

# Security-Constrained Optimal Power Flow including Post-Contingency Control of VSC-HVDC lines

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# IRENE-40 European Project

- Infrastructure Roadmap for the **E**nergy **N**etworks in **E**urope for the next **40** years

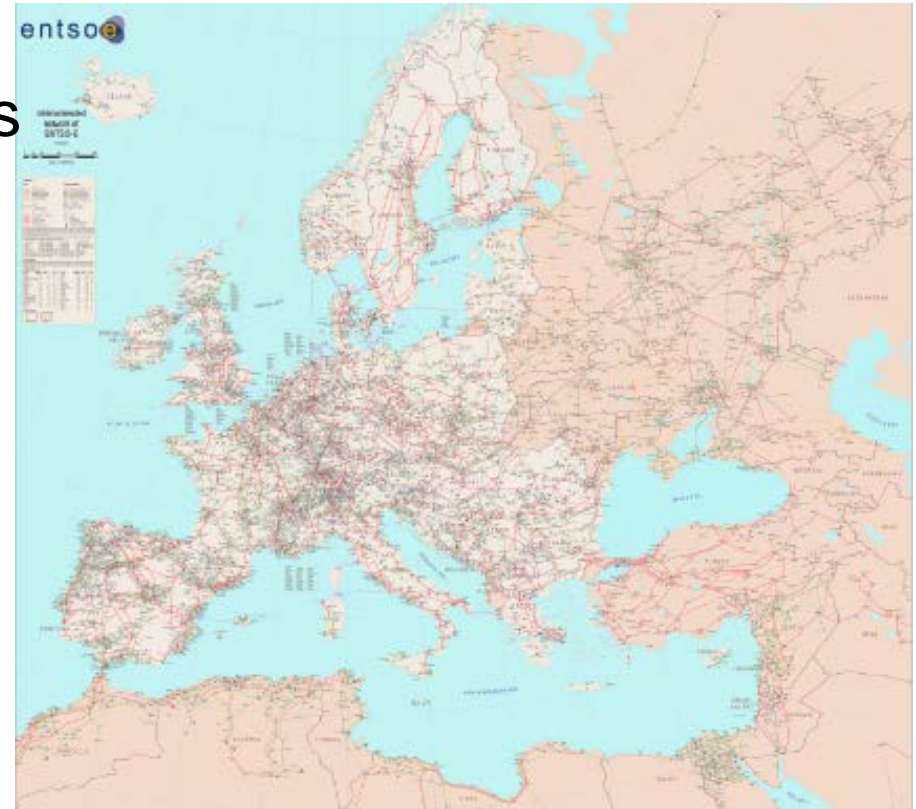


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- Partners:
  - 5 European Universities:  
RWTH Aachen, Imperial College, Delft, NTUA, ETH Zurich
  - ABB, Siemens, Alstom, Energy Center of the Netherlands

# IRENE-40

- Identify expansion measures with respect to:
  - Sustainability → more RES
  - **Security**
  - Competitiveness → efficient market operation
- Possible Options:
  - AC Lines, FACTS devices, HVDC lines, regulatory measures, etc.



## “Cost of Security” Index

- The “Cost of Security” represents the additional generation dispatch costs, in order to satisfy the N-1 criterion.
- Compare the total generation costs resulting from a Security-Constrained Optimal Power Flow (SC-OPF) and from a standard AC Optimal Power Flow (AC-OPF)
- Cost of Security =  
$$\text{Gen.Costs (SC-OPF)} - \text{Gen.Costs (AC-OPF)}$$
- Goal: find the *least* “Cost of Security”

## Motivation

VSC-HVDC lines can act fast and actively relieve line overloadings after a contingency

## Therefore:

We need a Security-Constrained OPF,  
which takes into account the increased control capabilities of  
the VSC-HVDC lines after a contingency.

