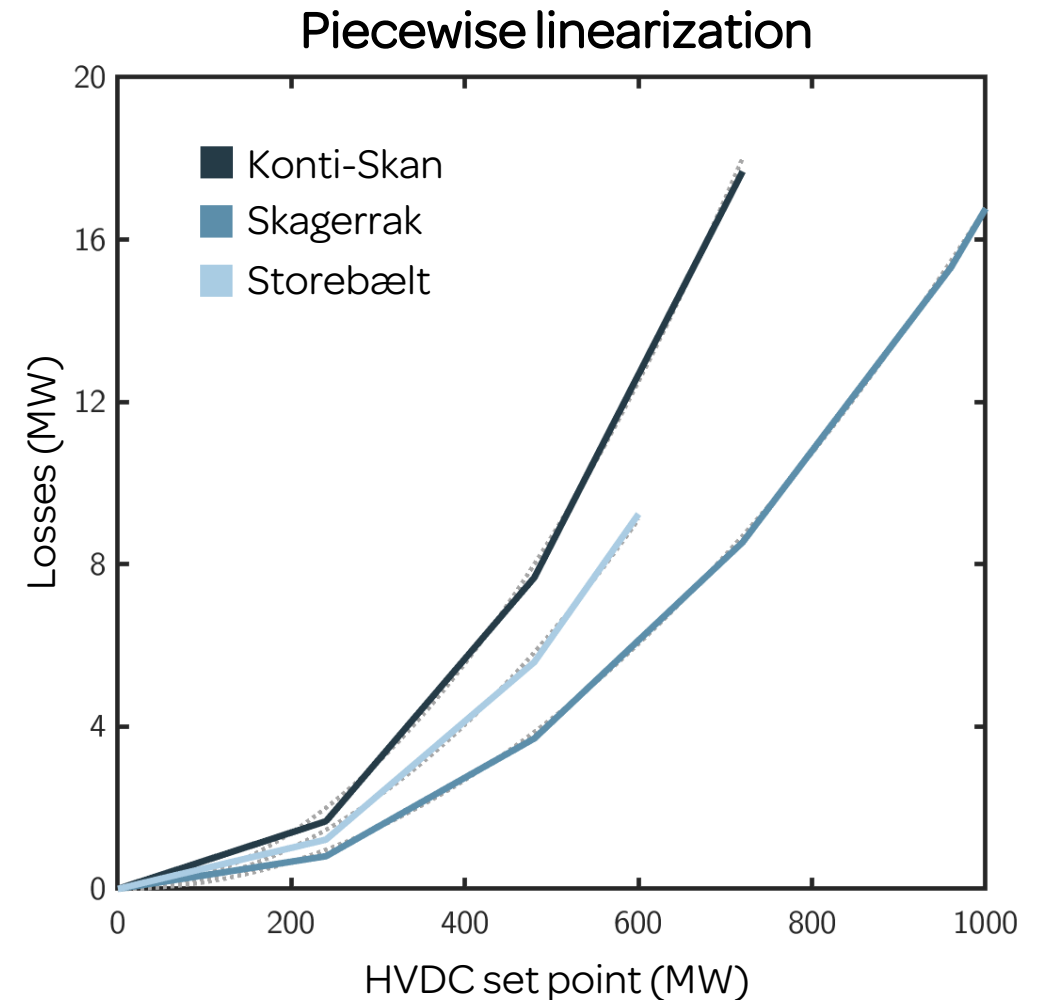
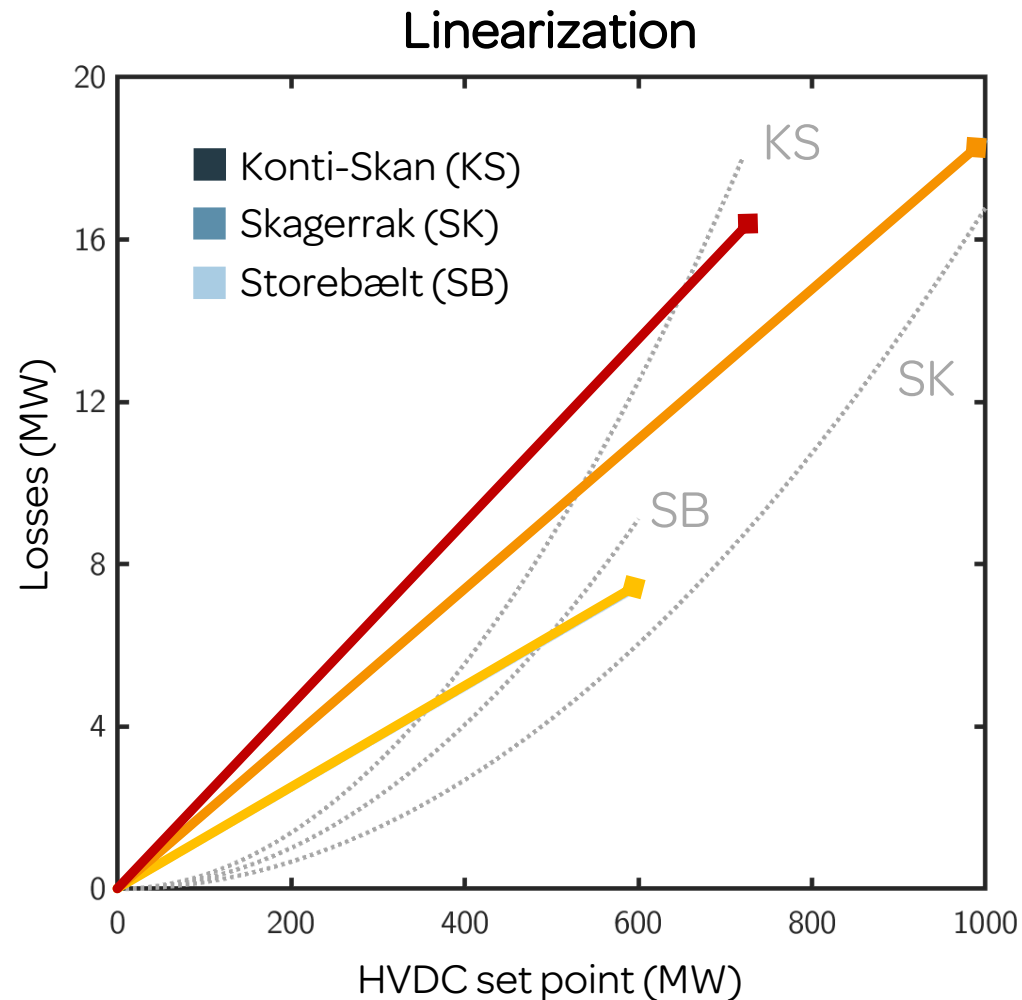
Linear vs. Piecewise-linear



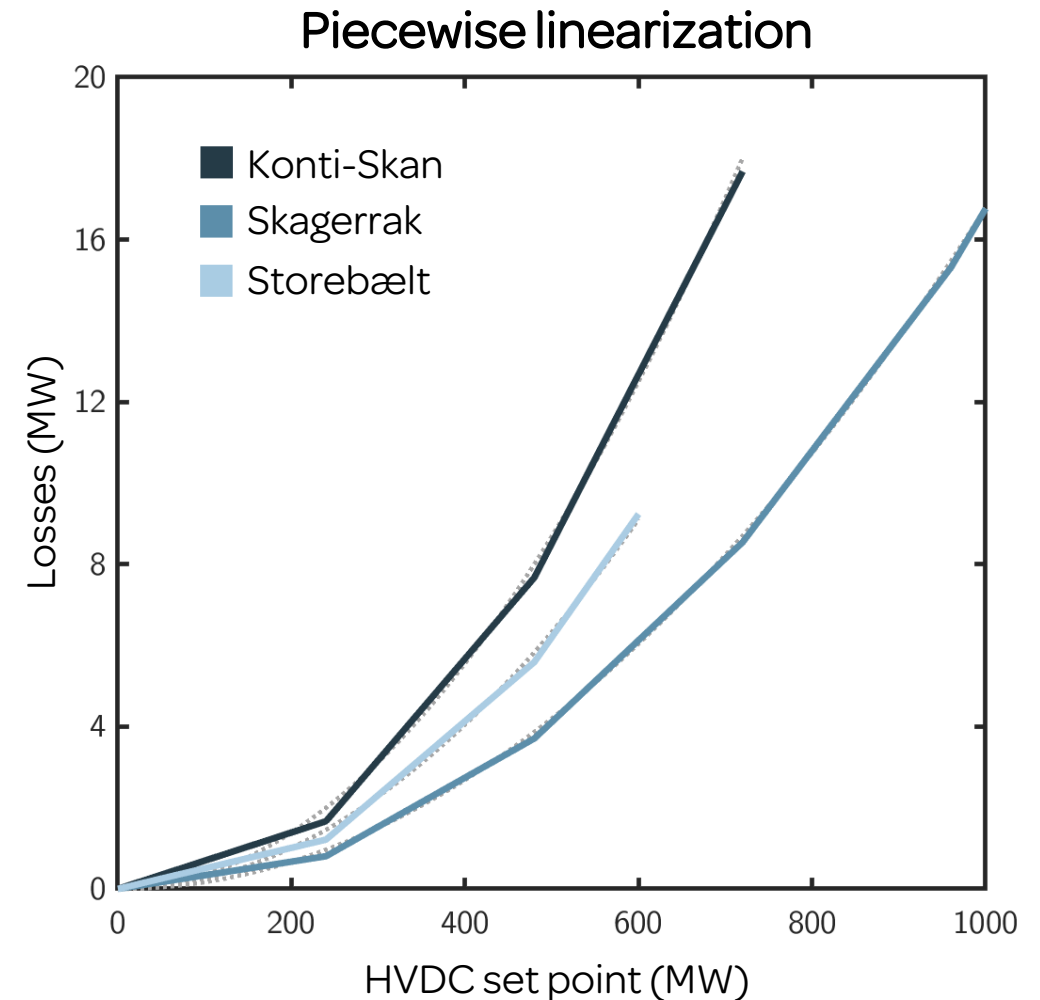
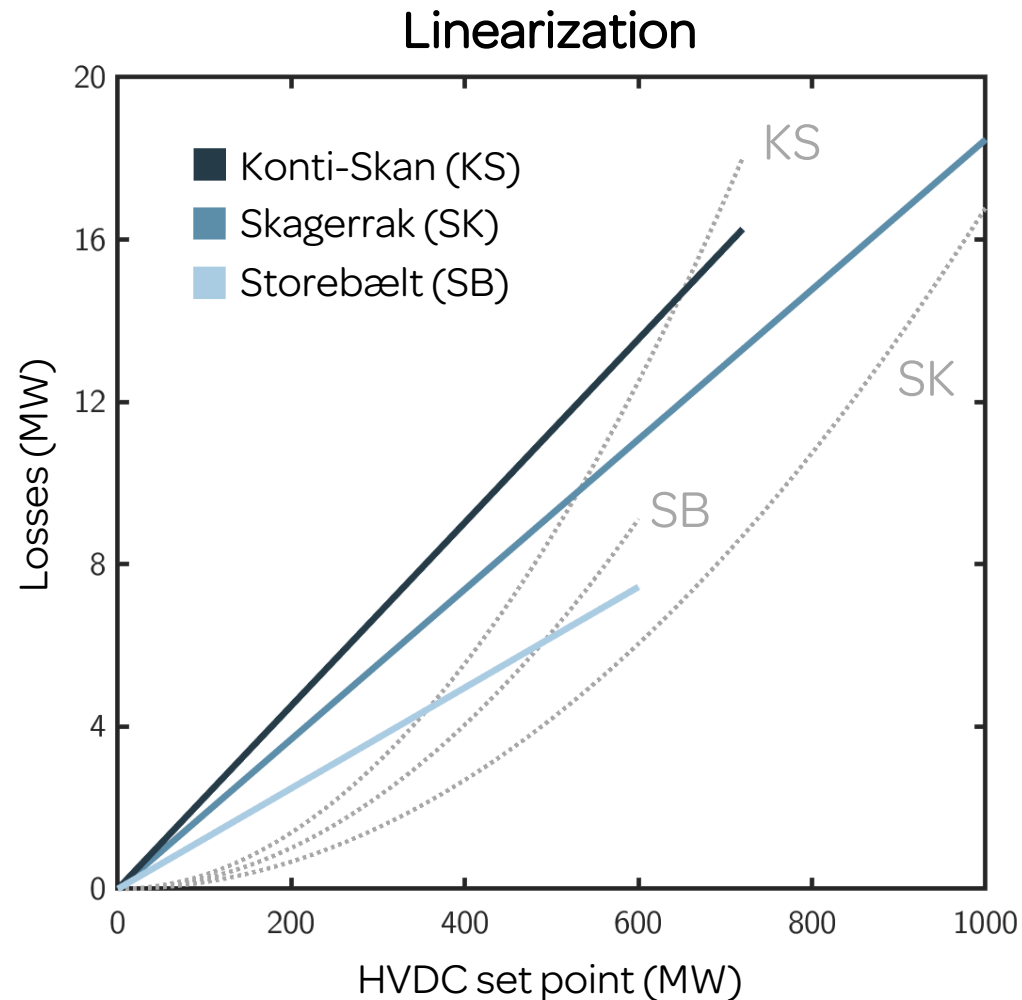
Linear vs. Piecewise-linear