\*VSC: Voltage-Source Converter technology



# OUTLINE

## 1. Method

## 2. Case Studies

- Operation: 10-bus network
- Planning: European Network

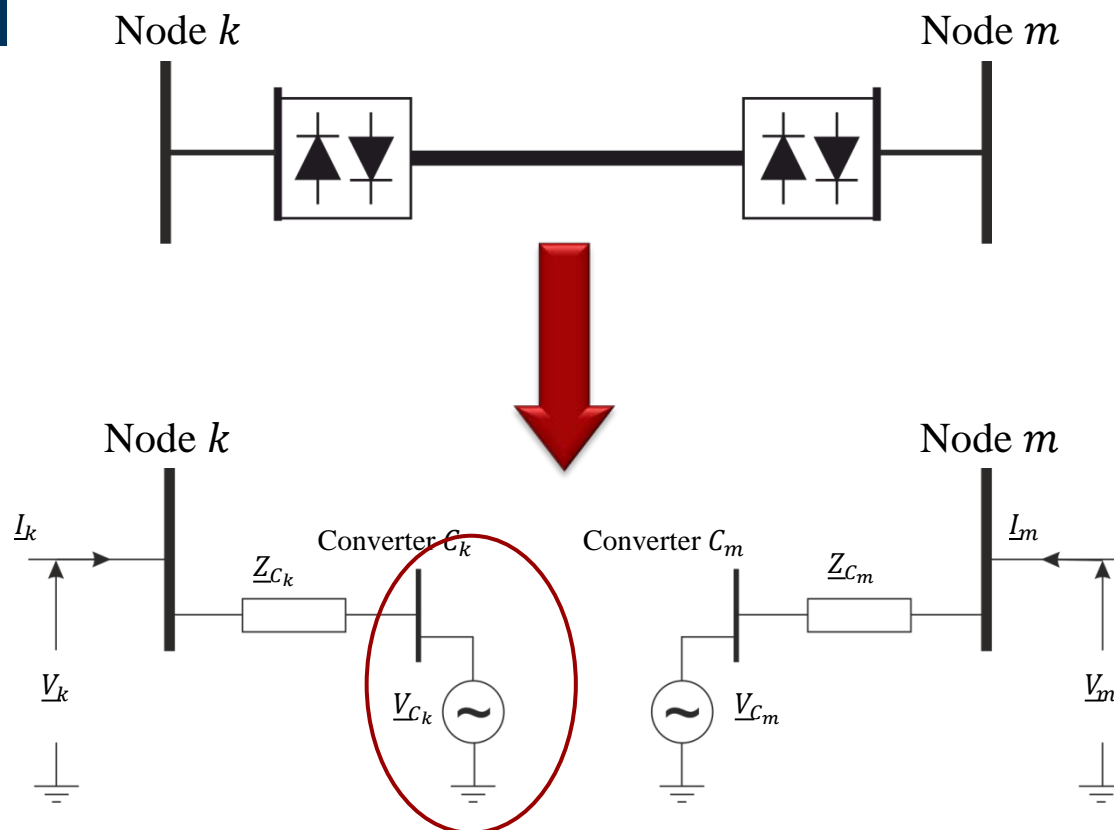
## 3. Conclusions

# Proposed Security-Constrained OPF (SC-OPF)

- The proposed SC-OPF is based on the current injection method for the calculation of the line currents in case of a line outage.
1. Standard AC-OPF
  2. Model for VSC-HVDC lines
  3. Current Injection Method
  4. Extension for VSC-HVDC Post-Contingency Control
  5. Extension for increased accuracy

## VSC-HVDC Model

- Two virtual nodes for each HVDC line
- Each converter represented by a voltage source
- Constraint for the exchanged active power