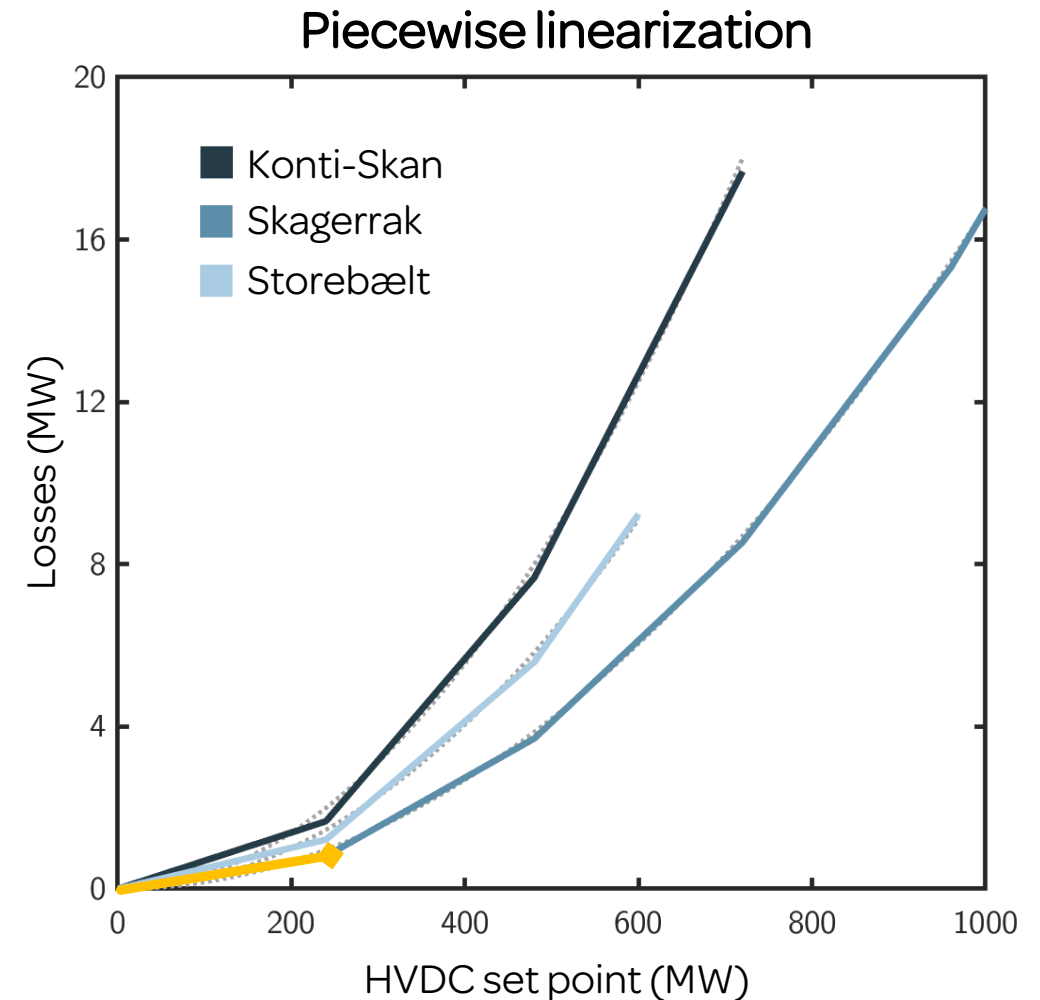
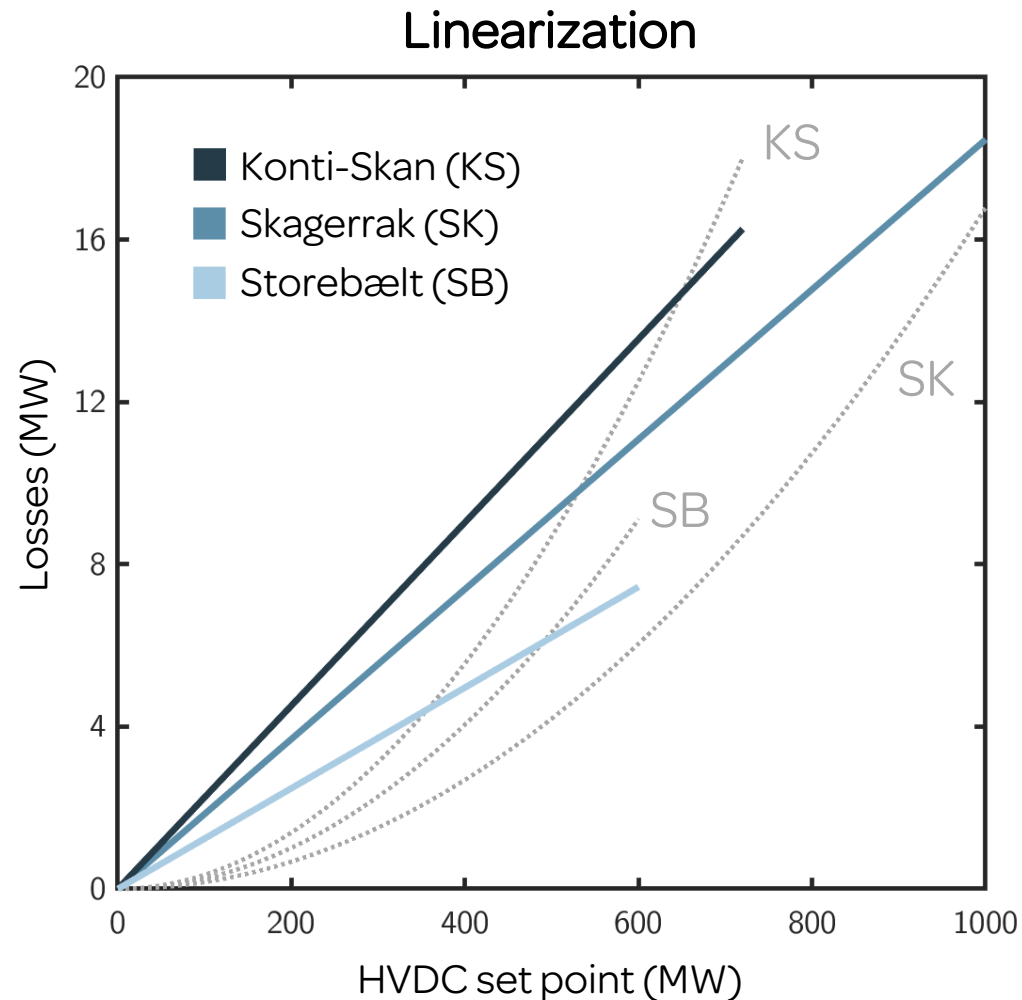
Linear vs. Piecewise-linear