$$P_k + P_m + P_{DC,loss} = 0$$

Based on Pizano-Martinez et al.,  
IEEE TPS, 2007

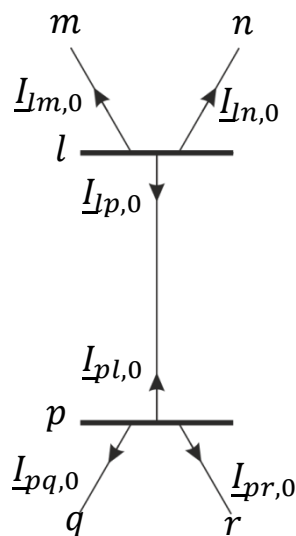


# Current Injection

- Virtual injection currents eliminate the flow on the outaged line

pre-fault

$$\underline{V}_0 = \underline{Z}_0 \cdot \underline{I}_0$$



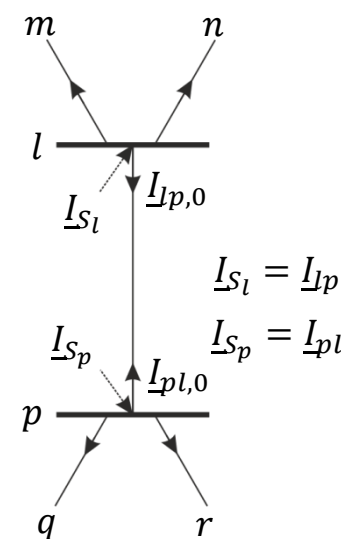
post-fault

$$\underline{V}_F = \underline{Z}_F \cdot \underline{I}_F$$



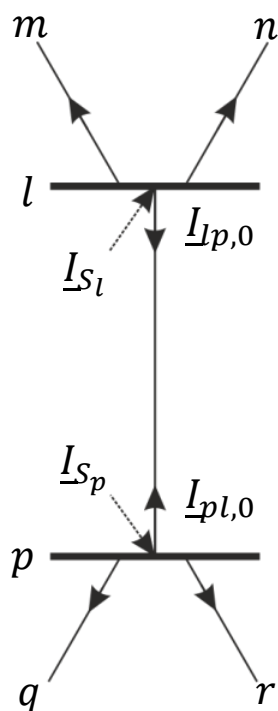
$$\underline{V}_F = \underline{Z}_0 \cdot (\underline{I}_F + \underline{I}_S)$$

≈



post-fault

$$\underline{V}_F = \underline{Z}_0 \cdot (\underline{I}_F + \underline{I}_S)$$



Change in  
line flows

$$\Delta \underline{I}_{line} = \underline{Y}_L \cdot \Delta \underline{V} = \underline{D} \cdot \underline{I}_S$$

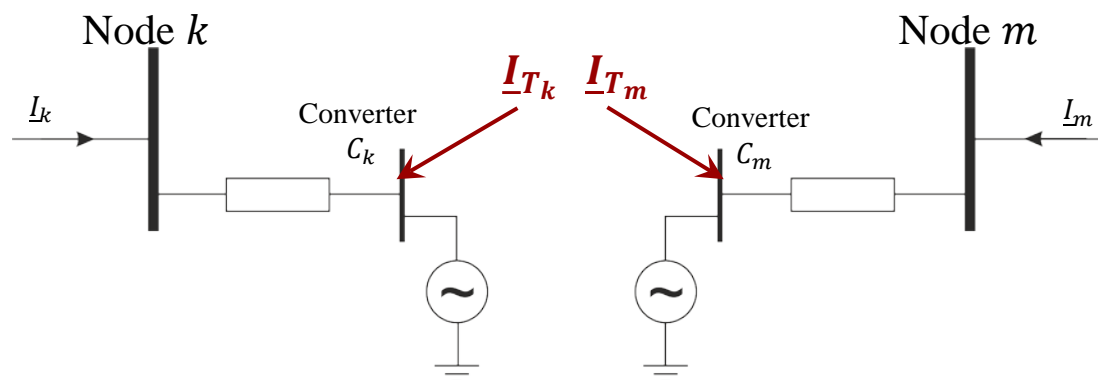
- Main Assumption:

Bus injections  
*before* the outage  
e.g. gens, loads

$$\underline{I}_0 = \underline{I}_F$$

Bus injections  
*after* the outage  
e.g. gens, loads

# HVDC for post-contingency control

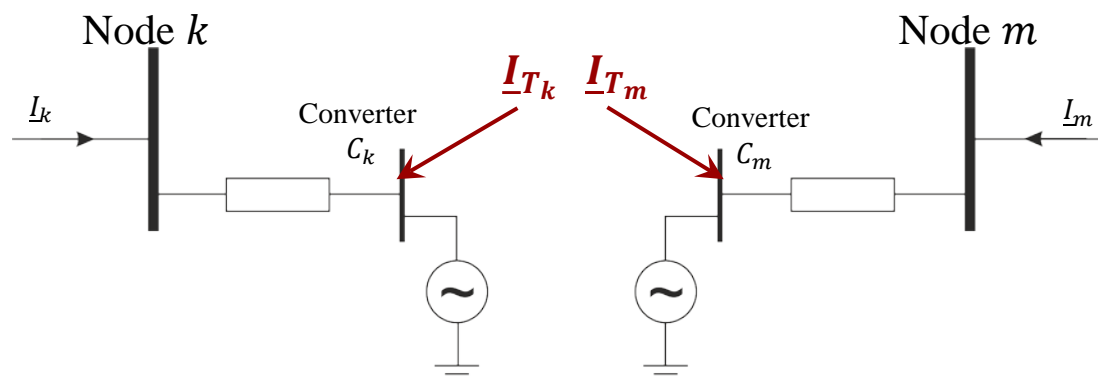


- If an HVDC “participates” during the outages:

$$\underline{I}_{0,\text{HVDC}} \neq \underline{I}_{F,\text{HVDC}}$$

Bus Current Injections  
at HVDC nodes are no  
longer zero

# HVDC for post-contingency control



- With VSC-HVDC, we can control:
  - The active power flow, in order to relieve overloadings on other lines (one additional optimization variable)
  - The reactive power flow, in order to keep the voltage at the HVDC buses to a pre-determined setpoint

## Extension for increased accuracy

- In reality:

$$\text{pre-fault} \quad \underline{I}_0 \neq \underline{I}_F \quad \text{post-fault}$$

*for all buses.*

$$\underline{I}_T = \begin{bmatrix} \underline{I}_{T_1} \\ \underline{I}_{T_2} \\ \vdots \\ \underline{I}_{T_i} \\ \vdots \\ \underline{I}_{T_n} \end{bmatrix}$$

- We assume an additional current  $\underline{I}_{T_i}$  for each bus, so that:
  - P and Q remain constant at PQ buses
  - P and V remain constant at PV buses
  - V and  $\delta$  remain constant at slack buses

(extension proposed by Hug, Andersson, PSCC 2008)

## SC-OPF Wrap-up

- Determine the injection currents  $\underline{I}_S, \underline{I}_T$
- Calculate the line flows after the fault

$$\underline{I}_{line,post-fault} = \underline{I}_{line,0} + D \cdot (\underline{I}_S + \underline{I}_T)$$

- Include them in the constraints
- Additional constraints of the AC-OPF
- Additional constraints for the HVDC model