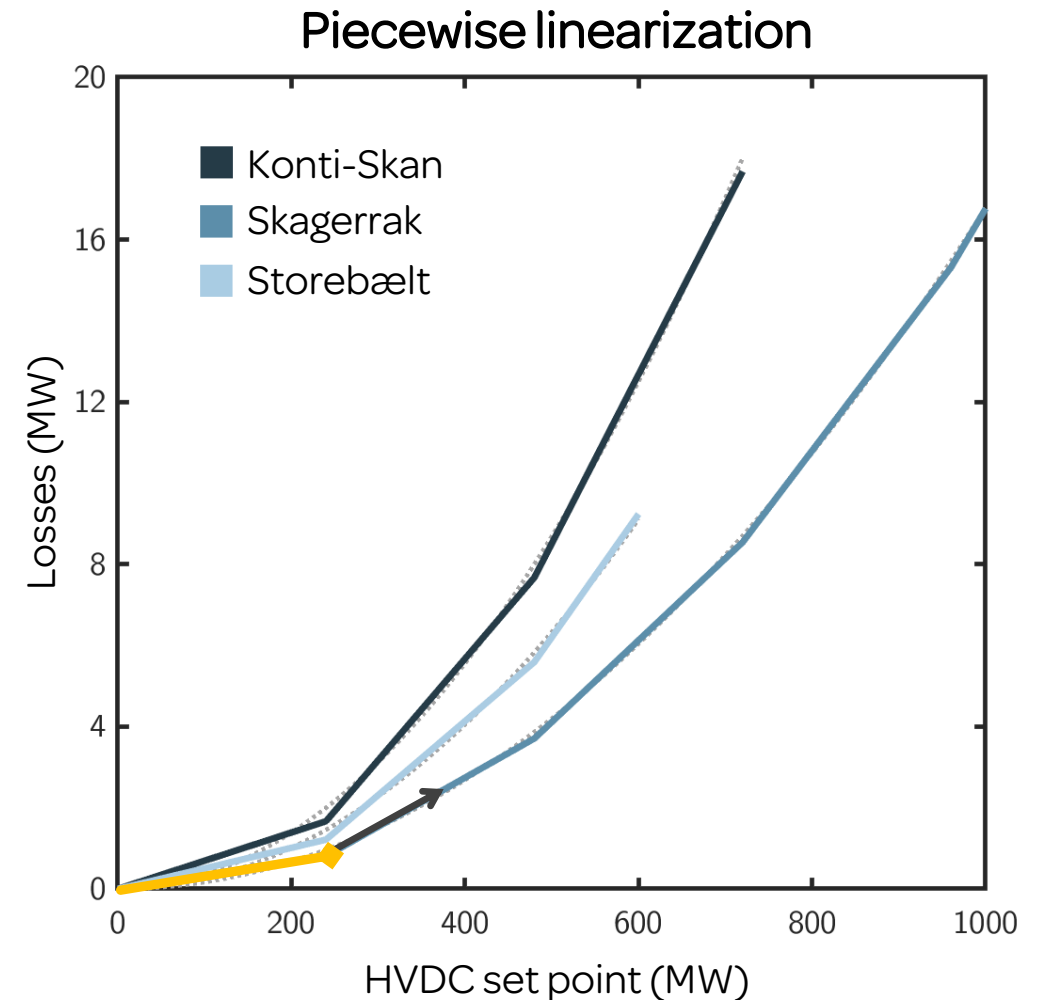
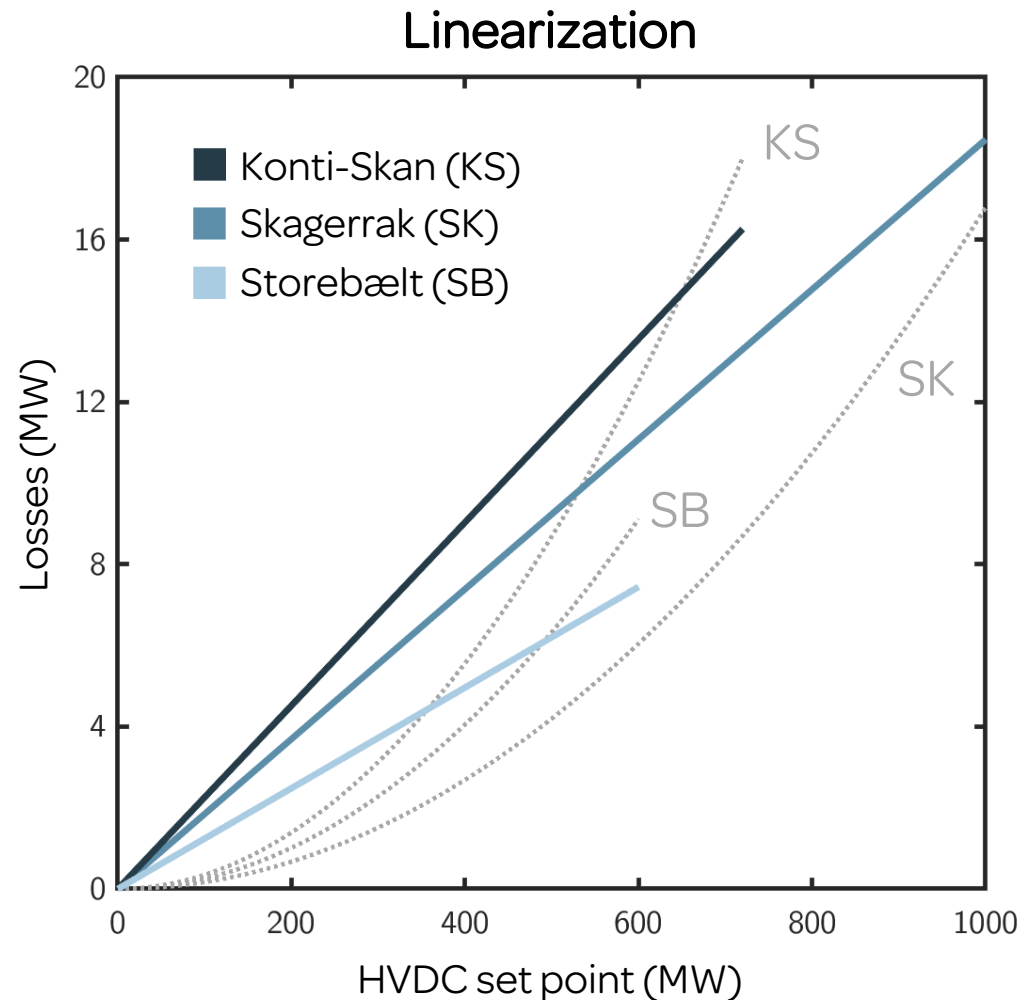
Linear vs. Piecewise-linear



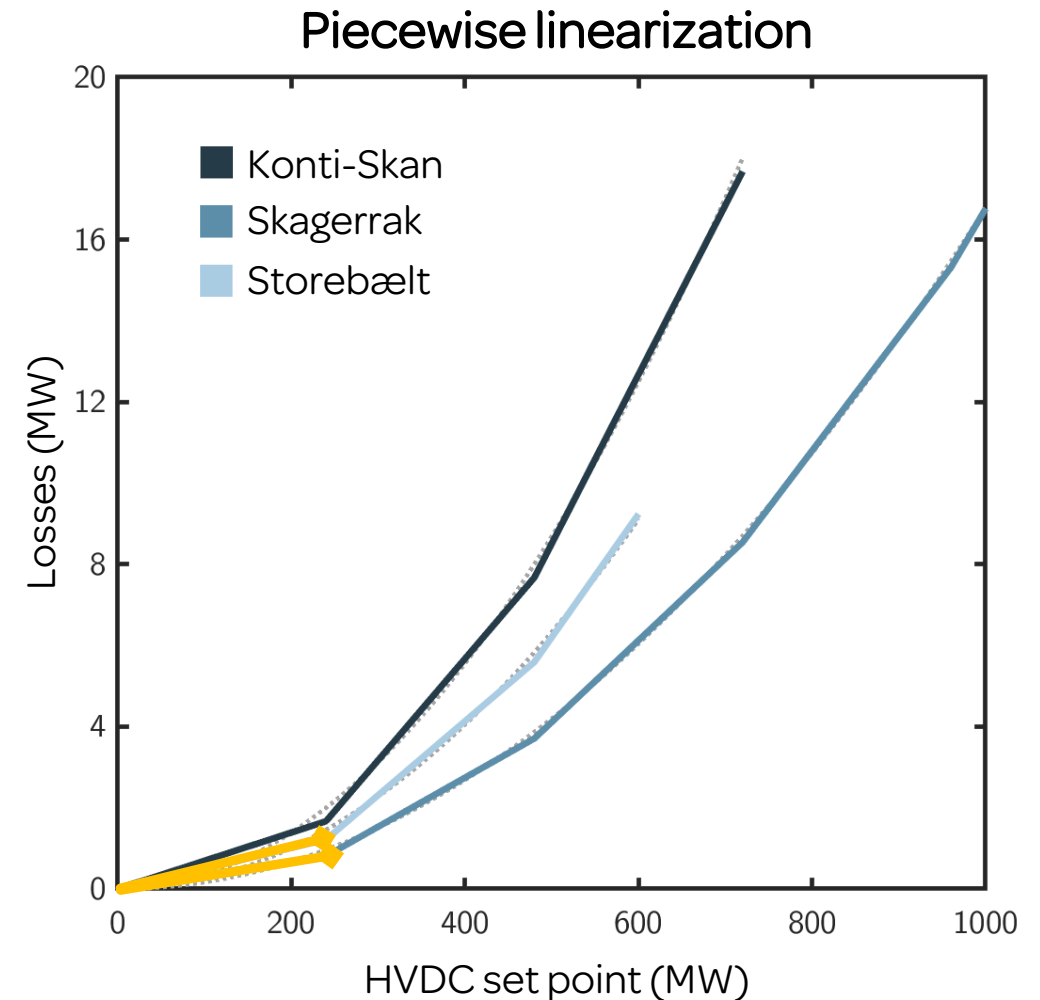
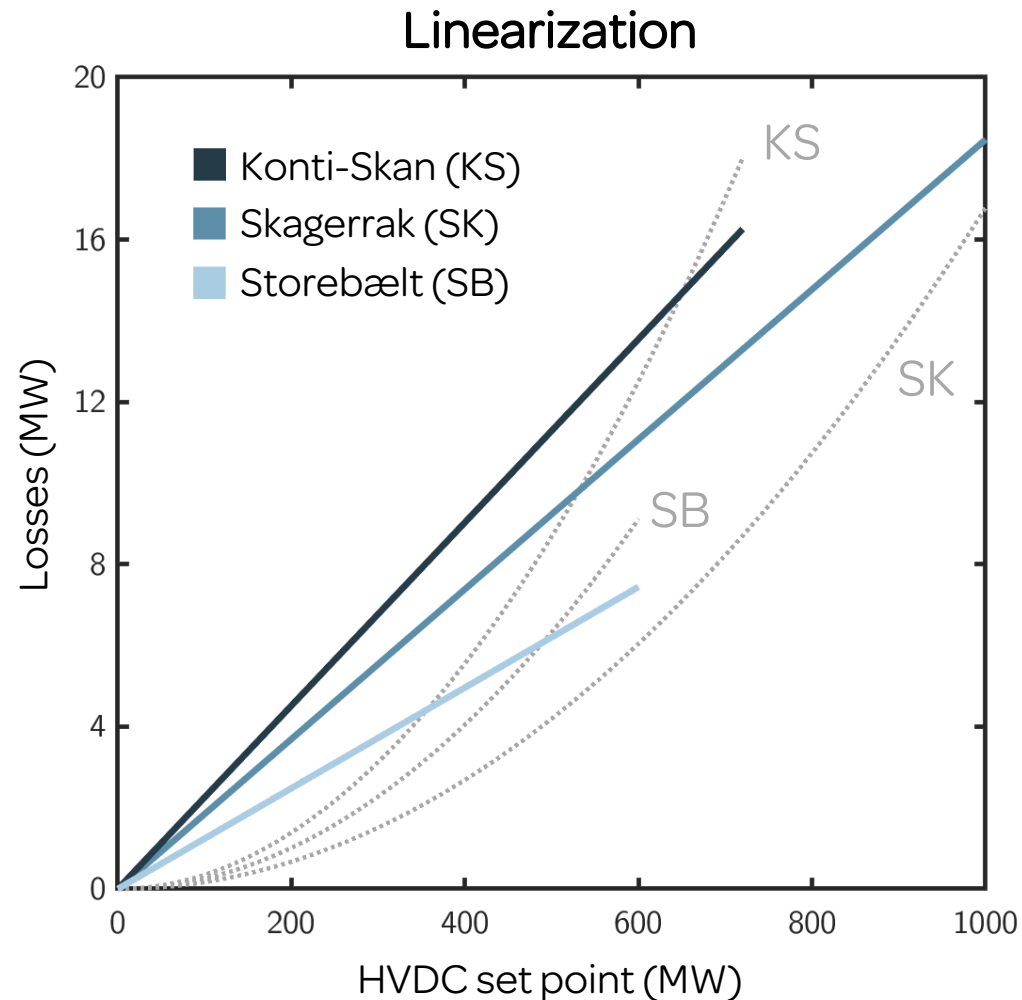
Linear vs. Piecewise-linear



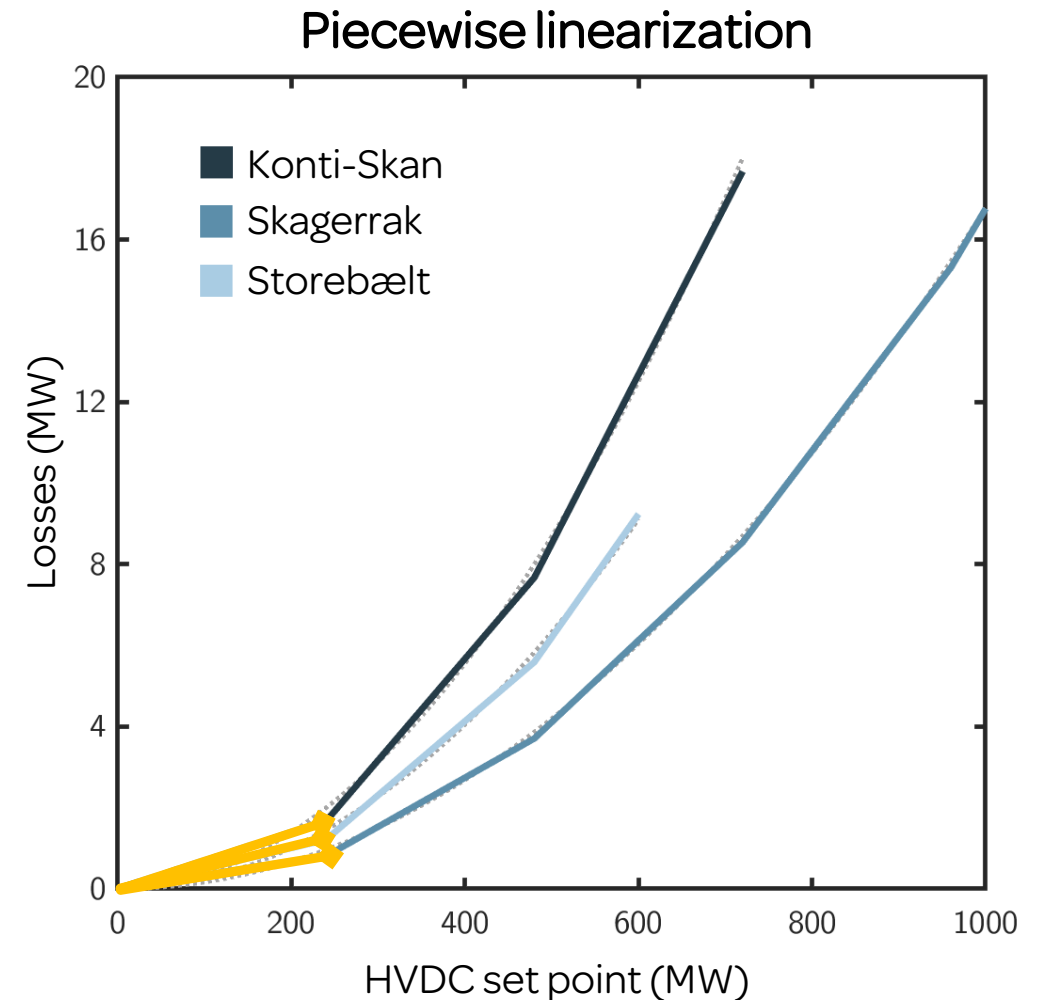
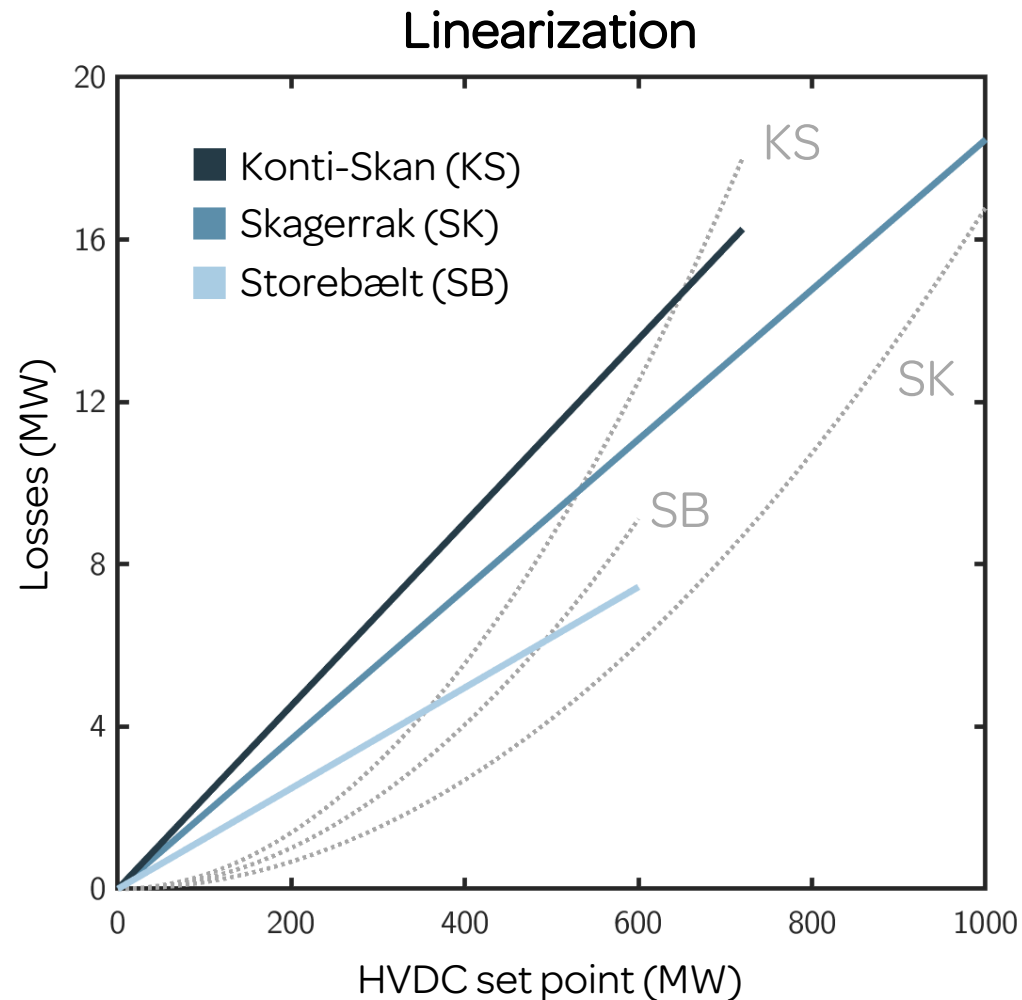
Linear vs. Piecewise-linear



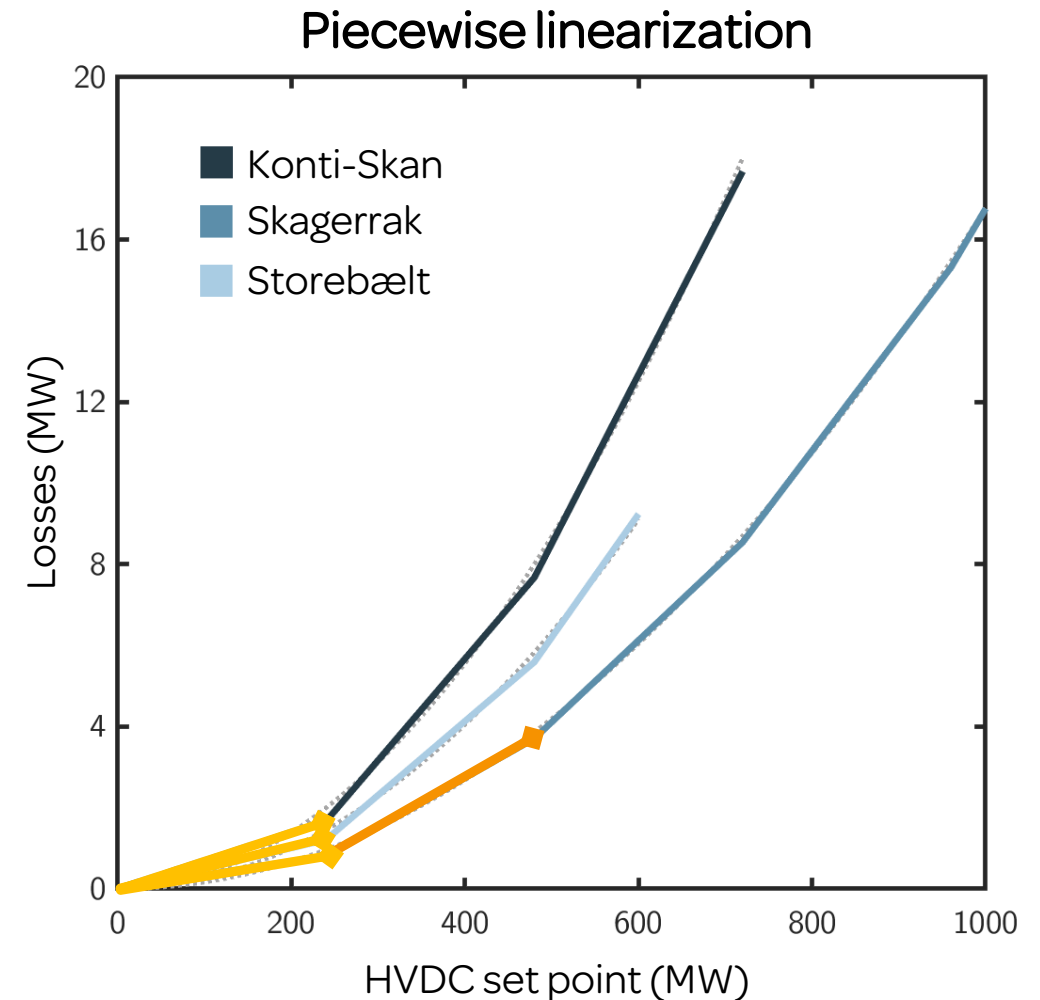
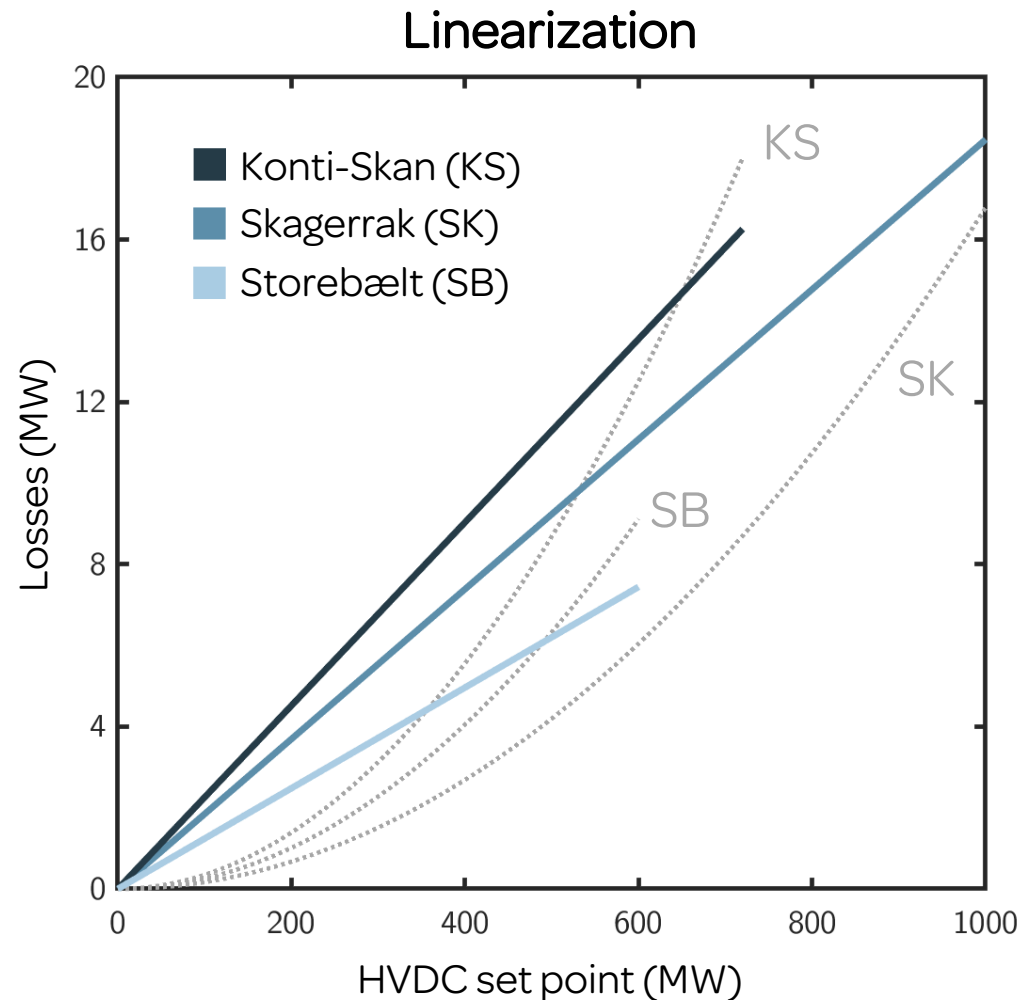
Linear vs. Piecewise-linear