# OUTLINE

## 1. Method

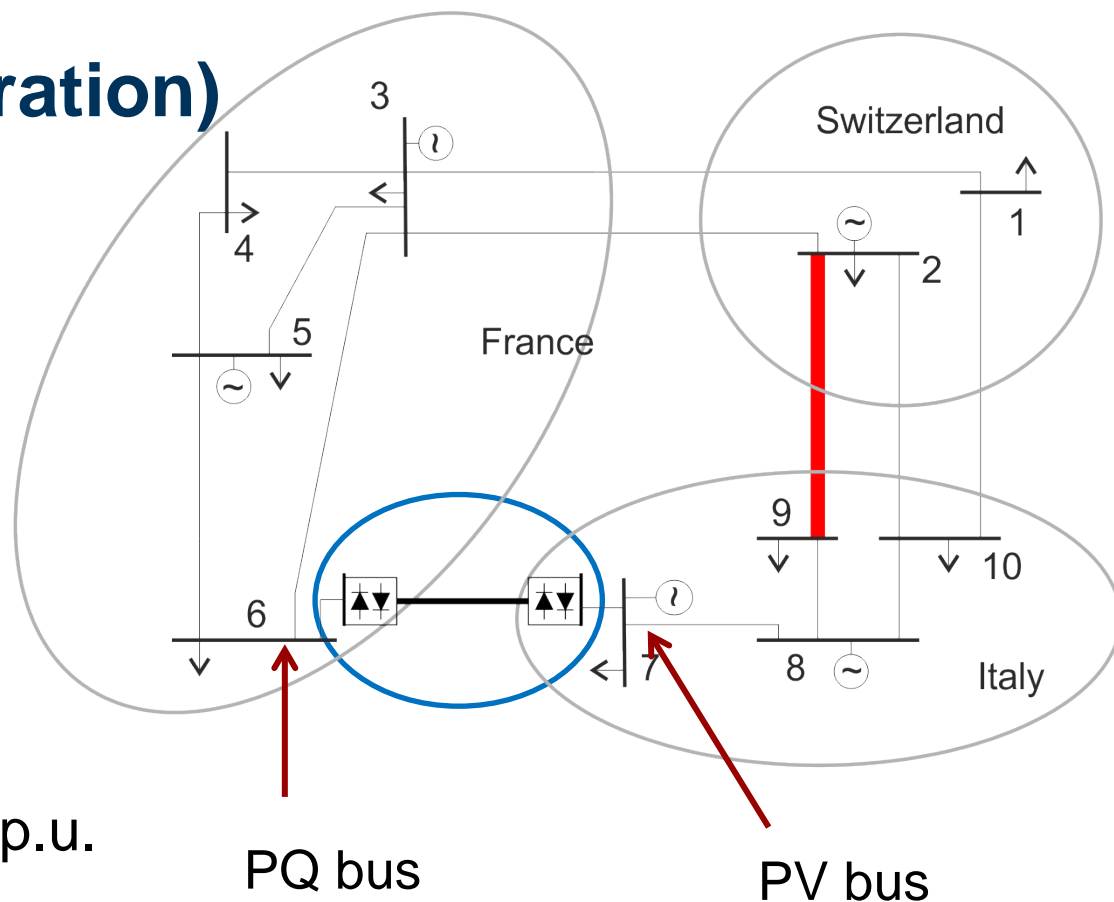
## 2. Case Studies

- **Operation: 10-bus network**
- **Planning: European Network**

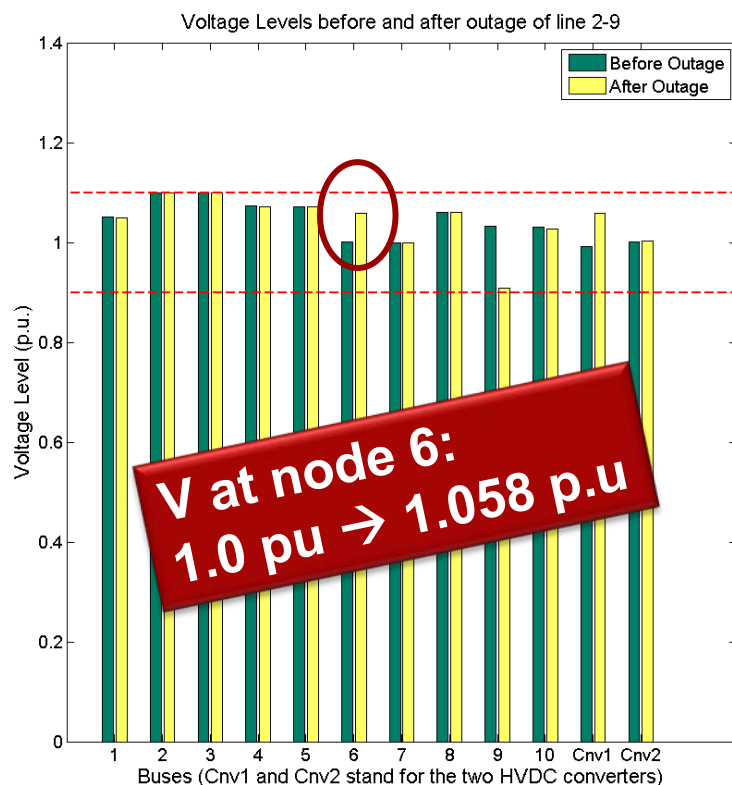