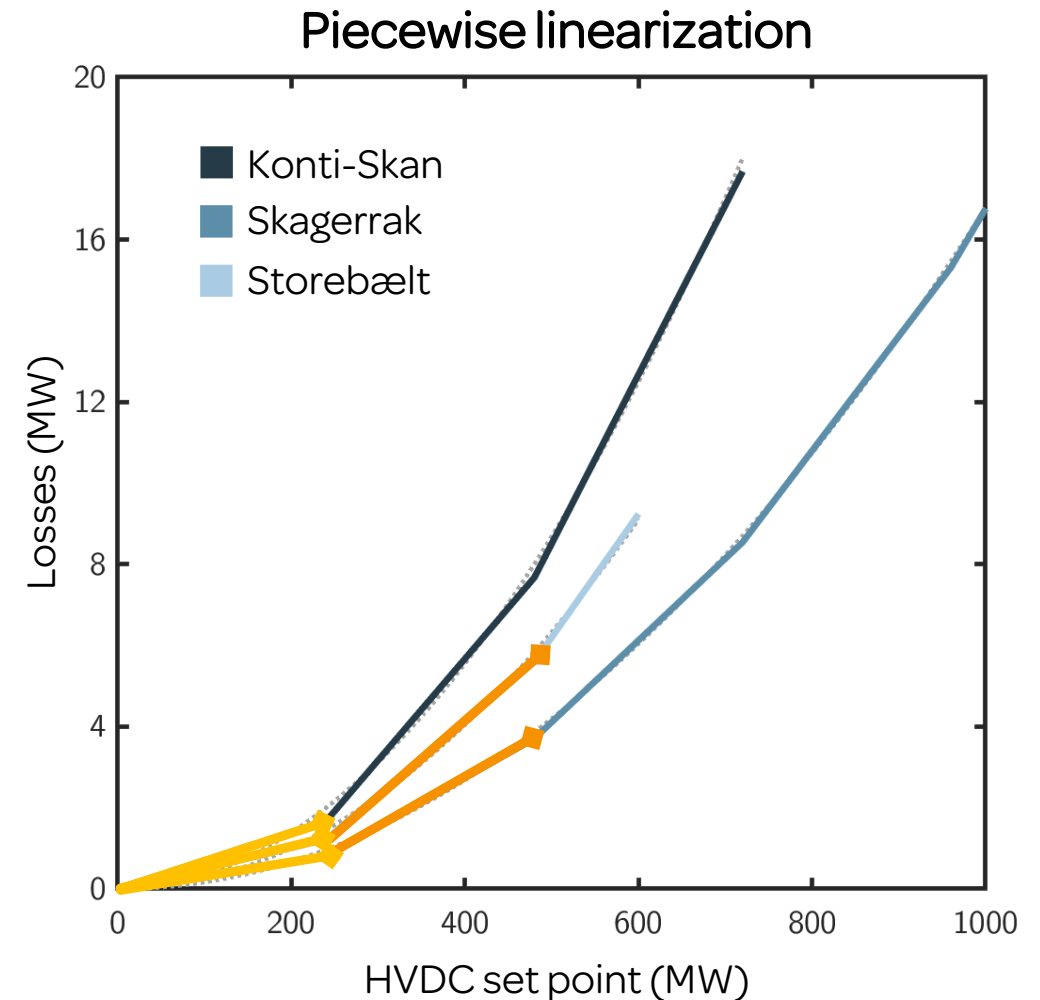
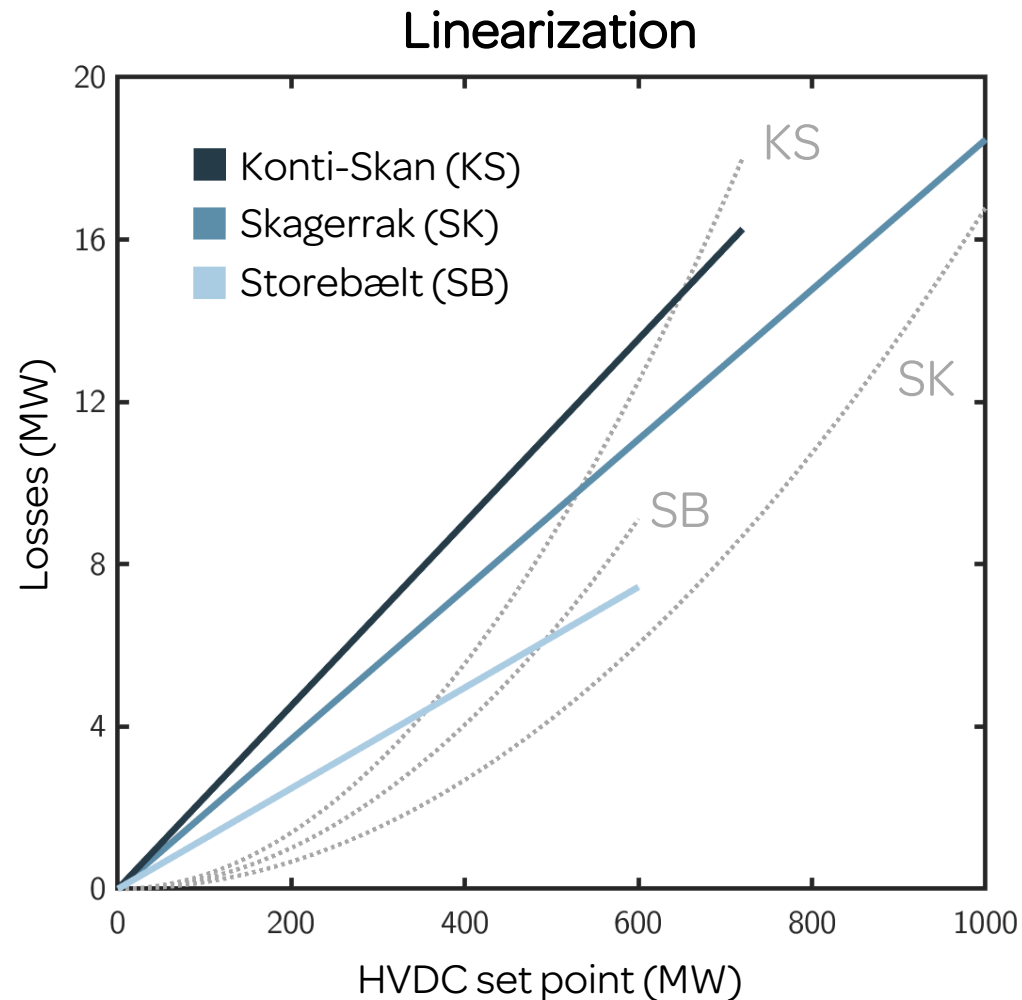
Linear vs. Piecewise-linear



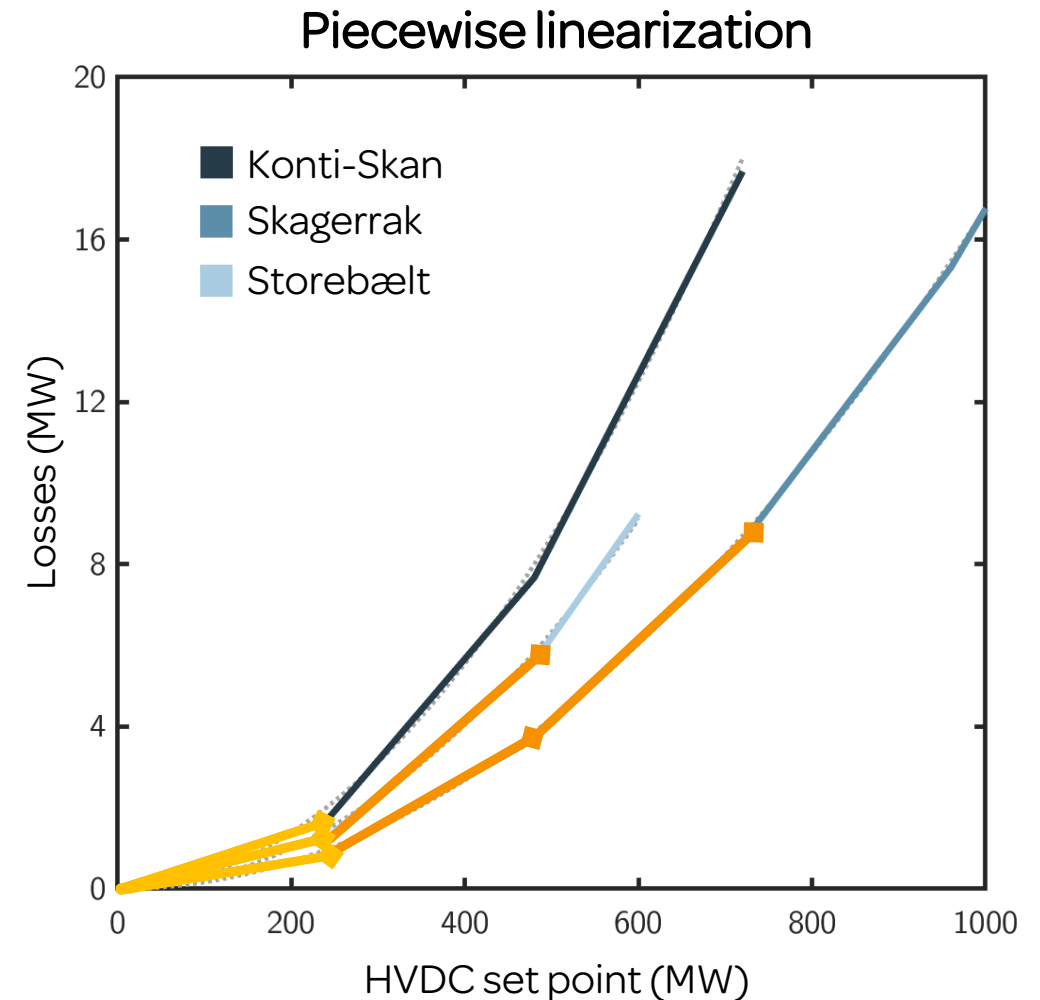
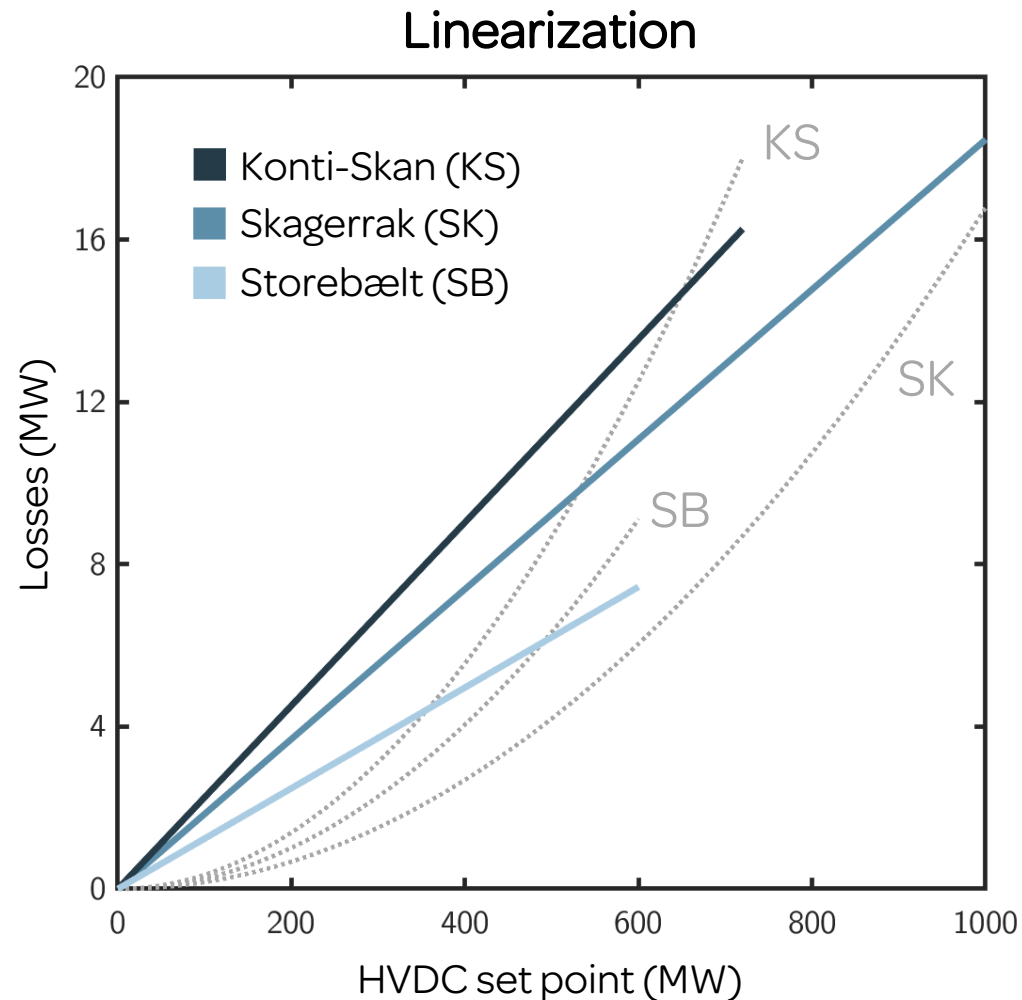
Linear vs. Piecewise-linear



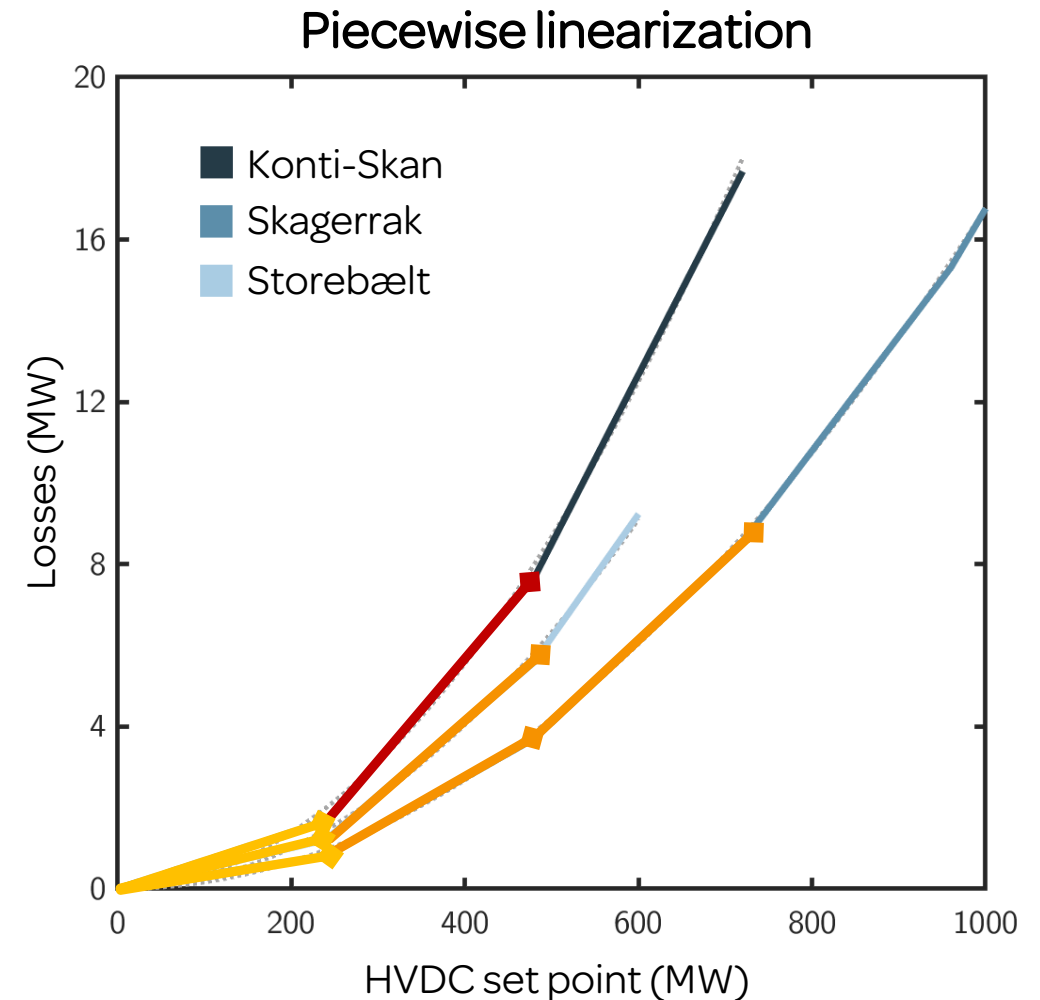
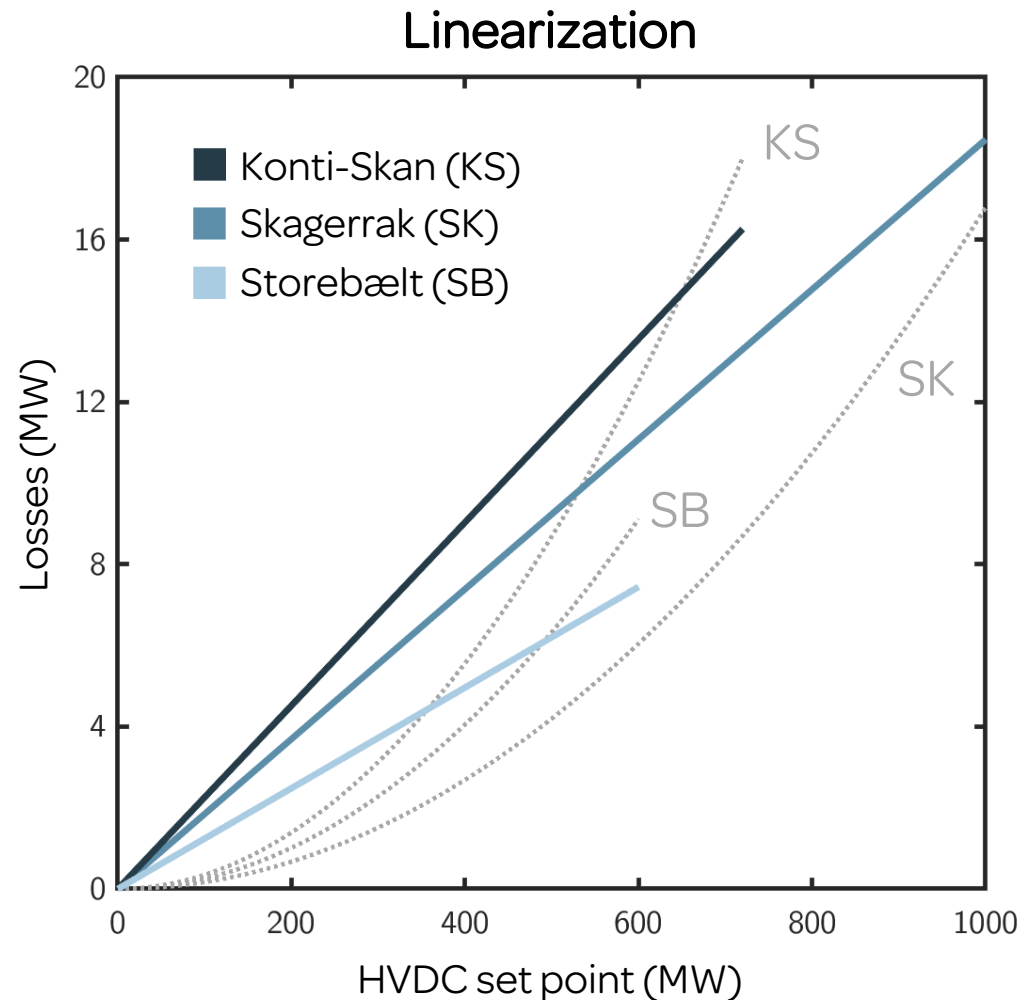
Linear vs. Piecewise-linear