## 3. Conclusions

## Case Study #1 (operation)

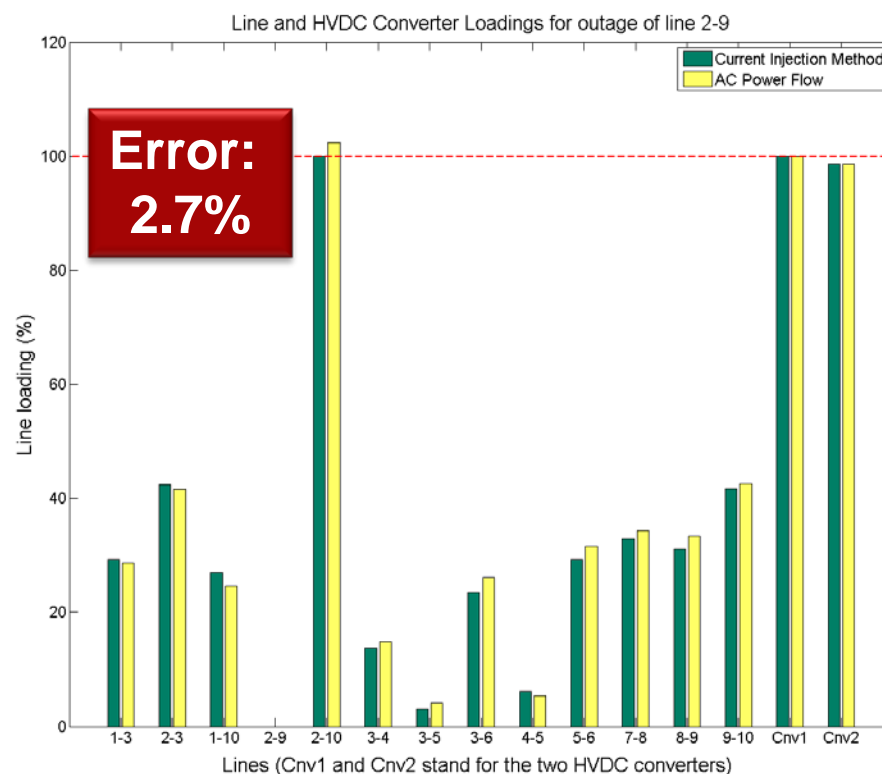
- Outage of Line 2-9
- HVDC at nodes 6-7
  - Node 6: PQ bus
  - Node 7: PV bus
- Post-contingency
  - Node 6 Voltage: 1.05 p.u.