Linear vs. Piecewise-linear

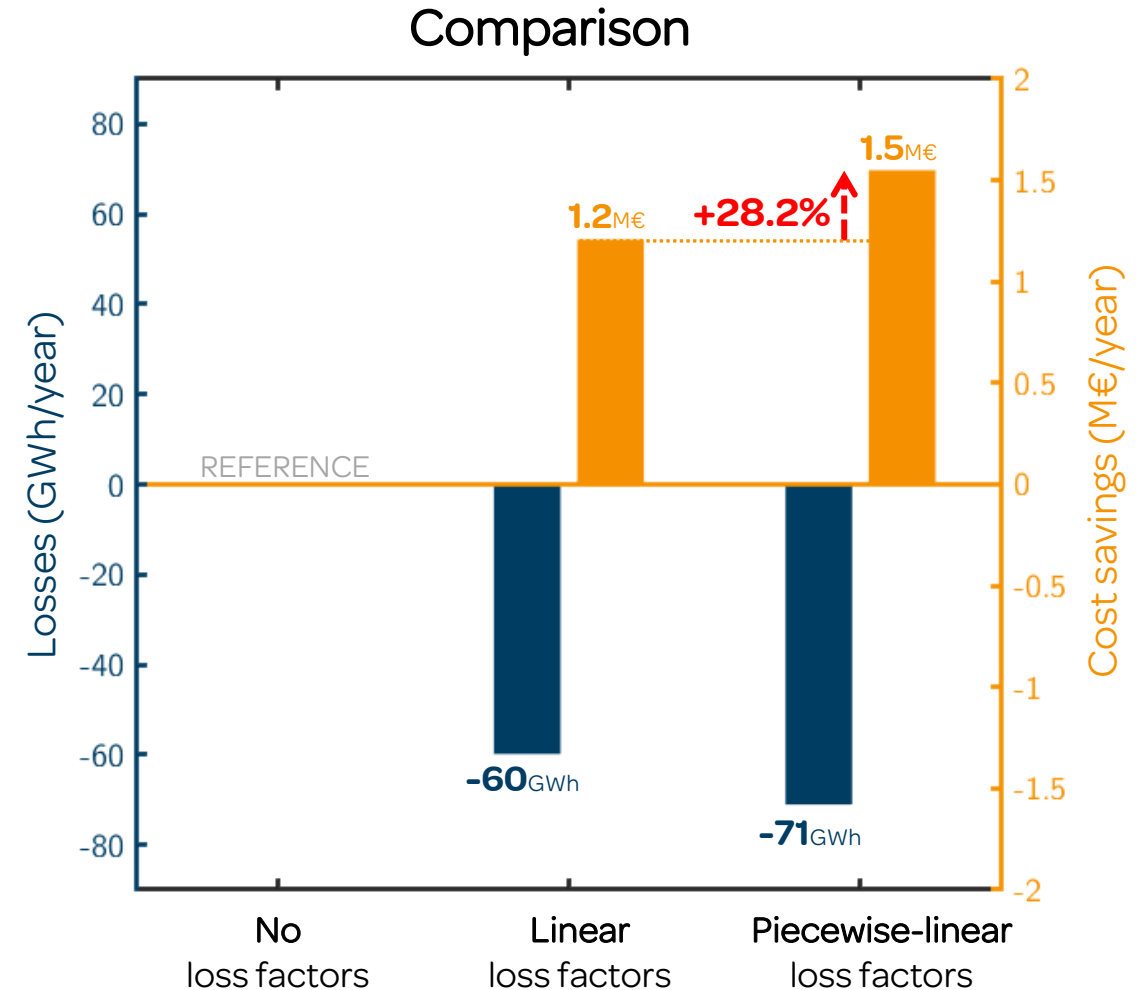


Linear vs. Piecewise-linear



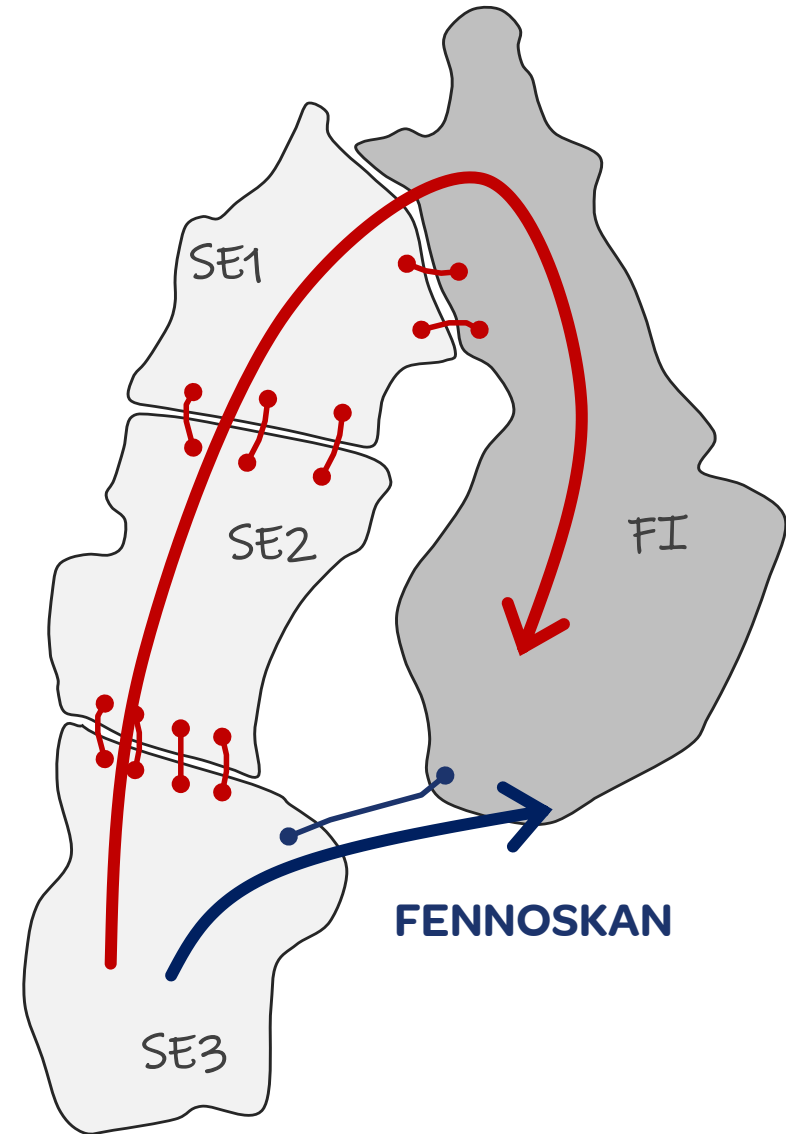
Linear vs. Piecewise-linear

- Piecewise-linear loss factors **better distribute the flows** over HVDC lines and losses are further decreased.
- Better **representation** of loss functions:
 - No under/over estimation of losses;
 - No discrimination in case of **merchant** lines.
- Cost savings increase by ~**30%**.
- **Recommendation**: use **piecewise-linear** loss factors.



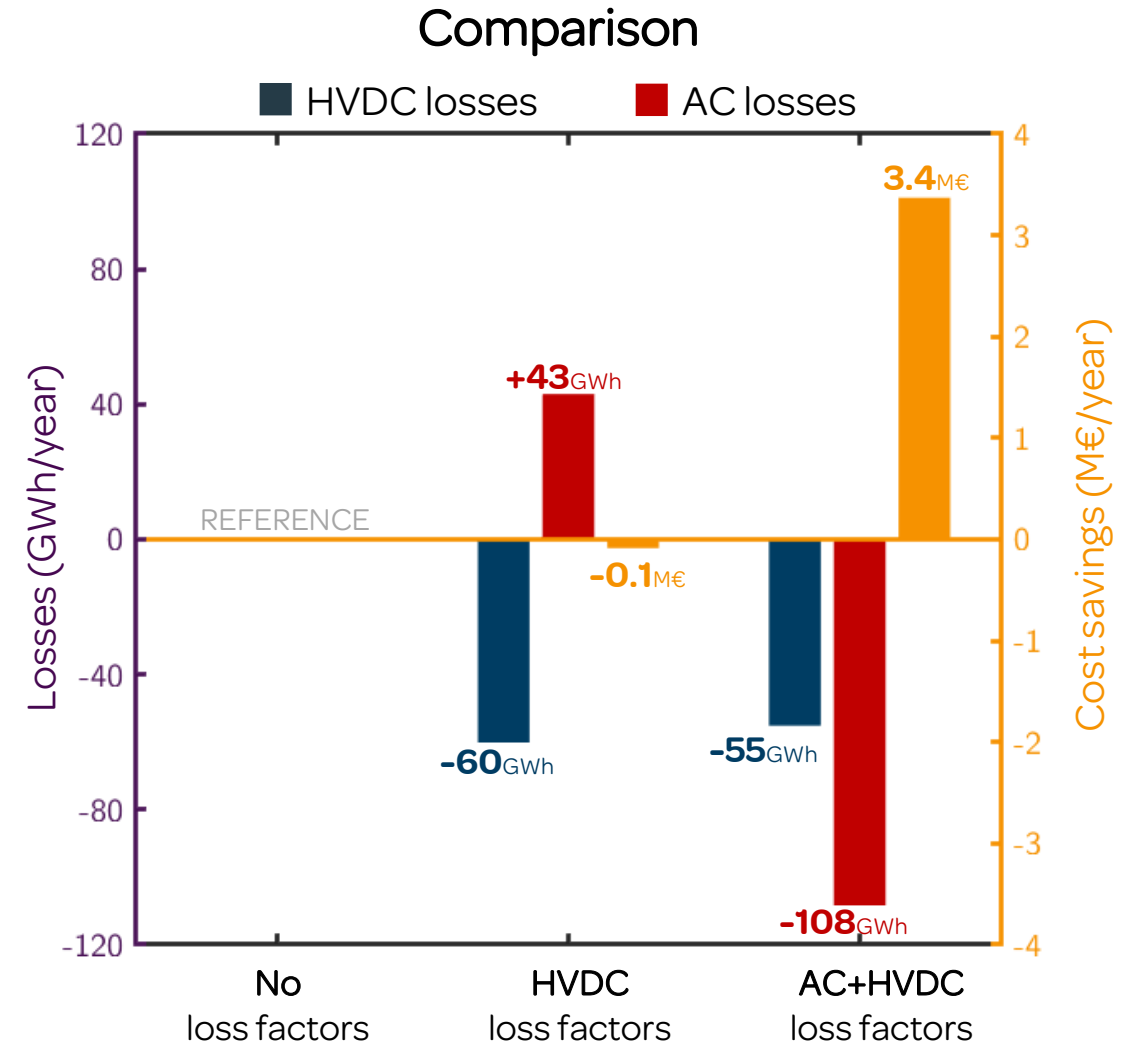
HVDC vs. AC+HVDC

- If introduced on only HVDC interconnectors, loss factors can **unfairly penalize** HVDC lines.
- What happens if there are parallel **AC paths**?
 - This is the case of Fennoskan.
- The solver will see the AC corridor as “**less costly**” and will reroute all the power through those lines.

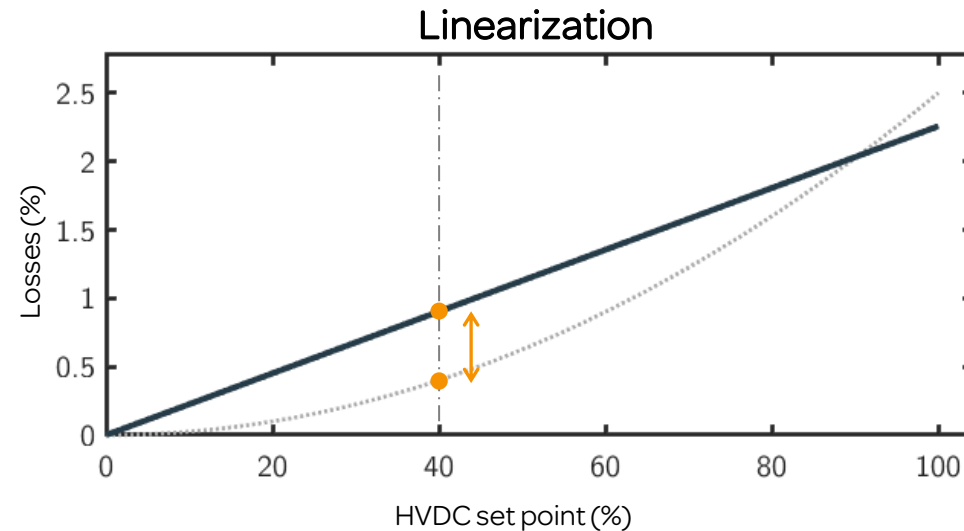


HVDC vs. AC+HVDC (linear loss factors)

- If we consider losses on AC interconnectors, HVDC loss factors are no longer effective.
- With both AC and HVDC loss factors, the total losses are **minimized (-7.4%)**.
- Substantial **cost savings** can be achieved.

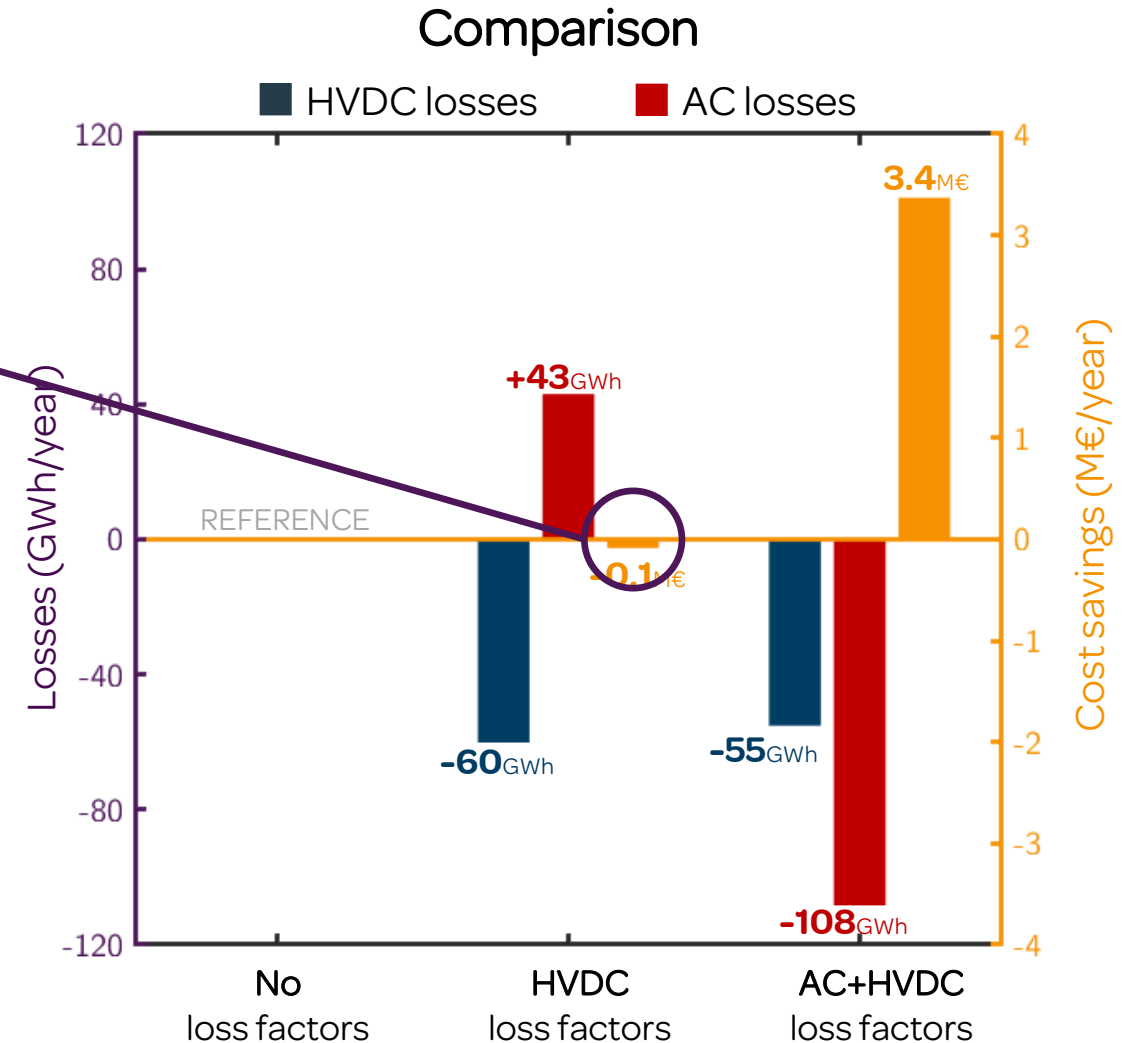


HVDC vs. AC+HVDC (linear loss factors)



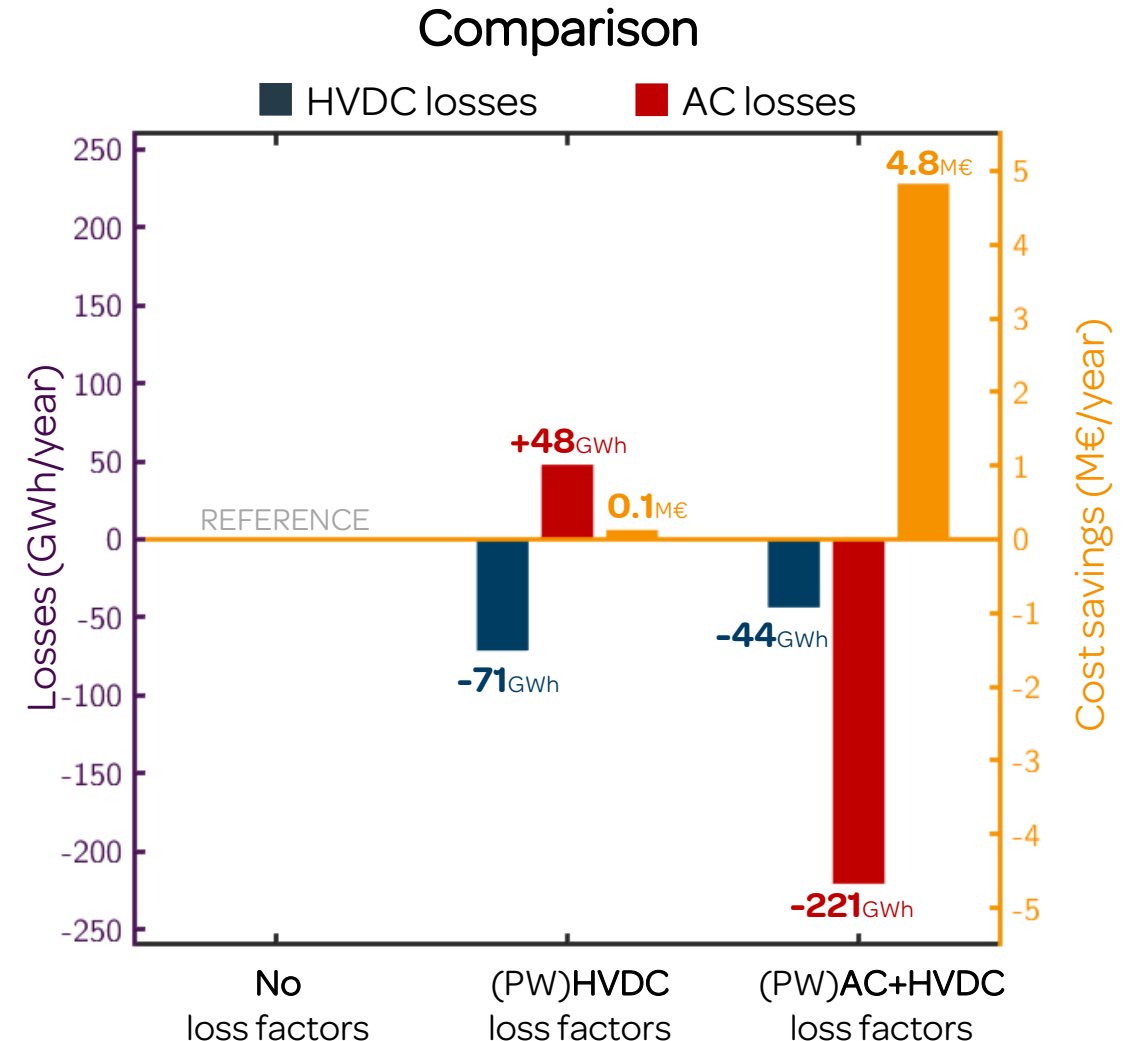
- The utilization of linear loss factors leads to an overestimation of losses.

Extra power = extra costs



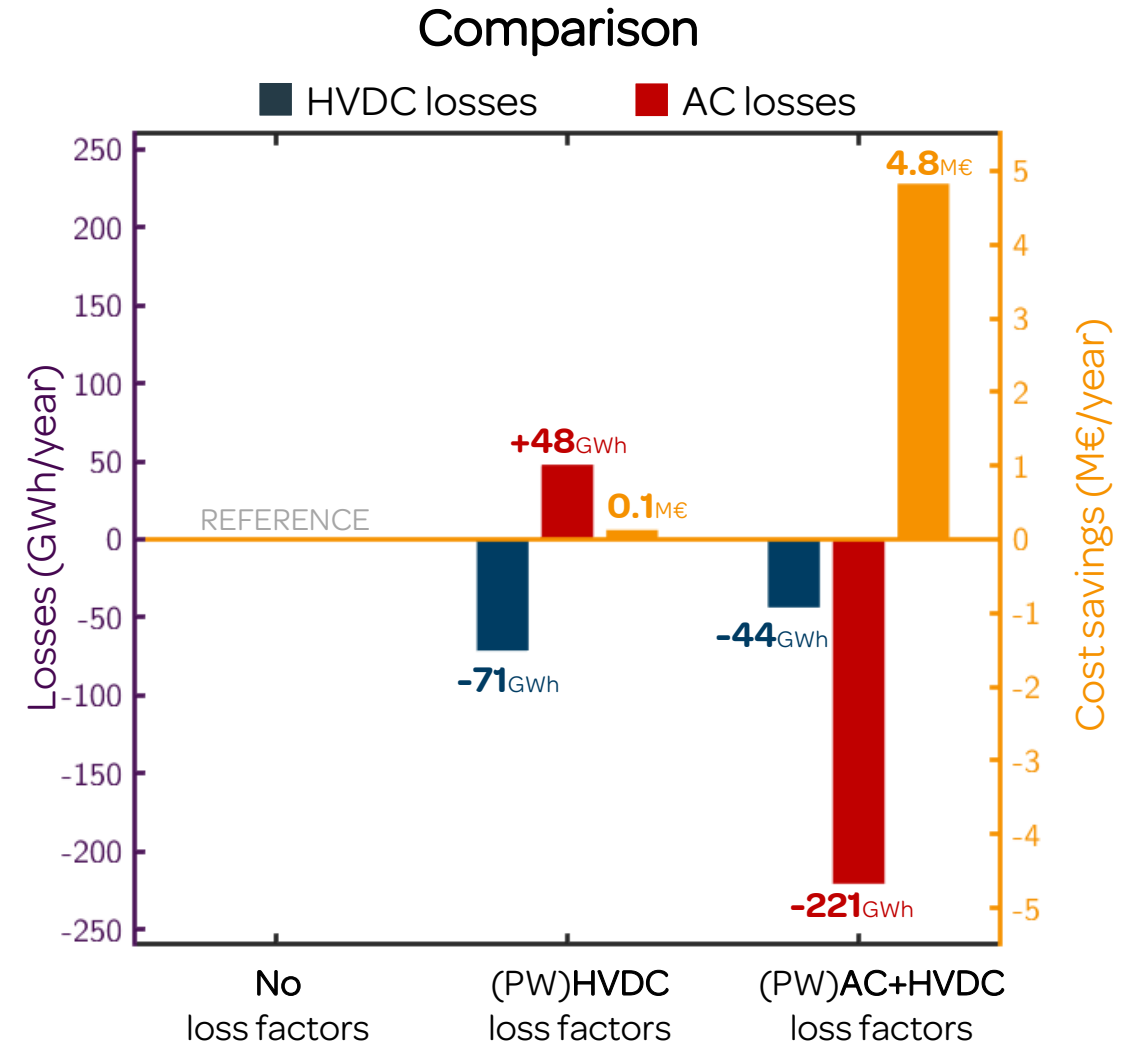
HVDC vs. AC+HVDC (piecewise-linear loss factors)

- With piecewise-linear loss factors loss functions are **better represented**.
- Only the **necessary power** is purchased in the market.
- With both AC and HVDC piecewise loss factors, the total losses are **minimized (-12.1%)**, resulting in cost savings of **4.8 million** Euros.



HVDC vs. AC+HVDC (piecewise-linear loss factors)

- With piecewise-linear loss factors loss functions are **better represented**.
- Only the **necessary power** is purchased in the market.
- With both AC and HVDC piecewise loss factors, the total losses are **minimized (-12.1%)**, resulting in cost savings of **4.8 million** Euros.
- **Recommendation**: introduce loss factors for **AC interconnectors** as well.



Main takeaways

1. Piecewise linear loss factors **better represent** the quadratic loss functions and allow for a **better distribution** of power flows.
2. Losses are **minimized** only if both AC and HVDC loss factors are introduced.
3. Internalizing losses results in cost savings for **TSOs** and for the **society**.





Thank you for the attention!

Andrea Tosatto
antosat@elektro.dtu.dk



PSCC2020

multiDC