# Bus Voltages pre-fault vs. post-fault

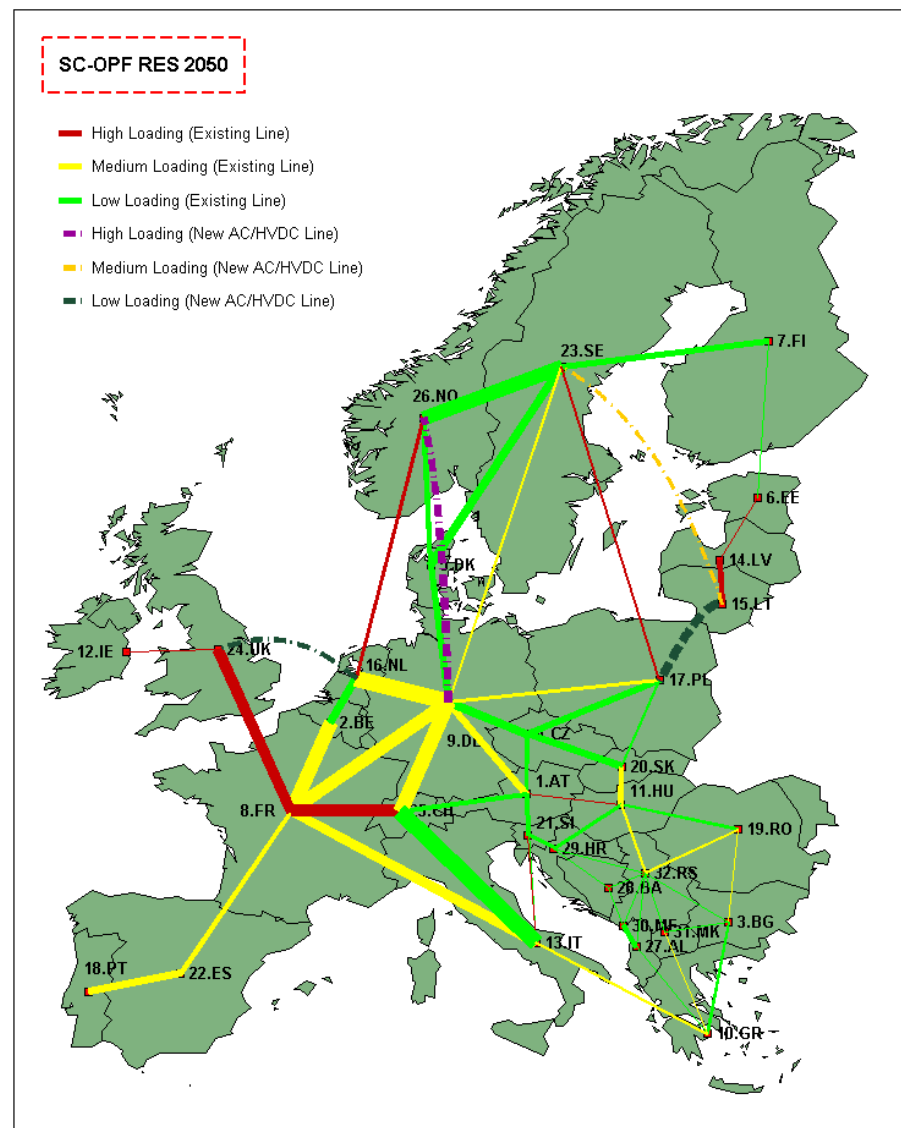


# Post-Fault Line Flows: Current Injection vs. AC power flow



## Case Study #2 (planning): European Network

- 32 nodes, 104 branches, ~100 generators
- Generation Scenario: 80% RES in 2050
- SC-OPF: 12 most critical outages
- Addition of:  
3 HVDC+1 AC



## Case #2: Cost of Security with post-contingency control [PCC]

	No Expansion	Addition of 1 AC + 3 HVDC lines
Standard AC-OPF	9.52 million €/h	9.50 million €/h
SC-OPF with PCC	10.61 million €/h	10.52 million €/h
<b>Cost of Security</b>	<b>1.09 million €/h</b>	<b>1.02 million €/h</b>
<b>Reduction in Cost of Security</b>	<b>6.4%</b>	

*Cost of Security: Additional generator re-dispatch costs, so that the N-1 criterion can be satisfied*

**~300-600 million Euros per year can be saved**


## Case #2: Cost of Security with and without PCC

	Cost of Security	Reduction in Cost of Security
<b>No expansion</b>	1.09 million €/h	---
<b>Expansion <i>without</i> PCC</b>	1.08 million €/h	1 %
<b>Expansion with PCC</b>	1.02 million €/h	6.4 %

\*PCC = Post-contingency control



# Conclusions

- Algorithm which integrates in a *single* optimization problem:
  - a Security-Constrained OPF including VSC-HVDC lines, and
  - calculates the control actions of multiple VSC-HVDC lines after line outages (post-contingency control)
- The algorithm can be used in both operation and planning studies  the “Cost of Security” index has been introduced for the planning studies
- The control capabilities of the VSC-HVDC lines have the potential to significantly decrease the “Cost of Security”.

# Obrigado!



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